# Optimizing Subduction Zone Monitoring

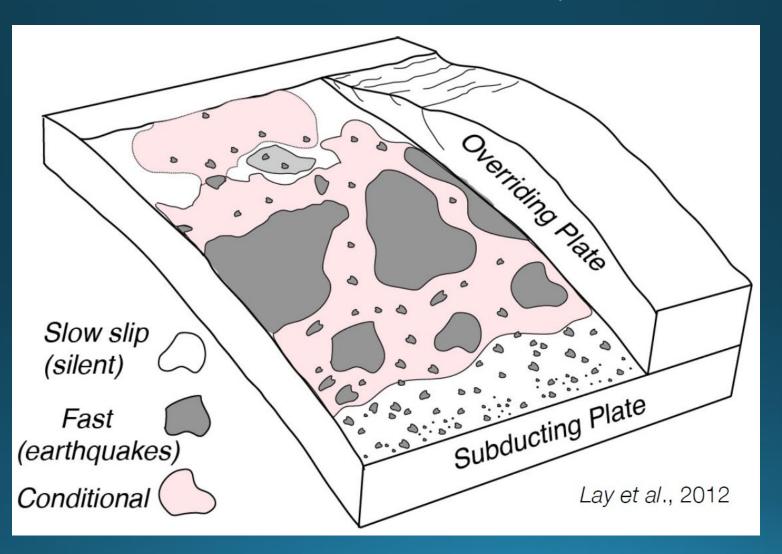
Sarah Minson
On behalf of Eileen Evans and Ben Brooks





#### Locking, slow slip, and in between

$$\dot{s}_{\mathrm{locked}} = \dot{s}_{\mathrm{tectonic}} - \dot{s}_{\mathrm{slow/creep}}$$

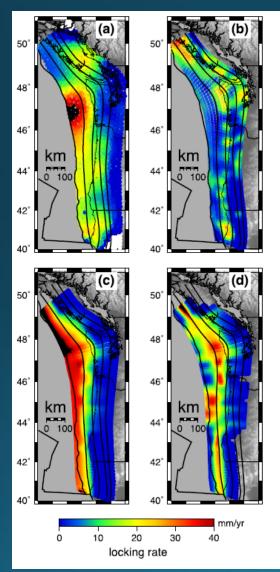


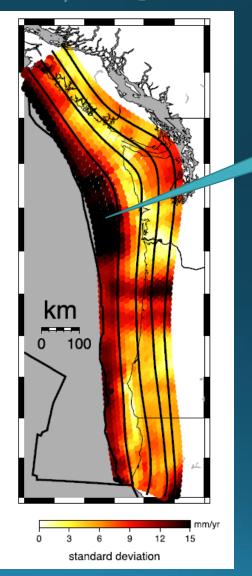
#### Locking, slow slip, and in between

$$\dot{s}_{\mathrm{locked}} = \dot{s}_{\mathrm{tectonic}} - \dot{s}_{\mathrm{slow/creep}}$$

Locking rates from *Pollitz* and Evans, 2017

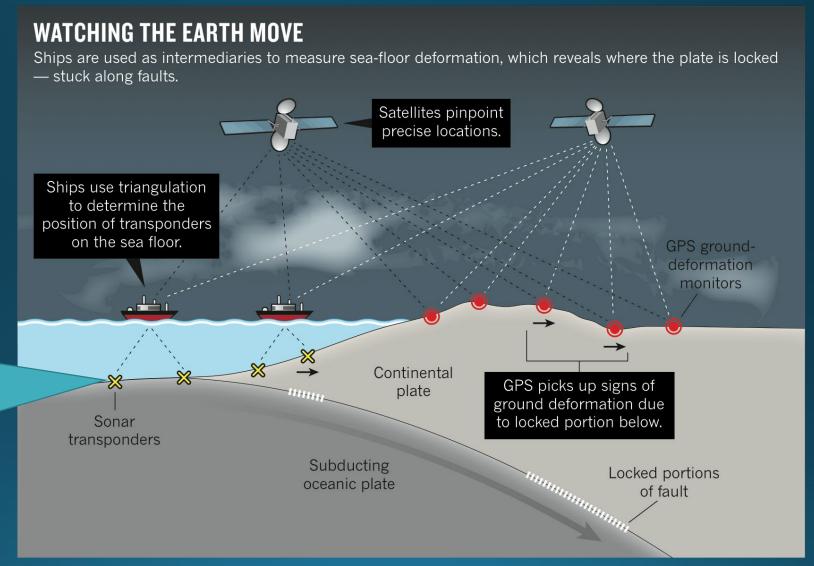
Locking rates from *McCaffrey et al., 2013* 

