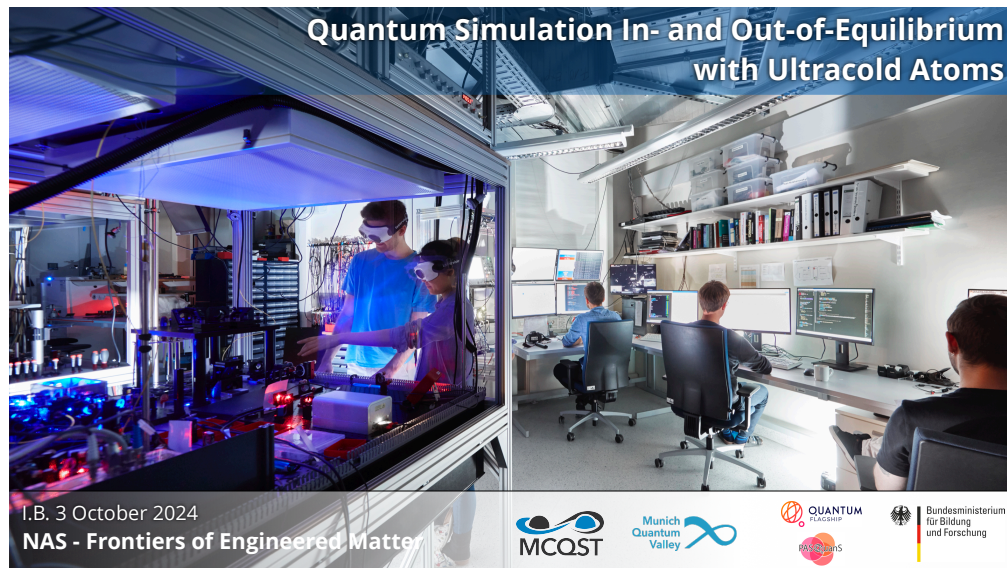
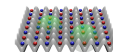


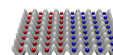
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State Preparation/Engineering and Detection
Manipulating the Orbital Bloch Sphere



1

Strongly Correlated Electron Physics
AFM, Polarons, Hole Pairing, Stripe Signatures,...

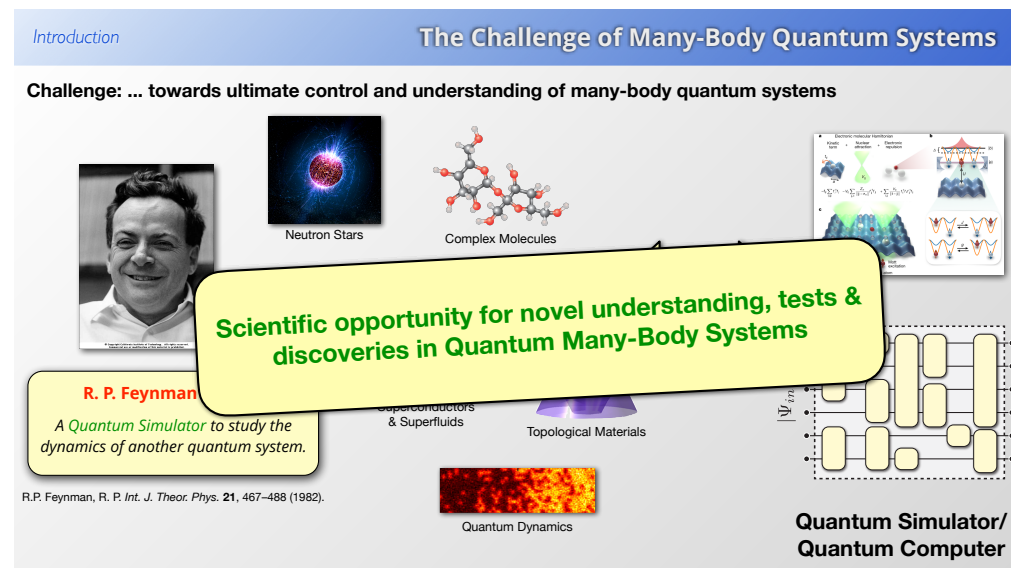
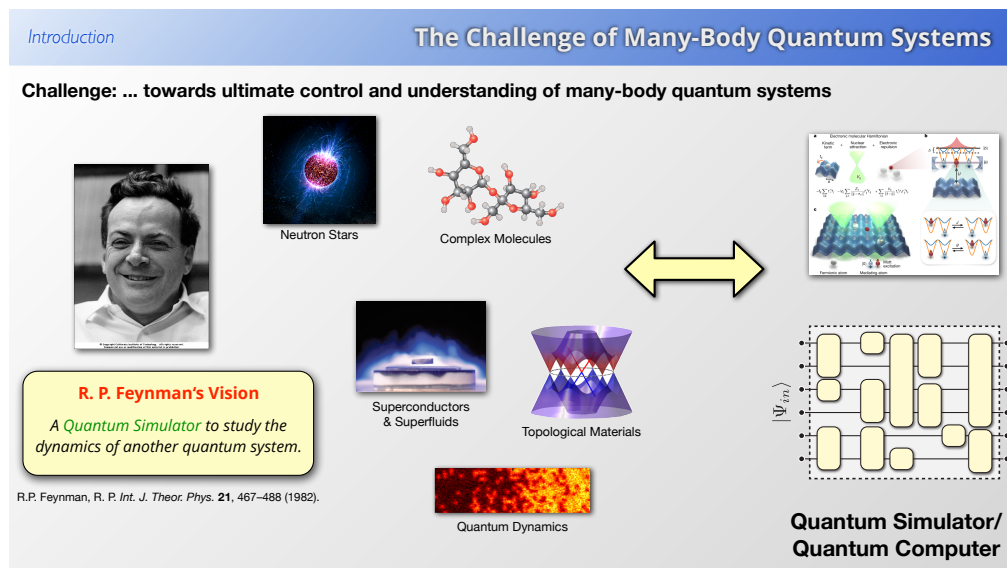


2

Non-Equilibrium Physics
Lieb-Robinson Bounds, Spin-Charge Fractionalization, Many-Body Localisation, Anomalous Spin Transport (KPZ)

3

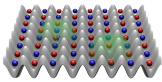
Outlook



Two approaches

Analog

Implement ruleset H_{model} directly



$$|\psi(t)\rangle = e^{-\frac{i}{\hbar} H_{\text{model}} t} |\psi(0)\rangle$$

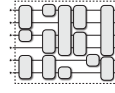
e.g. electrons, magnets,...

