

# An embedded Recursive SIR model for County Level Analysis

*The National Academies of*  
SCIENCES • ENGINEERING • MEDICINE

**Virtual Workshop on Geospatial Needs for a Pandemic-Resilient World**  
**Mapping Science Committee**

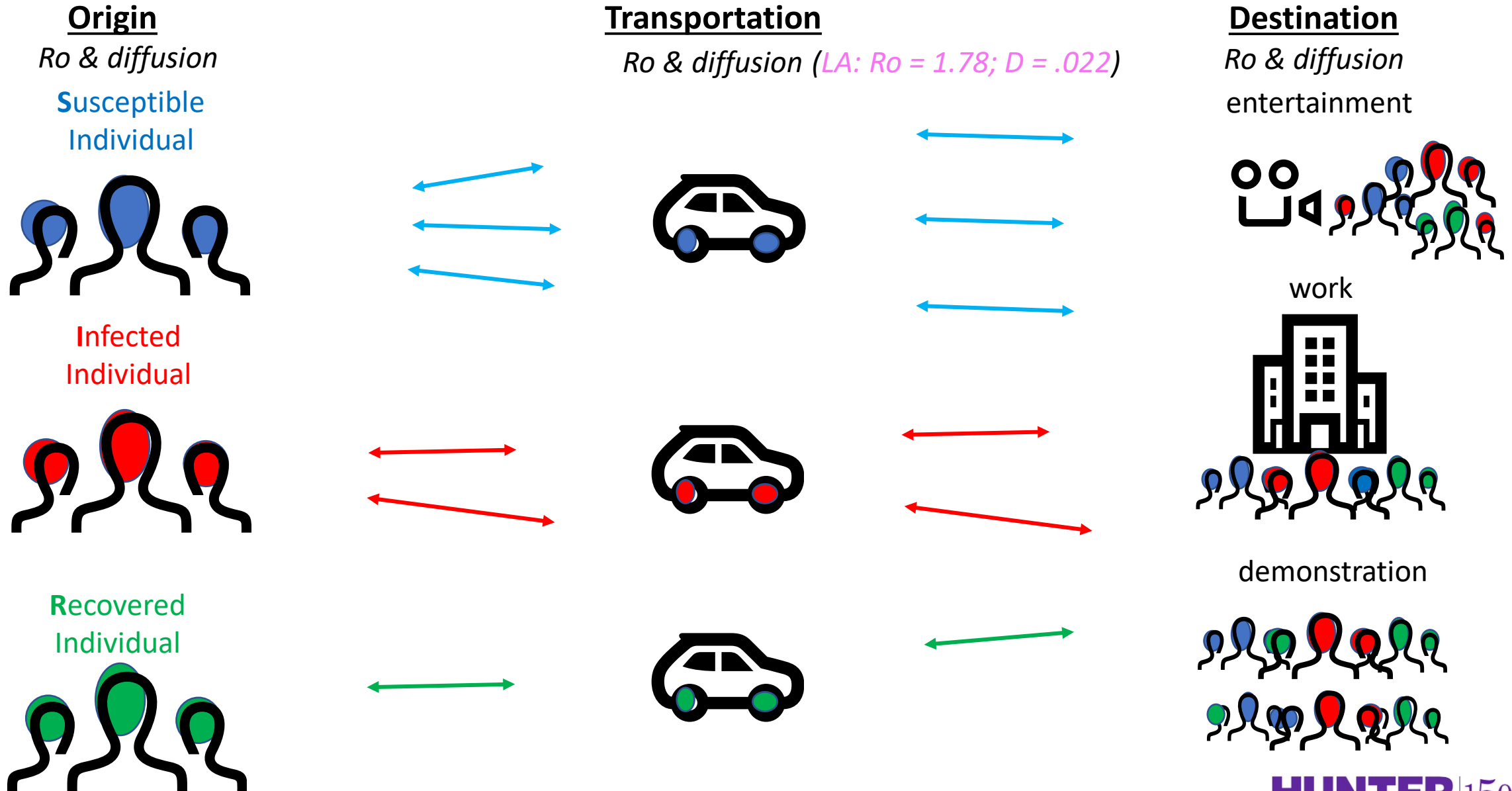
June 17, 2020  
1:00–5:15 pm eastern

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# Modeling Covid 19 Spread

- What approach to modeling?
  - Data driven
    - Poor data
    - No constraint on “what is possible”
    - Can result (and did) in gross overestimations of deaths
  - Epidemiological Model
    - Poor data but contextualized within epidemiological framework
    - Epidemiology captures process of viral spread and attenuation
    - Model provides constraint on “what is possible”.