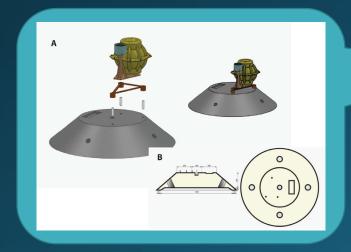


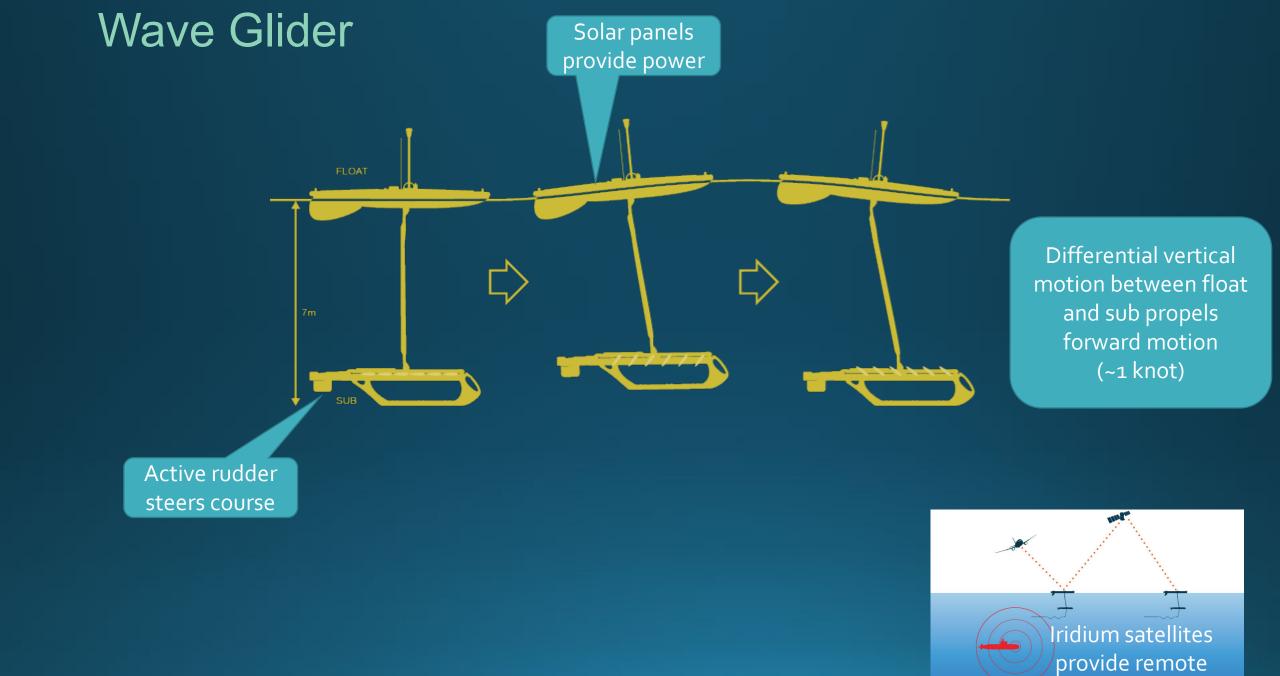


Uncertainty greatest at trench: ±15-20 mm/yr

# Seafloor Geodesy – GPS Acoustic (GPS-A)







command and control

#### What can we observe?

- GPS/A
  - Principally sensitive to horizontal motion
  - Sub-centimeter precision after 3-4 days of observation
- Seafloor pressure gauges
  - Sensitive to vertical motion
  - Centimeter-level precision
- Other sensors in various stages of development (e.g., seafloor strain)
- Modes of operation:
  - Repeat occupation (ship, wave glider)
    - Limited frequency of observation, very expensive
  - Continuous telemetry
    - Requires frequent battery changes, and sometimes additional infrastructure (e.g., buoy), even more expensive
  - Cabled (continuous telemetry and power)
    - So very expensive
      - The mode you choose will determine what kind of transients/precursors (if any) you can observe
- Have to make every observation count
  - Let's try calculating information entropy or differential entropy (Shannon 1948)

## Information entropy

 Information entropy (Shannon, 1948) is the amount of missing information about the value of a parameter:

