

# Power Flow Application in Power Systems

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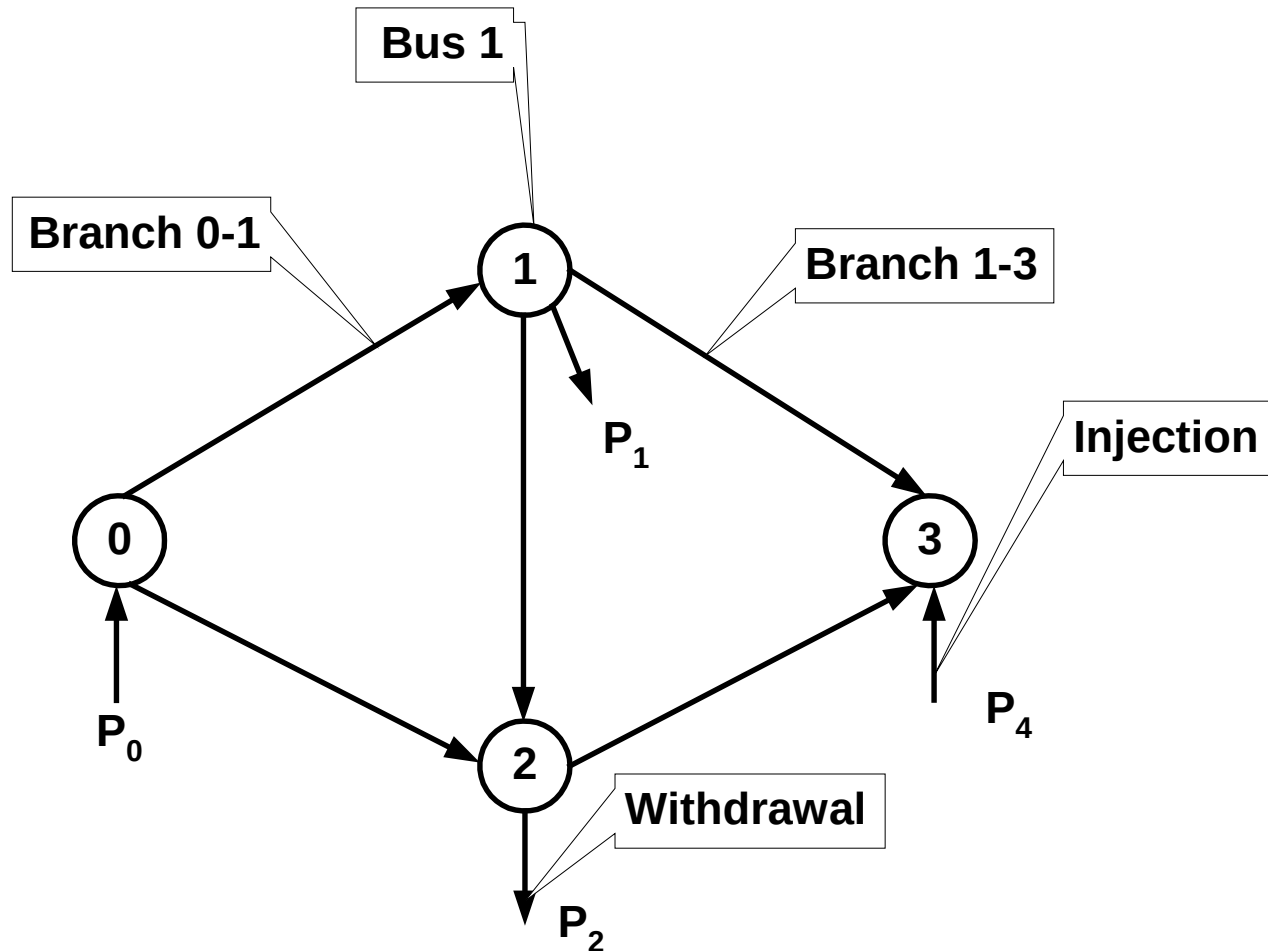


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# Electrical Network and its Model