# Conceptual Model (SIR)



# Conceptual Model (SIR)

## Origin

*Ro & diffusion*

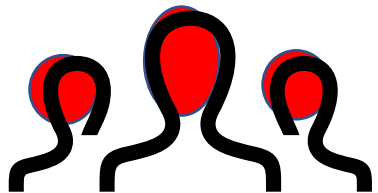
Susceptible

Individual



Infected

Individual



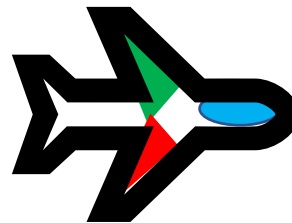
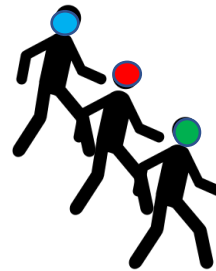
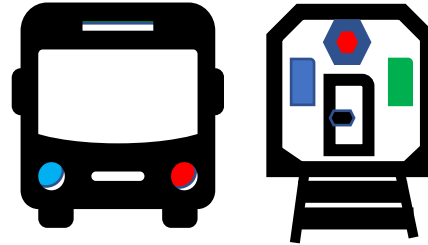
Recovered

Individual



## Transportation

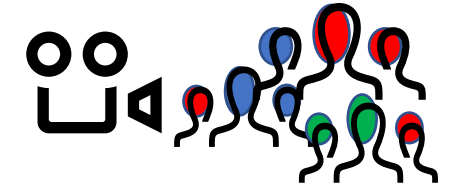
*Ro & diffusion (NYC:  $R_0 = 2.6$ ;  $D = .107$ )*



## Destination

*Ro & diffusion*

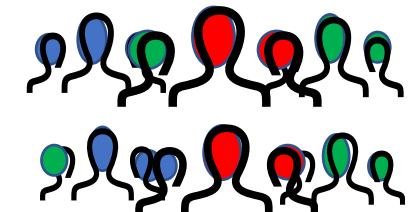
entertainment



work



demonstration





# Goal: Understand and reduce transmission & predict the trajectory of the virus's impact

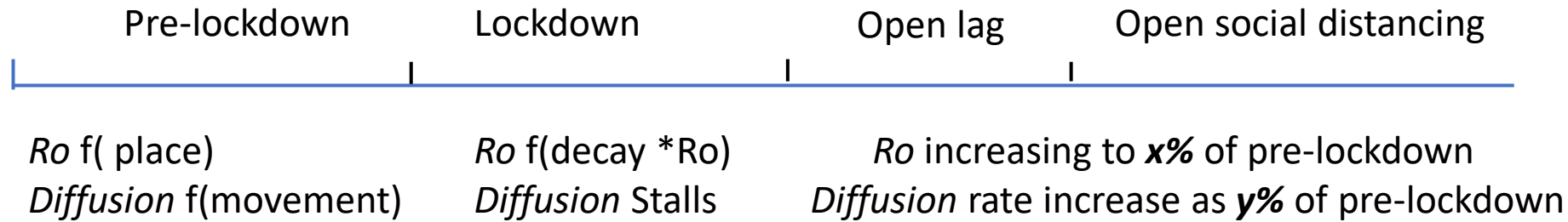
*Modeling and prediction*

- What is the transmission rate of individuals? **Ro**
- How dispersed is the interaction of individuals? **Diffusion**