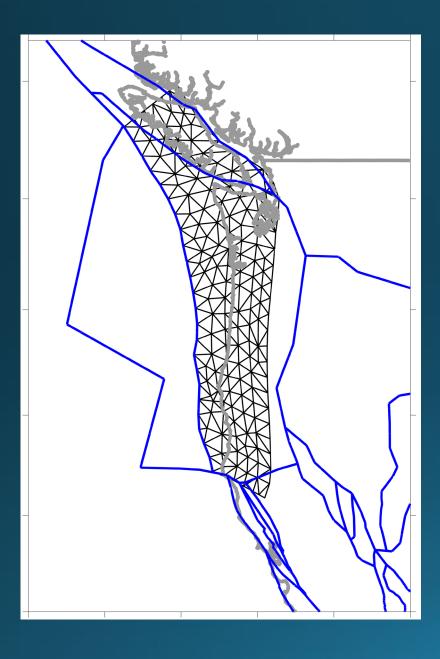
• 
$$\mathbf{H} = -\int_{x}^{x} f(x) \ln f(x) dx$$

For Gaussian statistics/linear inverse problems:

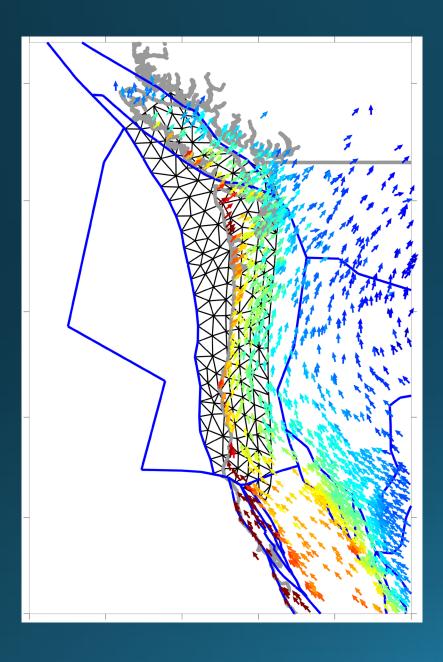
• 
$$f(x) = \mathcal{N}(x|m^*, \Sigma^*) \rightarrow \mathbf{H} = \frac{1}{2} \ln \det(2\pi e \Sigma^*)$$

- H is a function of the posterior model covariance matrix, which depends on the inversion design:
  - For determining distributed slip,  $\Sigma^* = C_m^* = \left[C_m^{-1} + G^T C_d^{-1} G\right]^{-1}$
  - For determining total moment deficit,  $\Sigma^* = \sum_{i=1}^p \sum_{j=1}^p C_{m_{i,j}}^*$
- Goal: Find observation locations that minimize entropy

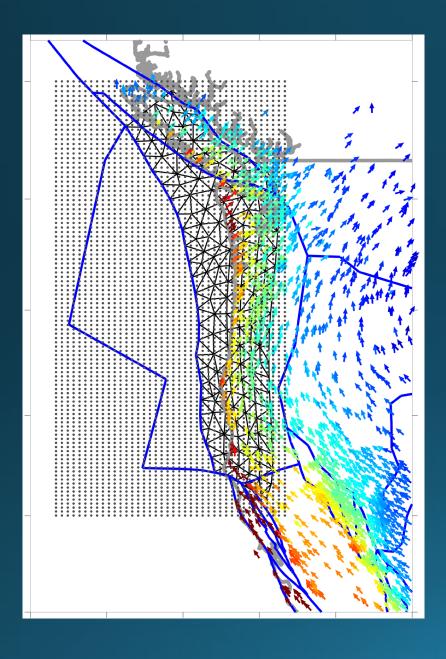
G is model design matrix  $C_d$  is data covariance  $C_m$  is a priori model covariance



- Block model
  - Divide crust into microplates bounded by faults (e.g., Meade & Hager, 2005)
  - Mesh of triangular dislocations (e.g., Meade and Loveless, 2009)
- Constraints
  - Currently: 4213 GNSS velocities (*Kreemer et al.*, 2014)
  - 4000 potential observation locations