= **powerful!**
but **non-universal**

Digital

Approximate H_{model} ruleset digitally

$$H_{\text{model}} = \sum_{i=1}^l H_i$$



e.g. single / 2 qbit operation

$$e^{-iH_{\text{model}}t} \approx \left(e^{-iH_1t/n} e^{-iH_2t/n} \dots e^{-iH_l t/n} \right)^n$$

= **“universal” digital**
but **resource hungry**

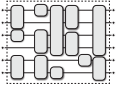


Two approaches

Digital

Approximate H_{model} ruleset digitally

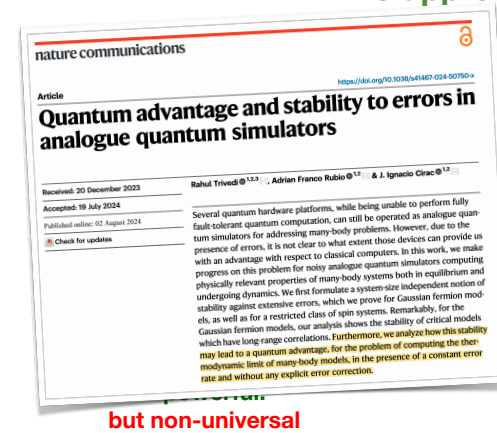
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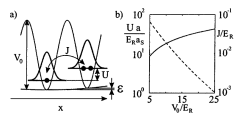
= **“universal” digital**
but **resource hungry**



but **non-universal**

20 Years of Quantum Simulation of Strongly Correlated States of Matter

VOLUME 81, NUMBER 15 PHYSICAL REVIEW LETTERS 12 OCTOBER 1998



Cold Bosonic Atoms in Optical Lattices

D. Jaksch,^{1,2} C. Bruder,^{1,3} J. I. Cirac,^{1,2} C. W. Gardiner,^{1,4} and P. Zoller^{1,2}
¹Institute for Theoretical Physics, University of Santa Barbara, Santa Barbara, California 93106-4030
²Institut für Theoretische Physik, Universität Innsbruck, A-6020 Innsbruck, Austria
³Institut für Theoretische Festkörperphysik, Universität Karlsruhe, D-76128 Karlsruhe, Germany
⁴School of Chemical and Physical Sciences, Victoria University, Wellington, New Zealand
 (Received 26 May 1998)

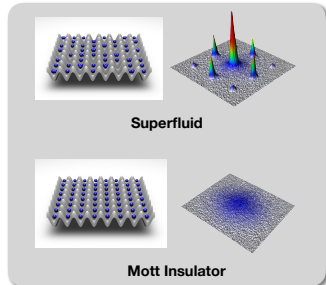
D. Jaksch et al. Phys. Rev. Lett. **81**, 3108 (1998)

Bose Hubbard Model: M. P. A. Fisher et al., Phys. Rev. B **40**, 546 (1989)



I. Cirac

P. Zoller



Superfluid

Mott Insulator

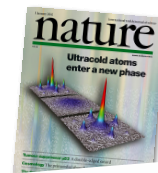
Quantum phase transition from a superfluid to a Mott insulator in a gas of ultracold atoms

Markus Greiner,¹ Olaf Mandel,² Thomas Esslinger,³ Theodor W. Hänsch,⁴ & Immanuel Bloch¹

M. Greiner, O. Mandel, T. Esslinger, T.W. Hänsch & I. Bloch
 Nature **415**, 39 (2002)

I. Bloch & M. Greiner Nat. Rev. Phys. (2022)

articles



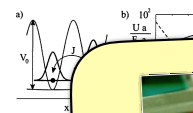
COMMENT

The superfluid-to-Mott insulator transition and the birth of experimental quantum simulation

Pre-quantum gases optical lattices: A. Hemmerich & T.W. Hänsch (LMU) / S.L. Rolston & W.D. Phillips (NIST)

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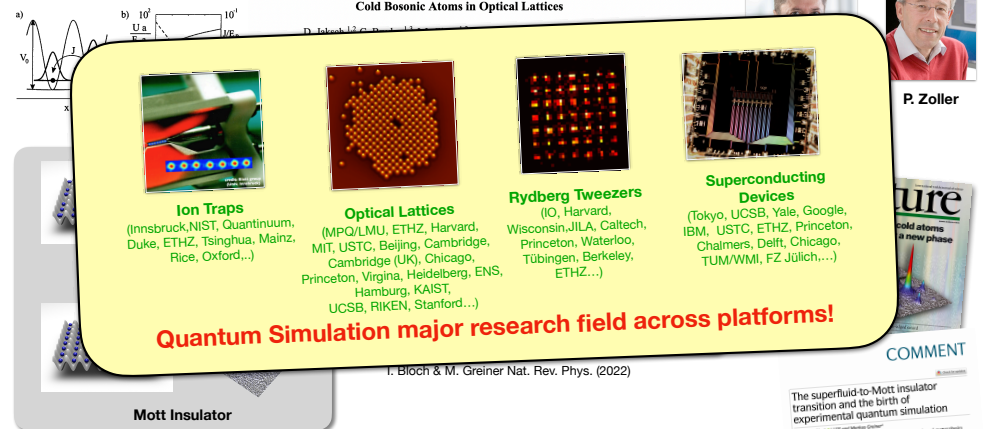
Cold Bosonic Atoms in Optical Lattices

D. Jaksch,^{1,2} C. Bruder,^{1,3} J. I. Cirac,^{1,2} C. W. Gardiner,^{1,4} and P. Zoller^{1,2}
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⁴School of Chemical and Physical Sciences, Victoria University, Wellington, New Zealand
 (Received 26 May 1998)



I. Cirac

P. Zoller



Ion Traps
 (Innsbruck, NIST, Quantumum, Duke, ETHZ, Tsinghua, Mainz, Rice, Oxford,...)

Optical Lattices
 (MPO/LMU, ETHZ, Harvard, MIT, USC, Beijing, Cambridge, Cambridge (UK), Chicago, Princeton, Virginia, Heidelberg, ENS, Hamburg, KAIST, UCSB, RIKEN, Stanford,...)

Rydberg Tweezers
 (IO, Harvard, Wisconsin, JILA, Caltech, Princeton, Waterloo, Tübingen, Berkeley, ETHZ,...)

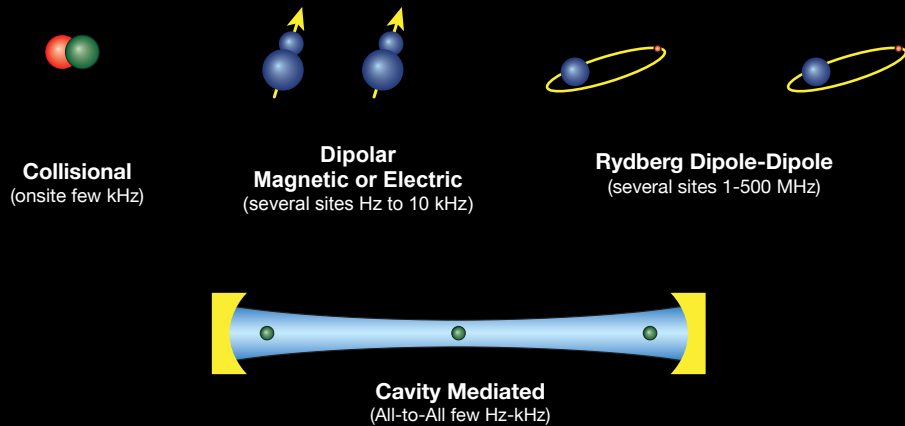
Superconducting Devices
 (Tokyo, UCSB, Yale, Google, IBM, USC, ETHZ, Princeton, Chalmers, Delft, Chicago, TUM/WMI, FZ Jülich,...)

Quantum Simulation major research field across platforms!