# Logical Model

- Use classic SIR Model (modified)
    - Susceptible – Infected - Removed
  - Model deaths, not case data, due to lack of testing
  - Model every county separately
  - Establish parameters (assumptions)
    - Death rate = 0.023 (South Korea)
    - Initial infection rate =  $i_0$  = .00125
    - Duration from S  $\rightarrow$  I  $\rightarrow$  R .....  
 $\nu$  = 0.071428 (21 days)
  - Calculated parameters using embedded recursion
    - $R_0$  - # individuals infected by an infected individual
    - *Diffusion*: # rate of spread of virus.  
i.e. what percent of population is exposed to virus?
- $$P = (1 / (1 + (\exp(-\beta \cdot t) * (1 - i_0) / i_0)))$$

# Calculated Parameters: Ro and Diffusion



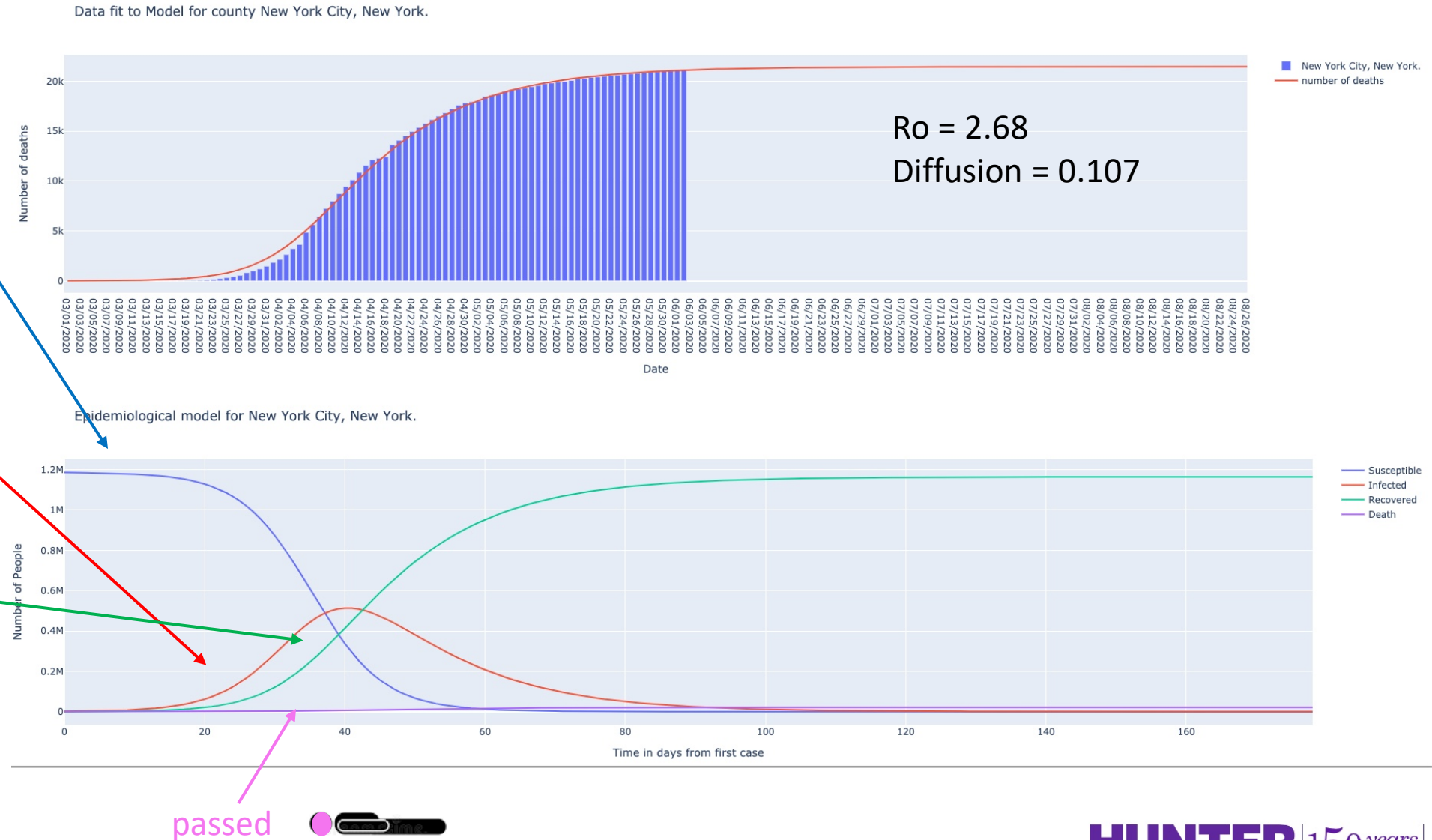
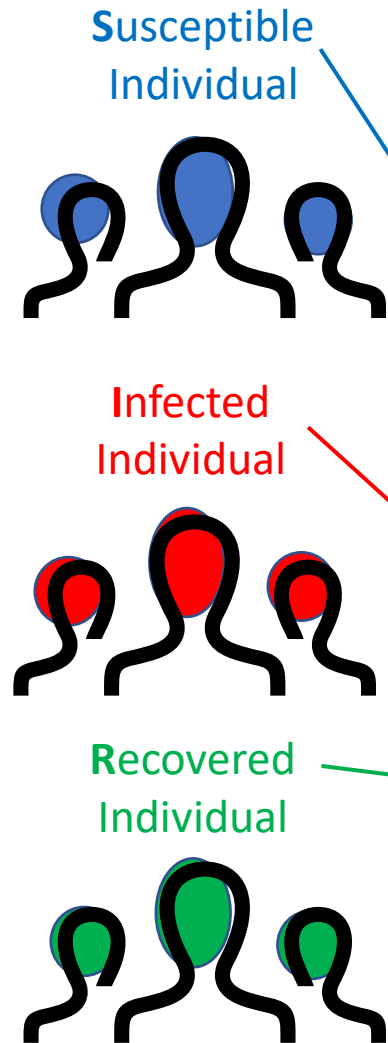
# Imbedded Recursive SIR Model (CARSI Model)