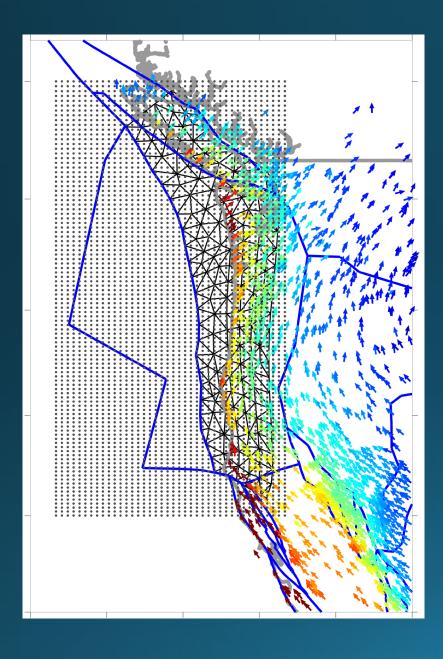


- Block model
  - Divide crust into microplates bounded by faults (e.g., Meade & Hager, 2005)
  - Mesh of triangular dislocations (e.g., Meade and Loveless, 2009)
- Constraints
  - Currently: 4213 GNSS velocities (*Kreemer et al.*, 2014)
  - 4000 potential observation locations

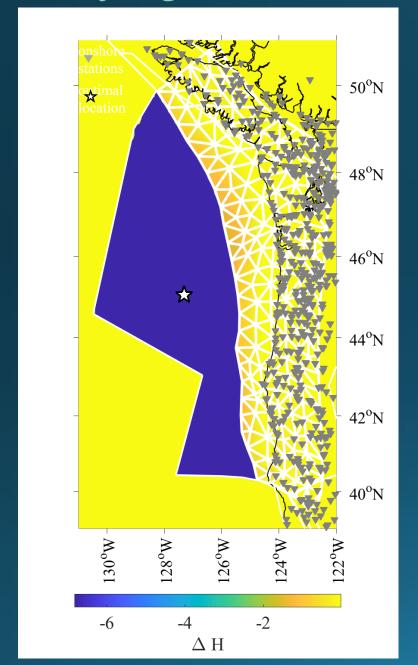


- Block model
  - Divide crust into microplates bounded by faults (e.g., Meade & Hager, 2005)
  - Mesh of triangular dislocations (e.g., Meade and Loveless, 2009)
- Constraints
  - Currently: 4213 GNSS velocities (*Kreemer et al.*, 2014)
  - 4000 potential observation locations

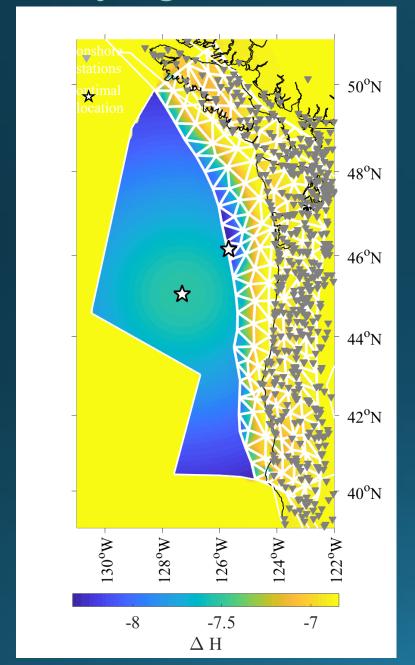
Which potential observation locations minimize information entropy?



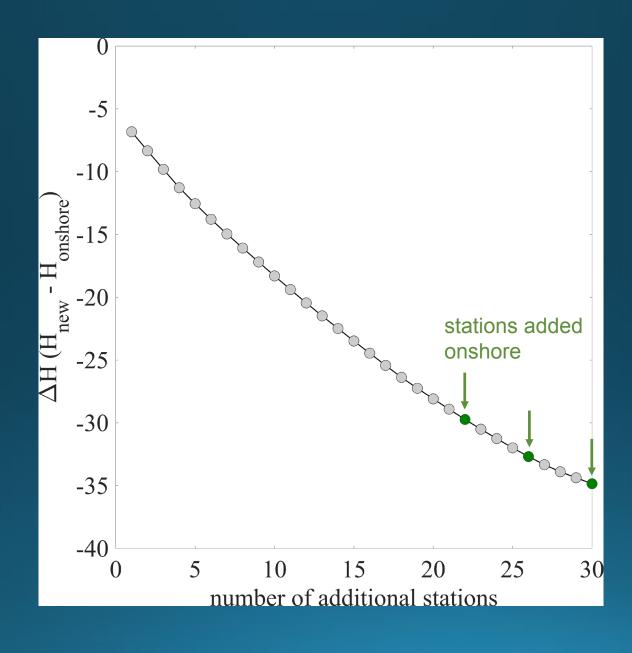
- Data uncertainties:
  - Existing uncertainties as reported (*Kreemer et al.*, 2014)
  - New offshore: **±3 mm/yr** (*Chadwell and Spiess*, 2008)
  - New onshore: ±0.85 mm/yr (mean of existing uncertainties)
- Model uncertainties
  - Euler pole: **±0.1°** Lat, Lon
  - Triangular slip distribution: ±20 mm/yr
  - Laplacian smoothing