I. Bloch & M. Greiner Nat. Rev. Phys. (2022)

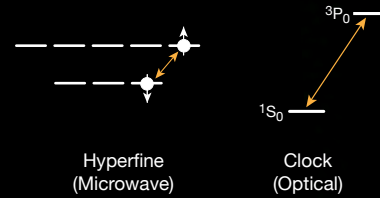
Pre-quantum gases optical lattices: A. Hemmerich & T.W. Hänsch (LMU) / S.L. Rolston & W.D. Phillips (NIST)

Interaction Control



Particles: Fermions, Bosons, Mixtures

Spin degree of freedom:



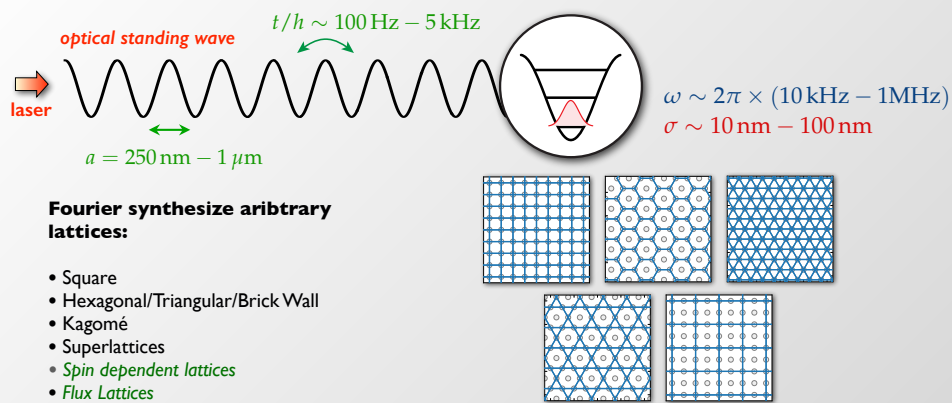
System size: up to few thousands of particles

Mobility: itinerant or static

courtesy: T. W. Hänsch

Introduction

Primer on Optical Lattices



Fourier synthesize arbitrary lattices:

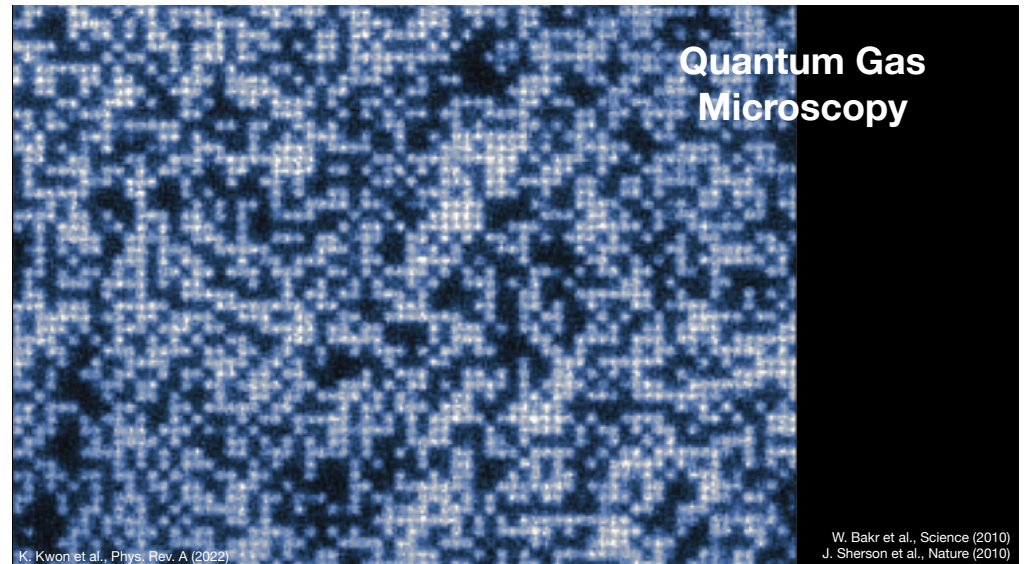
- Square
- Hexagonal/Triangular/Brick Wall
- Kagomé
- Superlattices
- Spin dependent lattices
- Flux Lattices

Full **dynamical** control over **lattice depth, geometry, dimensionality!**

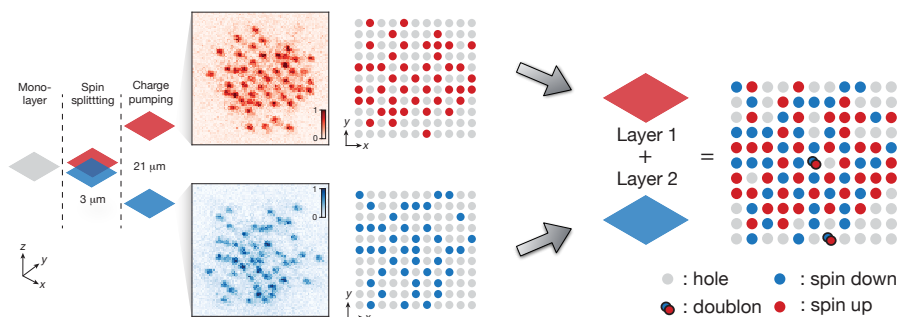
D. Wei et al. Phys. Rev. X **13**, 021042 (2023), recently used: W. Bakr group Nature **629**, 323 (2024) (Princeton)
related: D. Greif et al. Nature **535** 217 (2014), M. Xu et al. Nature **620**, 971-976 (2023)



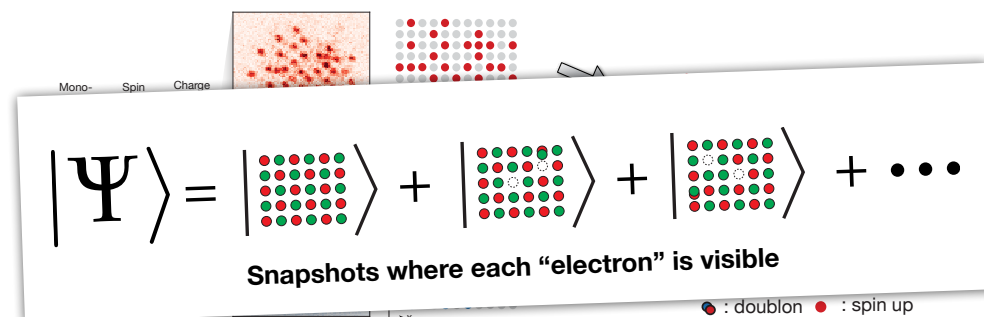
Quantum Gas Microscopy



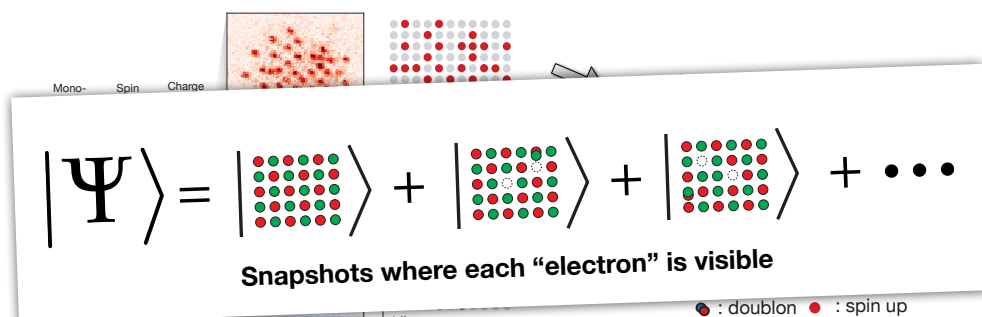
W. Bakr et al., Science (2010)
J. Sherson et al., Nature (2010)