*Classic SIR model with recursive Curve Fitting of  $R_0$  and Diffusion*



# Modeling the spread and predicting the future

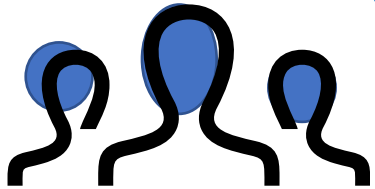
## Embedder Recursive SIR model (CARSI model): initial diffusion



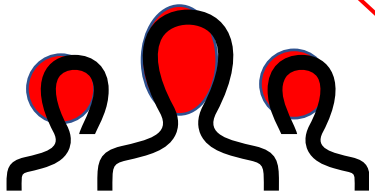
# Modeling the spread and predicting the future

## Embedder Recursive SIR model (CARSI model): increased diffusion

Susceptible  
Individual



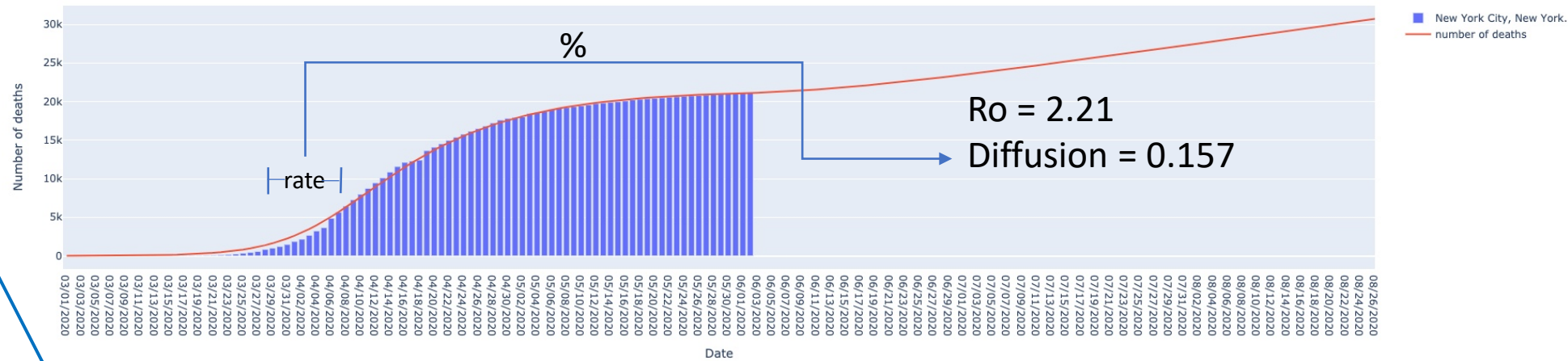
Infected  
Individual



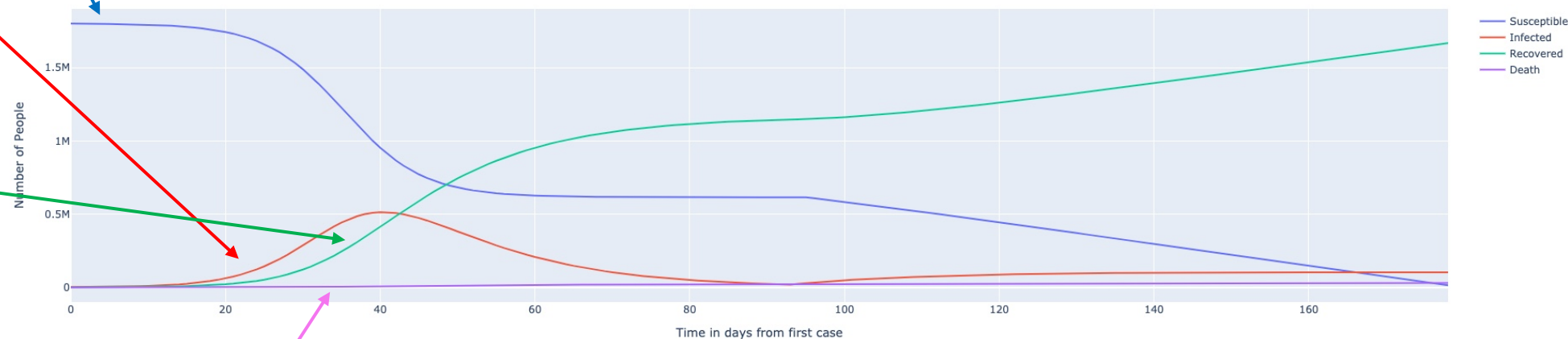
Recovered  
Individual



Data fit to Model for county New York City, New York.



Epidemiological model for New York City, New York.



passed

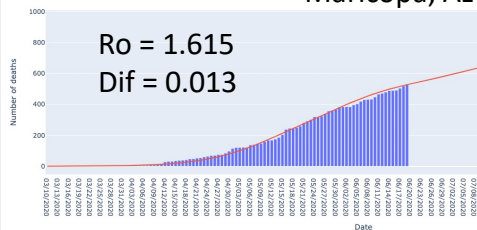




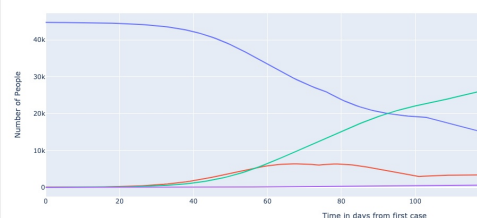


Data fit to Model for county Maricopa, Arizona.