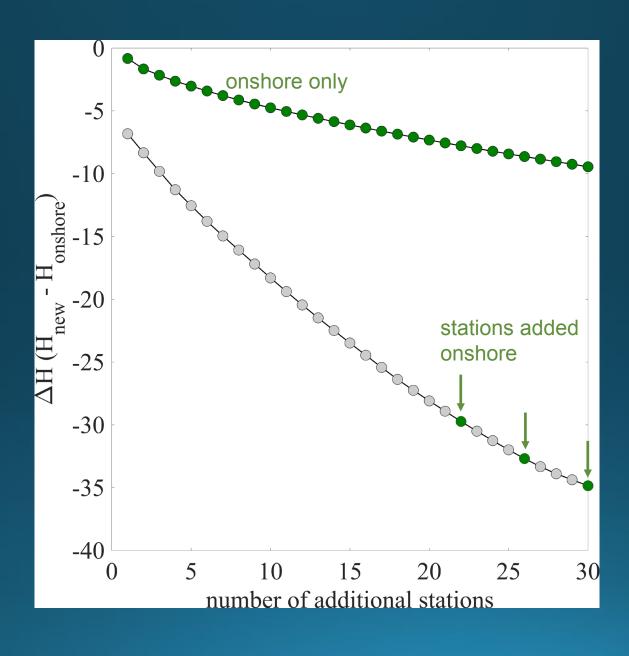


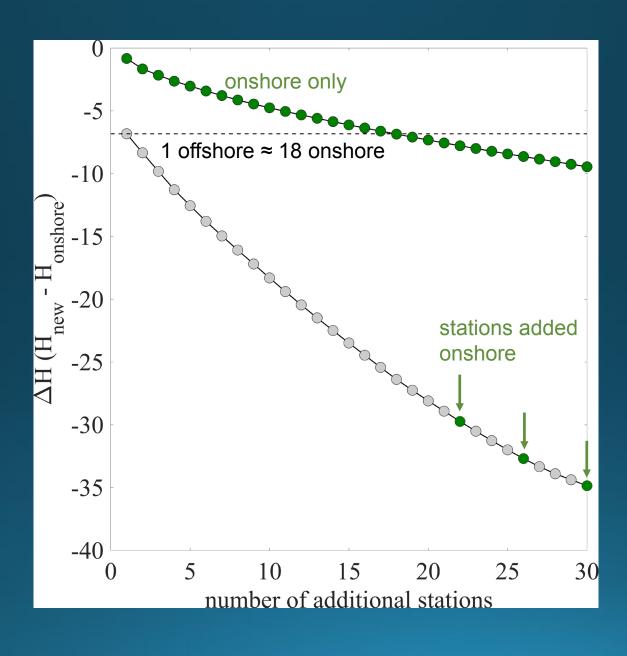
- $\Delta \mathbf{H} = \mathbf{H}_{new} \mathbf{H}_0$ , relative to current onshore network
- First minimum ∆H (most new information) on Juan de Fuca plate
  - This is for understanding interseismic coupling. If, e.g., we asked what is the total moment deficit, we could get a different answer.
- Subsequent stations along trench
- First onshore location after 21 offshore
- Distribution depends on model assumptions, previously selected locations



- $\Delta \mathbf{H} = \mathbf{H}_{new} \mathbf{H}_0$ , relative to current onshore network
- First minimum ∆H (most new information) on Juan de Fuca plate
  - This is for understanding interseismic coupling. If, e.g., we asked what is the total moment deficit, we could get a different answer.
- Subsequent stations along trench
- First onshore location after 21 offshore
- Distribution depends on model assumptions, previously selected locations







## Summary

- 27 of first 30 optimal observation locations are offshore
- Single offshore station provides information gain of 18 onshore stations

#### Considerations

- What is the entropy reduction per \$?
- What is the cost of obtaining a seafloor GPS/A reading vs. traditional telemetered onshore GPS stations?
- How often and for how long would we need to visit transponders to be able to observe transitory seismic precursors with desired accuracy?