# Network Model

- Bus – connection point of two or more branches in the network model
- Branch – physical or equivalent line connecting two buses
- Injection – flow of power into the bus – generation
- Withdrawal – flow of power from the bus – load



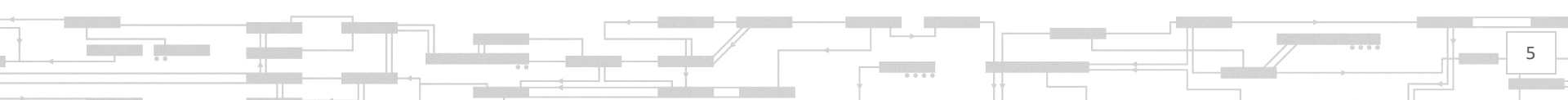
# Power Flow

- Power Flow is the most frequently used type of study applied to Power System operation and planning
- It is needed to make sure that the analyzed system state is compliant with the established reliability criteria
- Used to evaluate different scenarios in long- and short-term planning
- Power system state monitored variables are:
  - Voltages at every bus
  - Power Flows at every transmission line and transformer

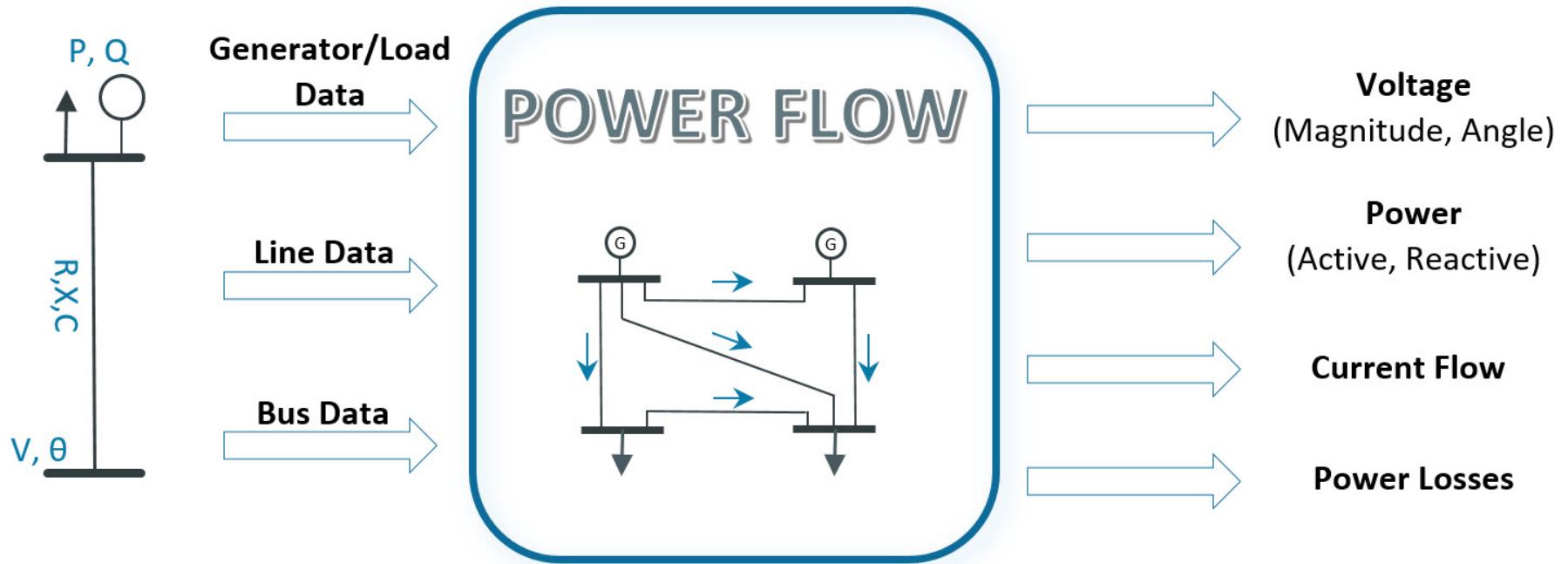


# Power Flow Calculation

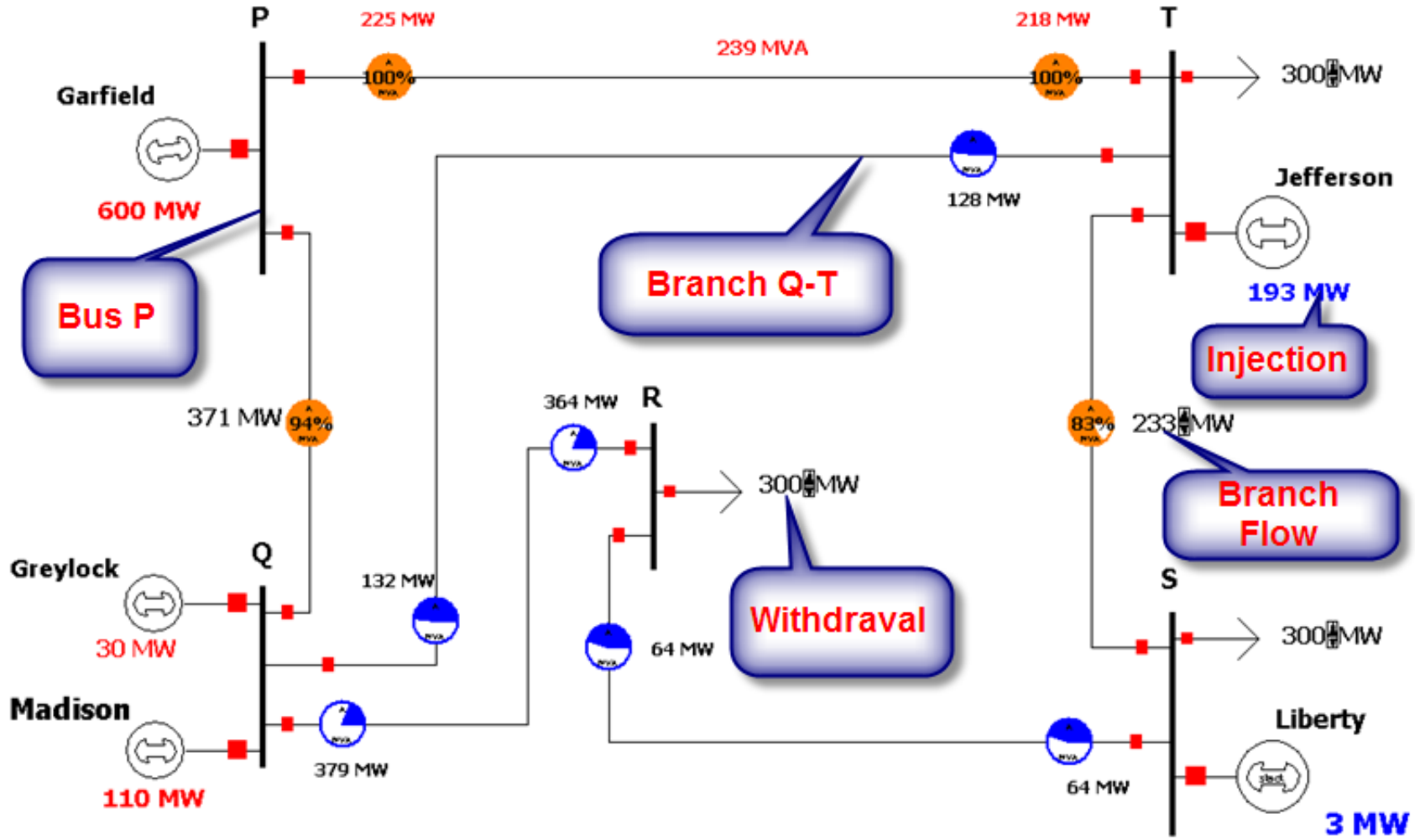
- Given: injections and withdrawals at every bus, branch parameters, network topology
- Find: power flows and currents in each branch and voltage at each bus
- High voltage electrical networks are three-phase alternate current circuits.
- The theory of power systems provides ways to perform calculations with one-line models for symmetric conditions.
- Complex numbers are used to represent an alternate current circuit variables
- Power Flow calculation implements a numerical solution of the model describing the steady state of the system
- The result is a **feasible** solution – making sure there are no violated reliability constraints