## Maricopa, Az



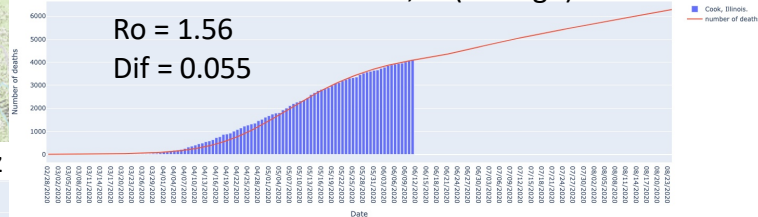
Epidemiological model for Maricopa, Arizona.



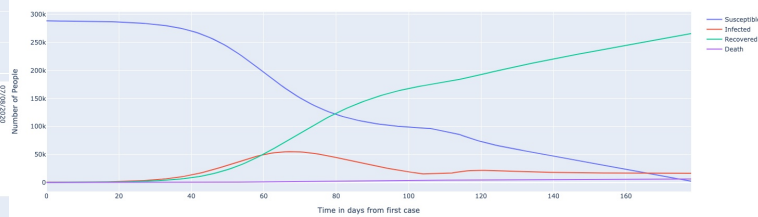
Data fit to Model for county Cook, Illinois.

$R_0 = 1.56$   
 $Dif = 0.055$

## Cook, Ill (Chicago)



Epidemiological model for Cook, Illinois.



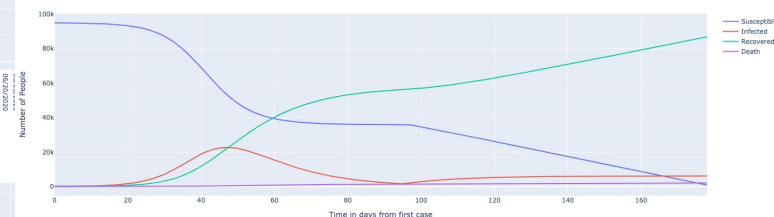
Data fit to Model for county Fairfield, Connecticut.

## Fairfield, Ct

$R_0 = 2.317$   
 $Dif = 0.10$

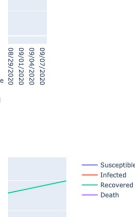


Epidemiological model for Fairfield, Connecticut.



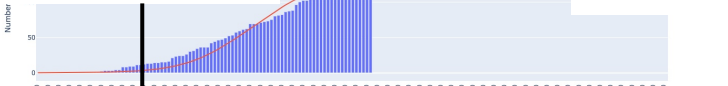
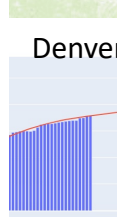
Data fit to Model for county Franklin, Ohio.

## Franklin, Ohio



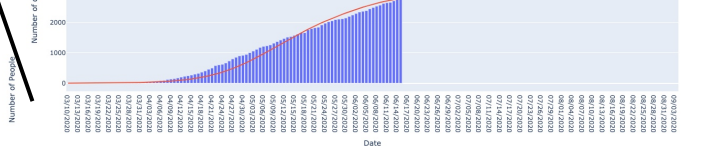
Data fit to Model for county Denver, Colorado.

## Denver, Colo



## Los Angeles, Ca

$R_0 = 1.78$   
 $Dif = 0.022$



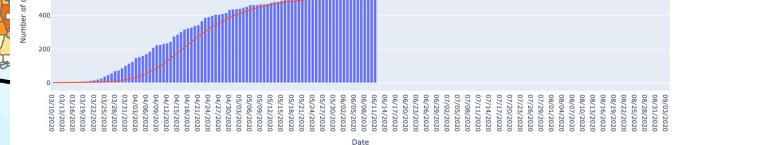
Epidemiological model for Los Angeles, California.