Density and spin readout: M. Boll et al. Science **353**, 1257 (2016), J. Koepsell et al. Phys. Rev. Lett. **125**, 010403 (2020),
see also: Harvard (Greiner), Princeton (Bakr) Phys. Rev. Lett. **129**, 123201 (2022), MIT (Zwierlein) Science **381**, 82 (2023)

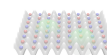


Density and spin readout: M. Boll et al. Science **353**, 1257 (2016), J. Koepsell et al. Phys. Rev. Lett. **125**, 010403 (2020),
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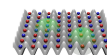


.... and also current snapshots! A. Impertro et al. Phys. Rev. Lett. (2024)
 B. Du, et al. Phys. Rev. Lett. (2024).

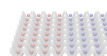
Density and spin readout: M. Boll et al. Science **353**, 1257 (2016), J. Koepsell et al. Phys. Rev. Lett. **125**, 010403 (2020),
see also: Harvard (Greiner), Princeton (Bakr) Phys. Rev. Lett. **129**, 123201 (2022), MIT (Zwierlein) Science **381**, 82 (2023)



0 State Preparation/Engineering and Detection
 Manipulating the Orbital Bloch Sphere



1 Strongly Correlated Electron Physics
 AFM, Polarons, Hole Pairing, Stripe Signatures,...



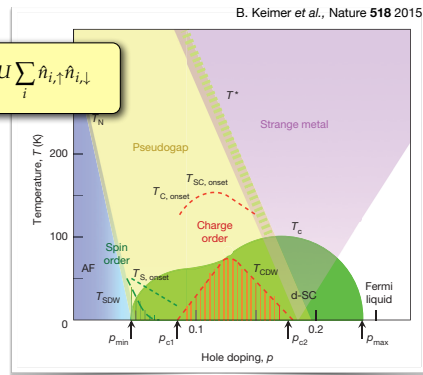
2 Non-Equilibrium Physics
 Lieb-Robinson Bounds, Spin-Charge Fractionalization,
 Many-Body Localisation, Anomalous Spin Transport (KPZ)

3 Outlook

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$

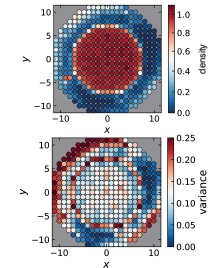
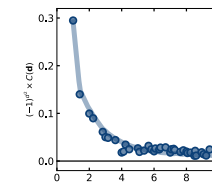
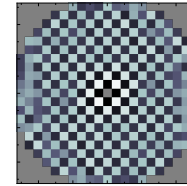
$$H = J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j \quad J = \frac{4t^2}{U}$$

magnetic order



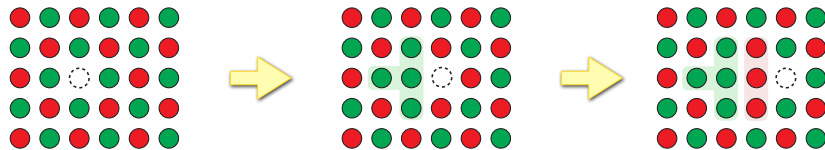
T. Esslinger, Fermi-Hubbard Physics with Atoms in an Optical Lattice.
Annu. Rev. Cond. Mat. Phys. **1**, 129–152 (2010).

$$\frac{\langle \hat{S}_i^z \hat{S}_j^z \rangle - \langle \hat{S}_i^z \rangle \langle \hat{S}_j^z \rangle}{\sigma(\hat{S}_j^z) \sigma(\hat{S}_i^z)}$$



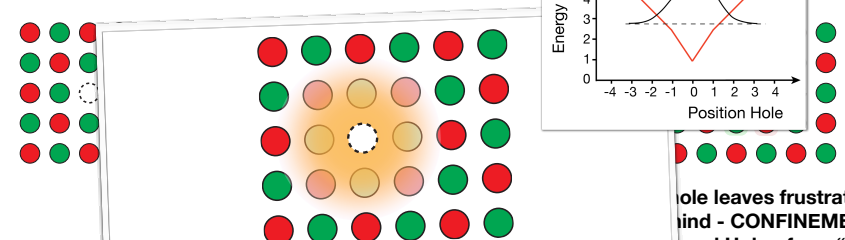
$$\begin{array}{ll} T/t \sim 0.25 & T/J \sim 0.4 \\ U/t = 6.5 & t/J \simeq 1.6 \end{array}$$

nature
A MAGNETIC MOMENT



J.M.F. Gunn & B.D. Simons Phys. Rev. B **42**, 4370 (1990)
F. Grusdt *et al.*, PRX **8**, 011046 (2018)

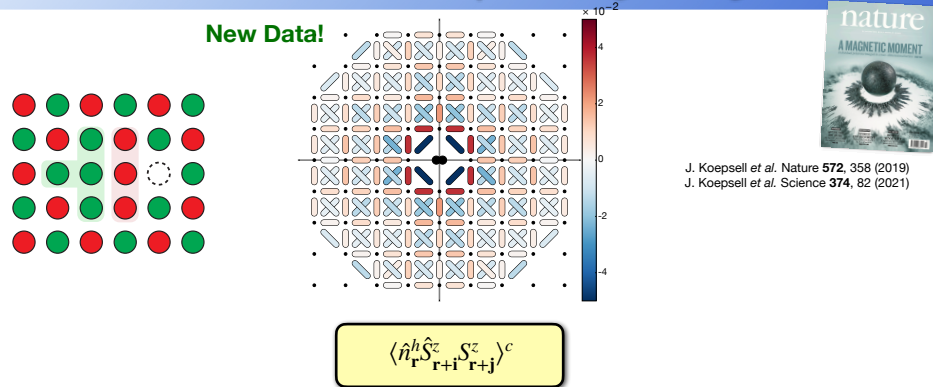
J. Koepsell *et al.* Nature **572**, 358 (2019) & J. Koepsell *et al.* Science **374**, 82 (2021)
See also recent results on frustrated systems: Princeton & Harvard
related: imprints of string patterns Ch. Chiu *et al.* Nature (2019)
attractive U: T. Hartke *et al.* Science **381**, 82 (2023)



D. Simons Phys. Rev. B **42**, 4370 (1990)
dt et al., PRX **8**, 011046 (2018)

J. Koepsell *et al.* *Nature* **572**, 358 (2019) & J. Koepsell *et al.* *Science* **374**, 82 (2021)
See also recent results on frustrated systems: Princeton & Harvard
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New Data!