# Power Flow Problem

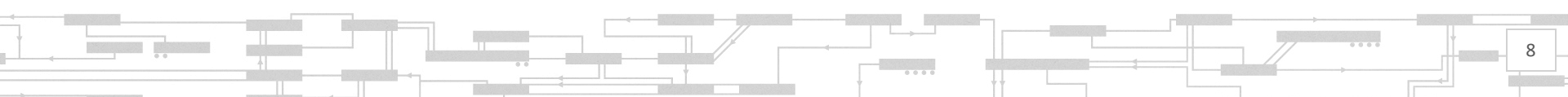


# Power Flow Solution



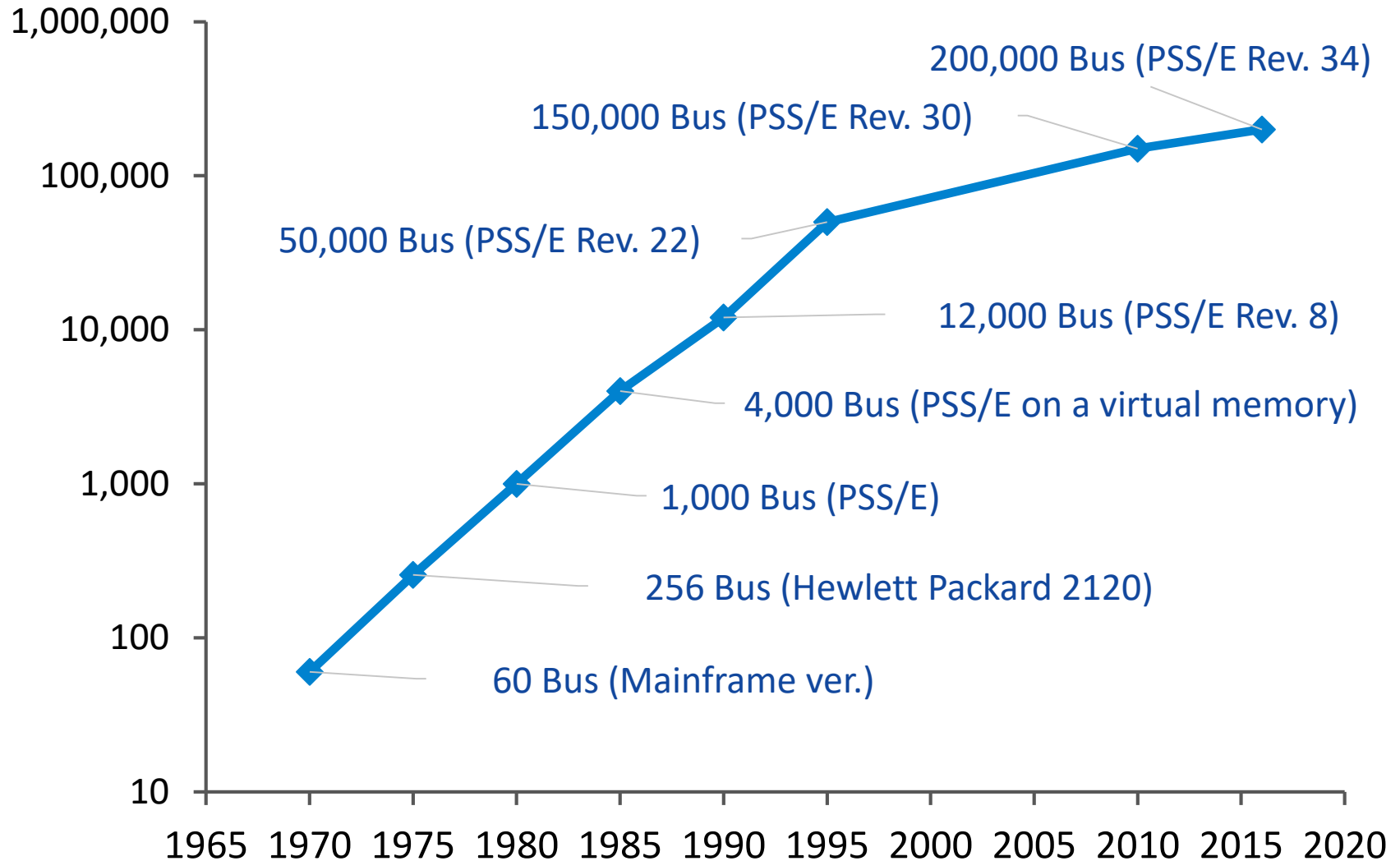
# Solving the Power Flow Problem

- Power Flow is described by the system of nonlinear algebraic equations with complex variables and therefore cannot be solved analytically
- Each equation is representing a power balance at each bus. Ohm's and Kirchhoff's laws are used to formulate the problem
- Power Engineers operate with power (voltage\*current) rather than currents while specifying generation and loads, therefore the nonlinear system
- Different numerical methods are used to solving these equations
- As any numerical solution of the non-linear system, it may not converge, so special measures are needed to make it more robust
- The most popular method is Newton-Raphson
- The size of the problem is quite large and requires using sparse matrix technique



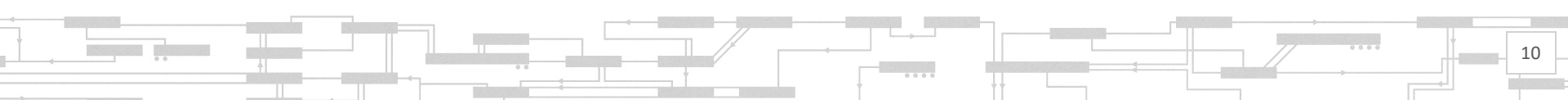


# PF Software Evolution (System Size)



# Optimal Power Flow (OPF)

- Finding a feasible solution that simultaneously satisfies certain objective function:
  - Minimize losses
  - Maximize transfer capability
  - Maximize social welfare or minimize the cost of production
- For almost all practical purposes, OPF should be used instead of traditional Power Flow. Application was limited by the lack of computational power
- This requires some cultural change for power system engineers who are used to run multiple PF solutions instead of one OPF formulating their task as an optimization problem