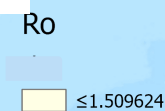
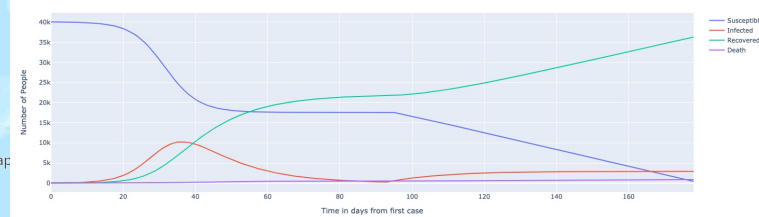
Data fit to Model for county Orleans, Louisiana.

## New Orleans

$R_0 = 3.063$   
 $Dif = 0.104$



Epidemiological model for Orleans, Louisiana.



# Bottom-line predictions

Sum for all counties:

$$\sum_1^{3000} (\# \text{ deaths in each county} \mid \text{SIR model prediction})$$

For August 7, 2020 estimate = 172,303



# Problem for prediction

How to estimate values of  $R_0$  and *Diffusion* going forward?

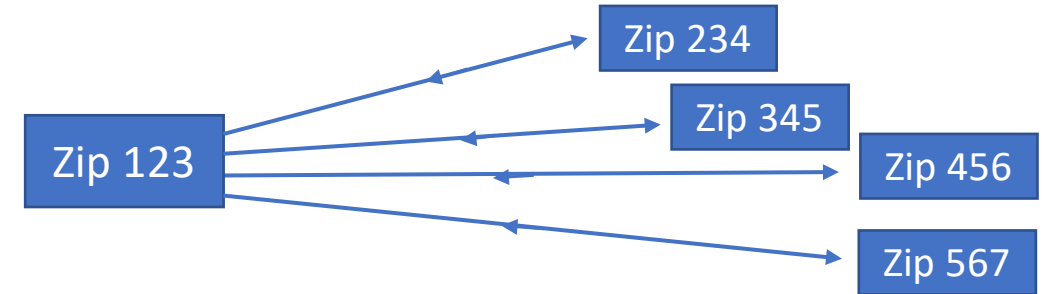
# New Sources of Movement Data

- Movement data of individuals from apps has been consolidated to capture movement from origin to destination(s) (*diffusion*)
- Proximity of devices (*Ro*)
- These data can be used to calibrate both *diffusion* and *Ro* by relating it to model output.

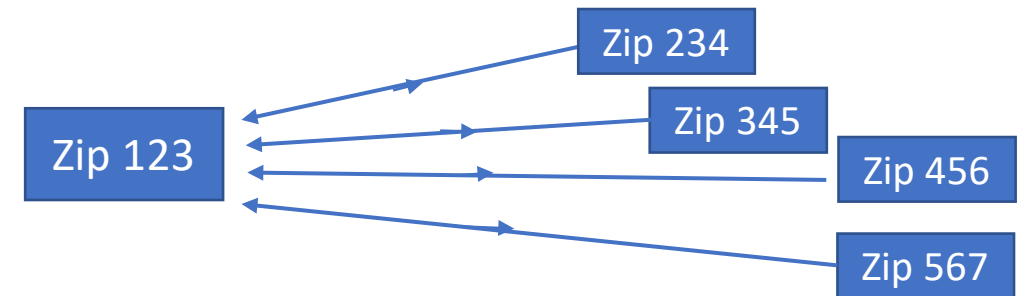
# Metrics: calibrate Ro and Diffusion from real-time device data

## Diffusion

**To:** # of zip codes visited by the population in a given zip code



**From:** # of zip codes that visitors come from that are visiting this zip code.



Sum of **To** & **From** normalized by population.