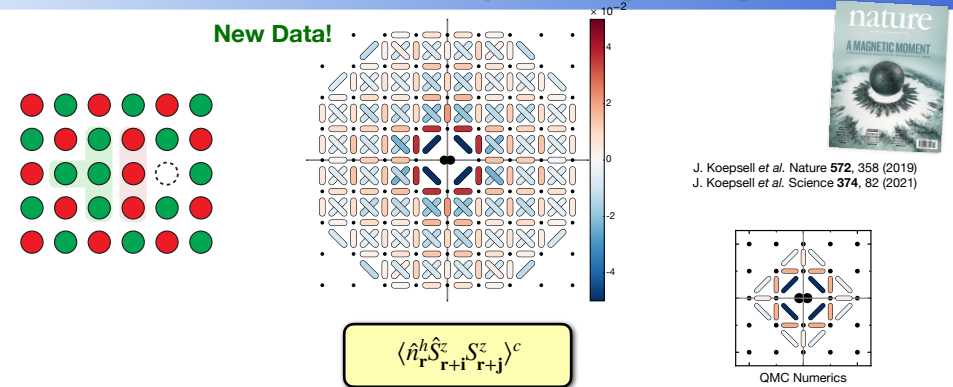


Three point hole-spin-spin correlator
(connected & symmetrized)

Kinetic Induced Polarons on Triangular Lattice:
M. Greiner arXiv:2308.12269 (Harvard)
W. Bakr arXiv:2308.12951 (Princeton)

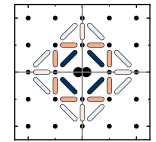


New Data!

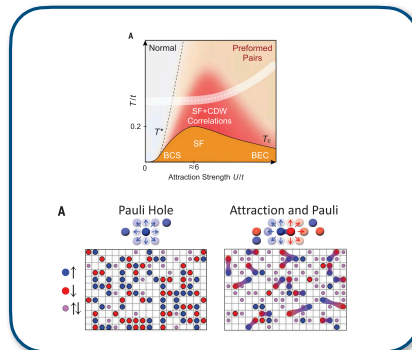


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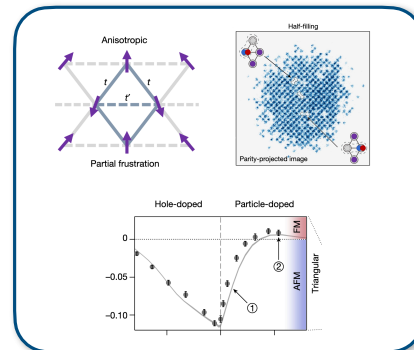


QMC Numerics
Z. Wang & Lode Pollet
Quantitative Match!



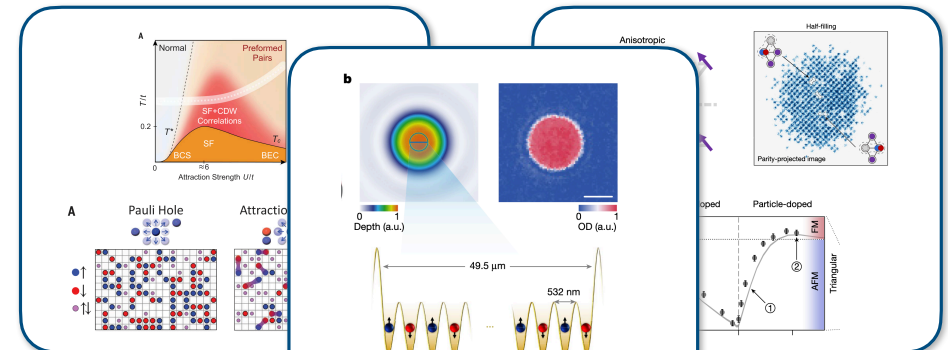
Attractive Interactions

Hartke *et al. Science* **381**, 82–86 (2023)
M. Zwierlein group (MIT)



Tunable Frustration

Xu, M. *et al. Nature* 1–6 (2023)
doi:[10.1038/s41586-023-06280-5](https://doi.org/10.1038/s41586-023-06280-5)
Greiner group (Harvard)
see also W. Bakr (Princeton)



Attractive Interactions

Hartke *et al. Science* **381**, 82–
M. Zwierlein group (MIT)

Large Scale 3D Systems

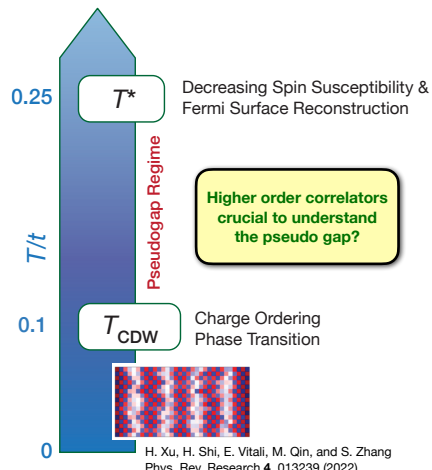
H.-J. Shao, Y.-A. Chen & J.-W. Pan,
Nature **632**, 267 (2024)

Tunable Frustration

Xu, M. *et al. Nature* 1–6 (2023)
doi:[10.1038/s41586-023-06280-5](https://doi.org/10.1038/s41586-023-06280-5)
Greiner group (Harvard)
see also W. Bakr (Princeton)



Square Lattice Hubbard Model - Phases (Low Doping)



H.J. Schulz Phys. Rev. Lett. 64, 1445 (1990)

What is the physical mechanism for the Pseudogap?

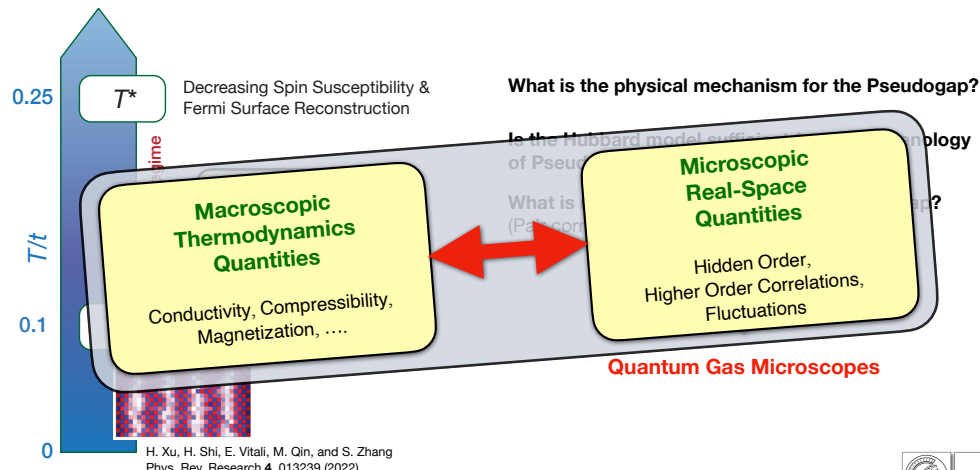
Is the Hubbard model sufficient for Phenomenology of Pseudogap?

What is real space manifestation of Pseudogap?
(Pair correlations, spin background,...)