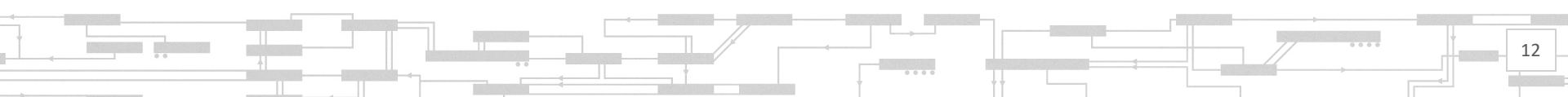
# Application of Power Flow

- Long-term and short-term planning studies of different scenarios
- Contingency analysis –  $n-1$  criterion
- Cascading analysis
- Real time monitoring of the system
- Economic Dispatch
- Stability analysis – numerical simulation of the transient process solving power flow at each step of the numerical integration
- Governor Power Flow – to analyze quasi steady state frequency response
- Continuation methods for Voltage Stability analysis
- Unbalanced 3-phase PF for distribution grids



# Computing Needs in Power Flow Analysis

- Challenges of the system model
  - Nonlinear, non-convex functions
  - Discrete and integer variables
  - Ill-behaved characteristics
  - Hundreds of Thousands of differential and algebraic equations
- Complexity of the power grid today and in the nearest future:
  - Distributed resources
  - Renewable resources
  - High volatility
  - Microgrids
  - Power electronics



# Future Directions

- Using High Performance Computing
- Phasor Measurement Units – linear solution
- Cloud computing
- Using Node/Breaker models without a need for topology processing
- Need for robust methods of solution – minimize convergence problems
- Ability to distinguish between numerical and physical instability of the solution. Holomorphic embedding.
- Transmission/Distribution co-simulation