# Metrics: calibrate $R_0$ and $Diffusion$ from real-time device data

## $R_0$

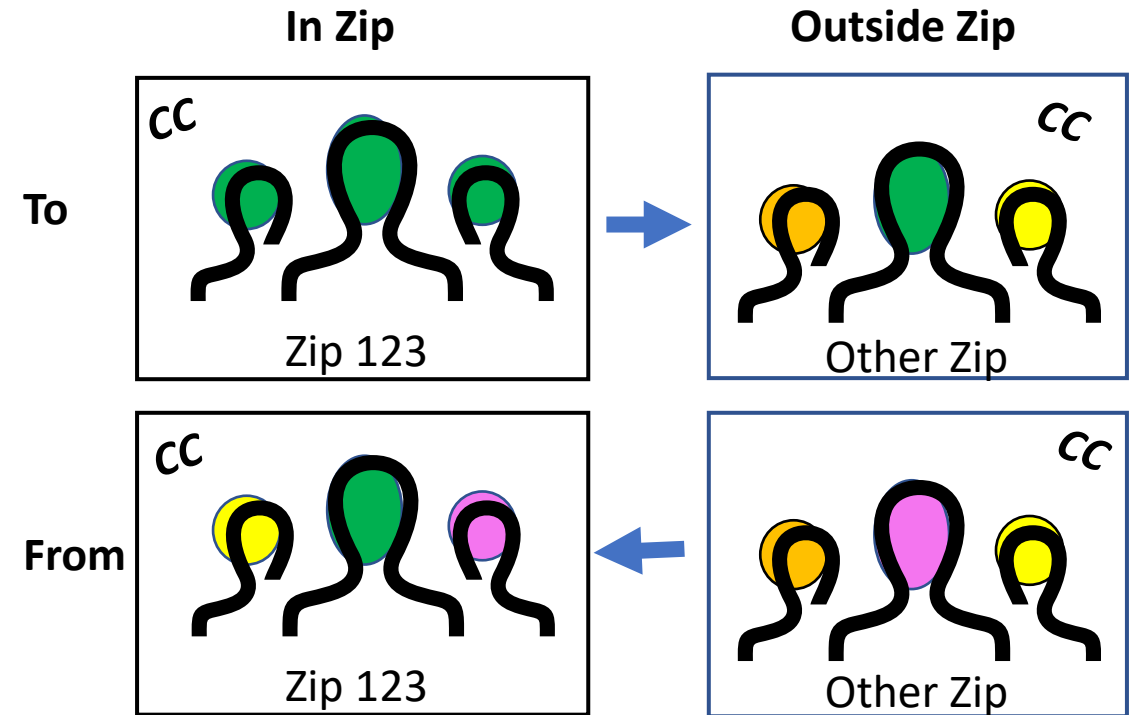
**To - In:** close contacts (CC) of a device within the zip for someone who **lives in** the zip code

**To - Out :** are the close contacts (CC) of individuals within the zip when they are outside the zip code

**From-In:** are CC of a person in a zip code for someone who lives **outside** the zip code

**From-Out:** are CC of a person for a visitor of a zip code when they are outside the zip code

Sum of matrix normalized by population



# What geographic correlates relate to Ro and Diffusion?

- Demographics
  - Income
  - Age
  - Car ownership
- Institutions
  - Nursing homes
  - Prisons
  - Public housing
- Corporate
  - Meat packing
  - Factories
- Transportations systems
  - Cars, subway, bus
- Movement to and from a county or other geo-unit
- Prevalence in surrounding counties

*What is the best level of granularity for these analysis?*

# Conclusion

- A modified Recursive SIR Model (CARSI model) was used to predict Covid19's trajectory into the future
- New mobile data sources are now available to calibrate two key parameters of the model: *R<sub>0</sub>* and *diffusion*.
- Process-based models have the advantage of constraining predictions to realistic scenarios of what is likely and possible



# Questions?

- Thanks to the New York Times for organizing the county level data used in this research
- Thanks to Harvey Miller & Anne Linn for organization of the workshop.