Quantum Gas Microscopes



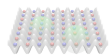
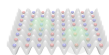
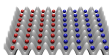
Square Lattice Hubbard Model - Phases (Low Doping)



H.J. Schulz Phys. Rev. Lett. 64, 1445 (1990)



Applications in Many-Body Physics

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Manipulating the Orbital Bloch Sphere1 Strongly Correlated Electron Physics
AFM, Polarons, Hole Pairing, Stripe Signatures,...2 Non-Equilibrium Physics
Lieb-Robinson Bounds, Spin-Charge Fractionalization,
Many-Body Localisation, Anomalous Spin Transport (KPZ)

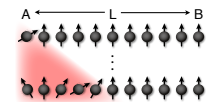
3 Outlook

Optical Lattices

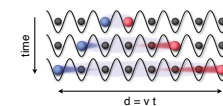
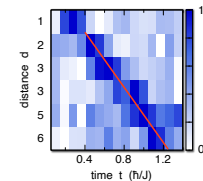
Non-Equilibrium Dynamics

1 Information Spreading in Many-Body Systems
Lieb-Robinson Bounds

E.H. Lieb & D.W. Robinson Comm. Math. Phys. (1972)

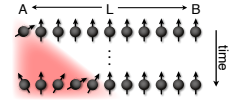


$$|(A(t)B(t)) - (A(t))(B(t))| \leq \lambda' \exp\left(\frac{vt - L/2}{\xi}\right)$$

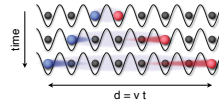
M. Cheneau et al., Nature (2012)
Ion traps: P. Jurcevic et al. Nature (2014),
Ph. Richerme et al. Science (2014)

1 Information Spreading in Many-Body Systems Lieb-Robinson Bounds

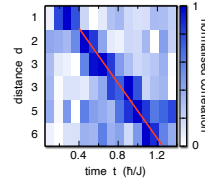
E.H. Lieb & D.W. Robinson Comm. Math. Phys. (1972)



$$|(A(t)B(t)) - (A(t))(B(t))| \leq \lambda' \exp\left(\frac{vt - L/2}{\xi'}\right)$$

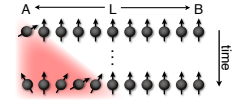


M. Cheneau et al., Nature (2012)

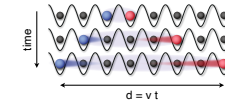
Ion traps: P. Jurcevic et al. Nature (2014),
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1 Information Spreading in Many-Body Systems Lieb-Robinson Bounds

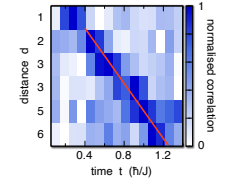
E.H. Lieb & D.W. Robinson Comm. Math. Phys. (1972)



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M. Cheneau et al., Nature (2012)

Ion traps: P. Jurcevic et al. Nature (2014),
Ph. Richerme et al. Science (2014)

2 Spin-Charge Fractionalization Real space, time-resolved observation

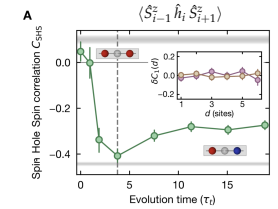
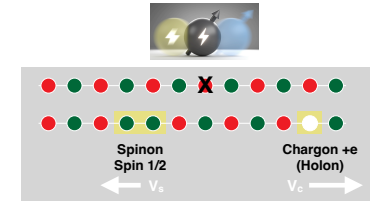
Experiment:

J. Vijayan et al. Science 367, 186 (2020)

Spectroscopic determination:

C. Kim, et al. Phys. Rev. Lett. 77, 4054 (1996)

O.M. Auslaender et al. Science 308, 88 (2005)



3 Thermalisation in Quantum Many-Body Systems

How do isolated Quantum Many-Body systems thermalise?

Measure entanglement entropy via
Many-Body Hong-Ou-Mandel:

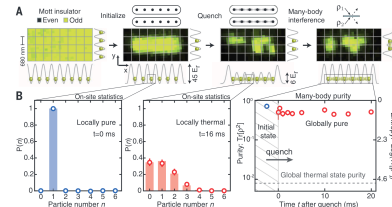
R. Islam et al. Nature 528, 77–83 (2015).

Theory:

C.M. Alves & D. Jaksch Phys. Rev. Lett. 2004

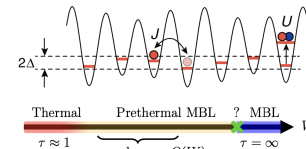
A. Daley et al. Phys. Rev. Lett. 2012

$$S_{VN} = -tr(\rho_A \log \rho_A) = S_{th}$$



A. Kaufmann et al. Science 2016

4 Non-Thermalizing Behaviour



D.M. Long et al. Phys. Rev. Lett. 131, 106301 (2023)

Many-Body Localization

review:

R. Nandkishore & D. A. Huse

Annu. Rev. Condens. Matter Phys. 6, 15 (2015)

D.A. Abanin, E. Altman, I. Bloch & M. Serbyn

Rev. Mod. Phys. 91, 021001 (2019)

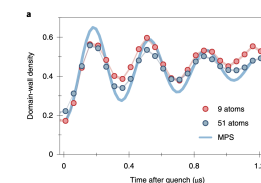
exp: M. Schreiber et al. Science (2015)

J.Y. Choi et al. Science (2016)

M. Rispoli, et al. Nature (2019)

A. Lukin et al. Science (2019)

GS: Kondov et al. Phys. Rev. Lett. (2015)



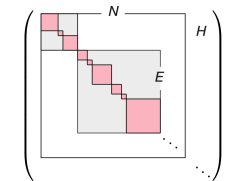
Many-Body Quantum Scars

review:

M. Serbyn, D.A. Abanin & Z. Papić

Nature Phys. 17, 675 (2021)

exp: H. Bernien et al. Nature 551, 579 (2017)



Hilbert Space Fragmentation

V. Khemani, M. Hermele, and R. Nandkishore

Phys. Rev. B 101, 174204 (2020)

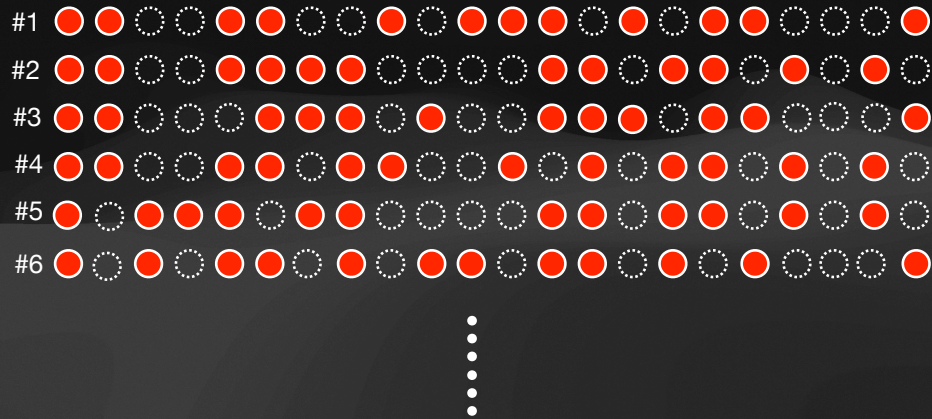
P. Sala, ... & F. Pollmann

Phys. Rev. X 10, 011047 (2020)

exp: 1D S. Scherg et al. Nat. Commun. 12, 4490 (2021)

2D D. Adler et al., arXiv:2404.14896

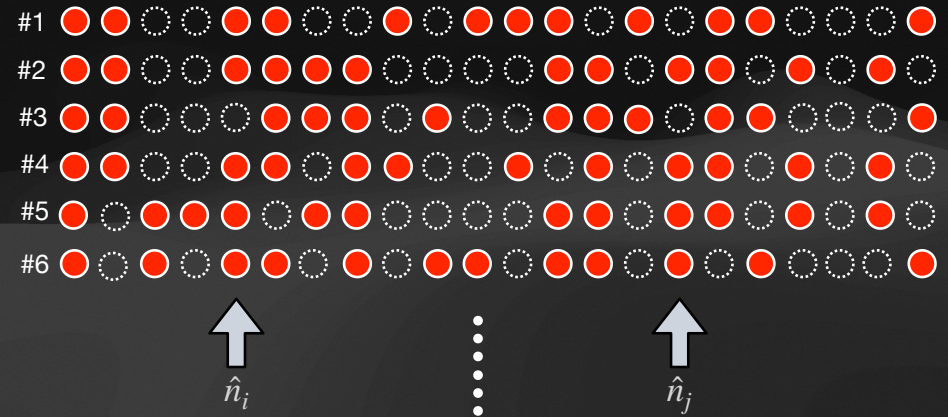
Quantum Transport - Atom-by-Atom



J.F. Wienand *et al.*, Nature Physics (2024)

See also: (Endres group) J. Choi *et al.*, Nature **613**, 468 (2023)

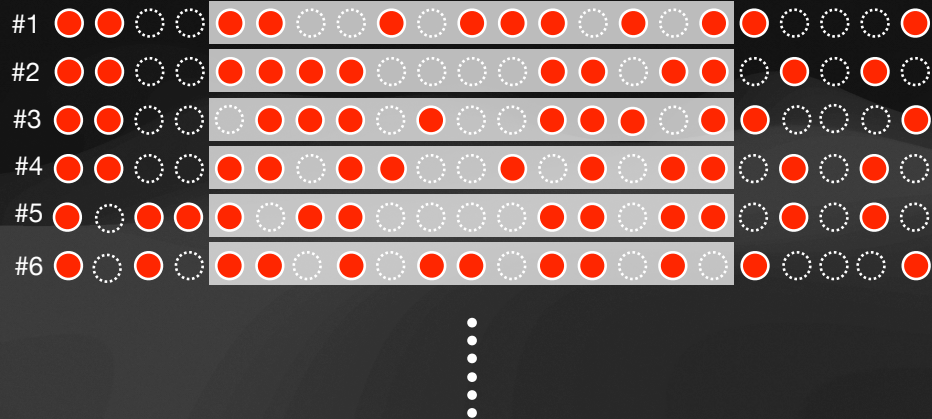
Quantum Transport - Atom-by-Atom



J.F. Wienand *et al.*, Nature Physics (2024)

See also: (Endres group) J. Choi *et al.*, Nature **613**, 468 (2023)

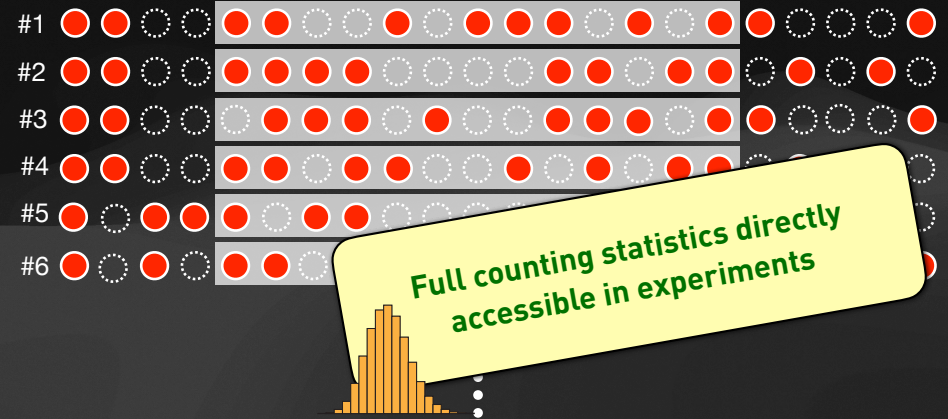
Quantum Transport - Atom-by-Atom



J.F. Wienand *et al.*, Nature Physics (2024)

See also: (Endres group) J. Choi *et al.*, Nature **613**, 468 (2023)

Quantum Transport - Atom-by-Atom

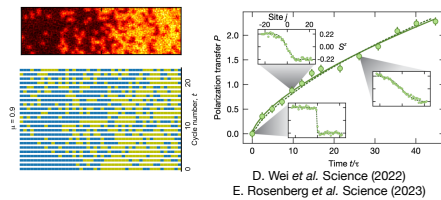
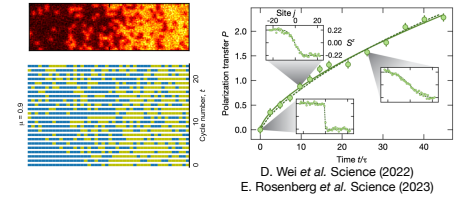
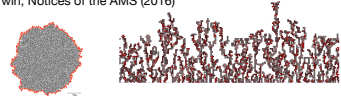
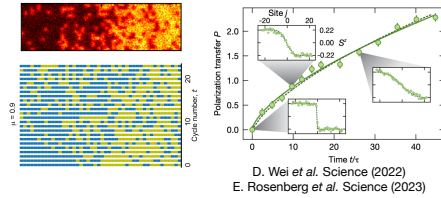


J.F. Wienand *et al.*, Nature Physics (2024)

See also: (Endres group) J. Choi *et al.*, Nature **613**, 468 (2023)

5 Anomalous Spin Transport - Kardar-Parisi-Zhang Universality

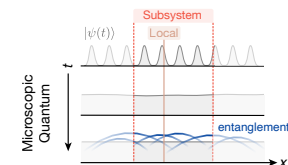
M. Kardar, G. Parisi & Y.-C. Zhang Phys. Rev. Lett. (1986)
M. Ljubotina *et al.*, Phys. Rev. Lett. (2019)
Review: V. Bulchandini, S. Gopalakrishnan, E. Ilievski
J. Stat. Mech. 084001 (2021)
I. Corwin, Notices of the AMS (2016)



6 (Hydro) Dynamics of Fluctuations (?) in diffusive systems

Dynamics of Subsystem Fluctuations

J.F. Wienand *et al.* Nature Physics (2024)
MFT: Bertini, L., De Sole, A., Gabrielli, D., Jona-Lasinio, G. & Landim, C.
Rev. Mod. Phys. 87, 593–636 (2015).



$$\partial_t n + \partial_x j = 0, \quad j = -D(n) \partial_x n + \sqrt{2D(n)} \chi(n) \xi$$

Where Next?

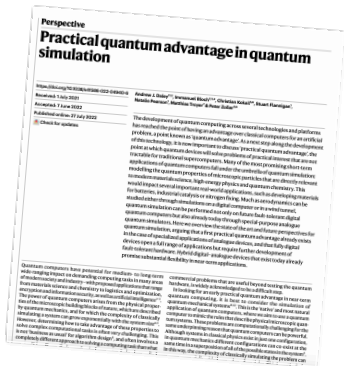
A Joint Look Ahead...

Quantum Simulation & Computation Platforms
(Atoms, Ions, SC Qubits, Photons, NV Centers...)

(Digital)
Circuit Model

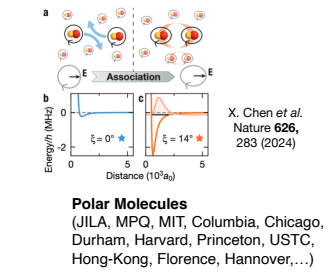
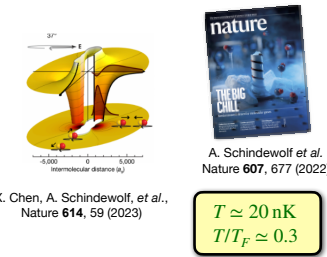
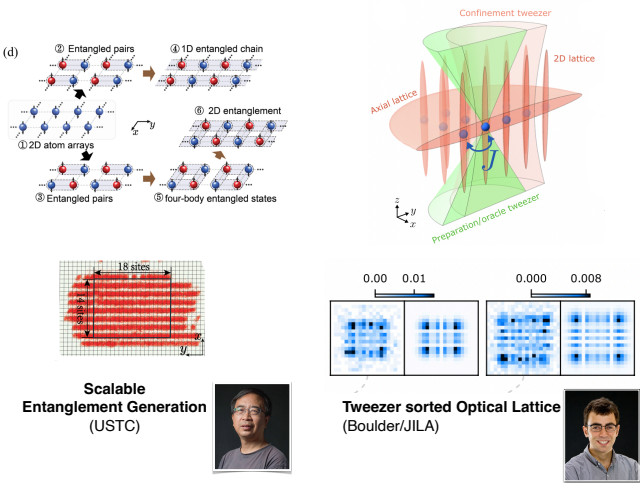
Analog-Digital
Hybrid Operation

(Analog)
Direct Modeling

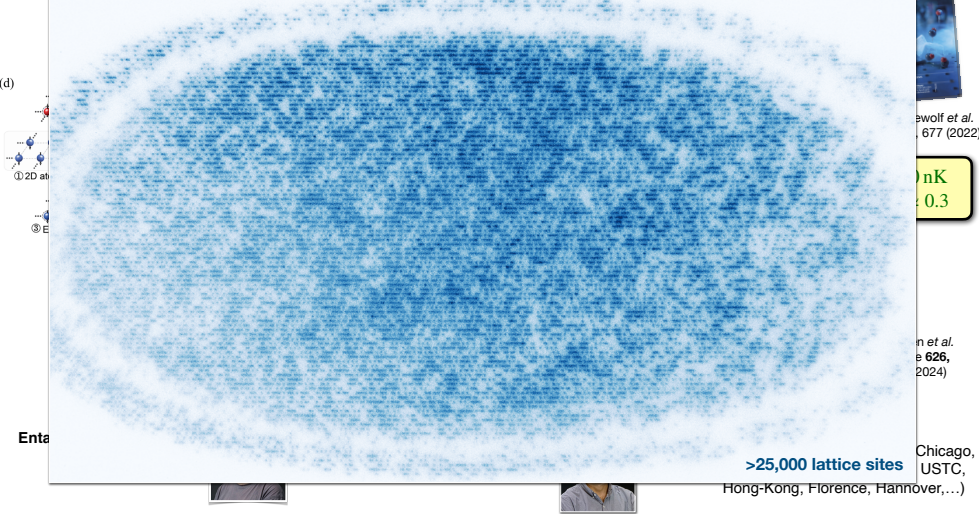


A.J. Daley, I. Bloch, C. Kokail, S. Flannigan, N. Pearson, M. Troyer, P. Zoller
Nature **607**, 667–676 (2022)

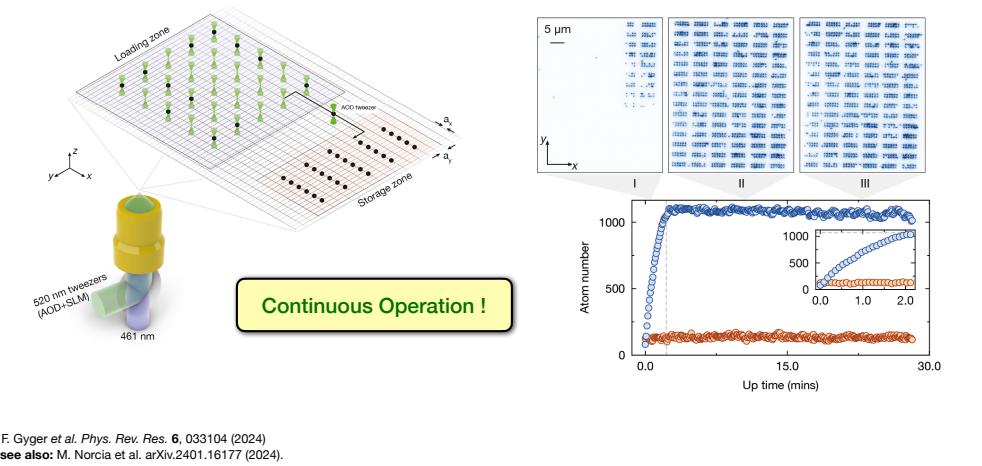
Enhanced Programmability



Enhanced Programmability



Continuously Loaded & Sorted Optical Lattice



Continuous Loading in Action

Continuously operated array for up to 1.5h with > 1200 atoms

Readily scalable to >10,000 atoms

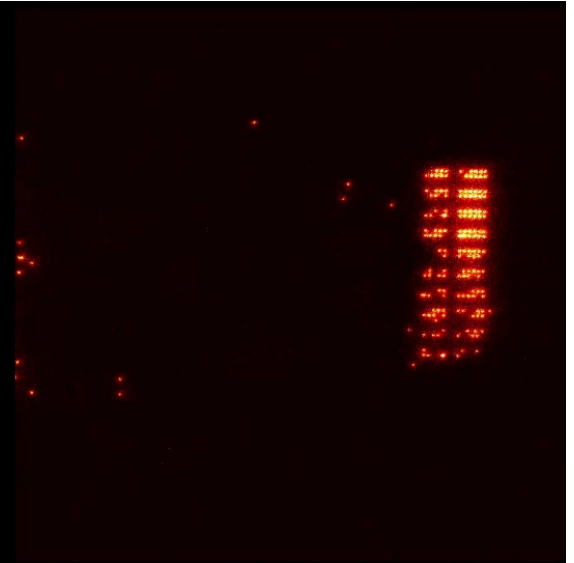


F. Gyger et al. PRR 6, 033104 (2024)
see also: M. Norcia et al. arXiv.2401.16177 (2024).

Continuous Loading in Action

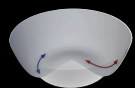
Continuously operated array for up to 1.5h with > 1200 atoms

Readily scalable to >10,000 atoms

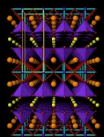


F. Gyger et al. PRR 6, 033104 (2024)
see also: M. Norcia et al. arXiv.2401.16177 (2024).

Quantum Universe in the Lab



Particle Physics



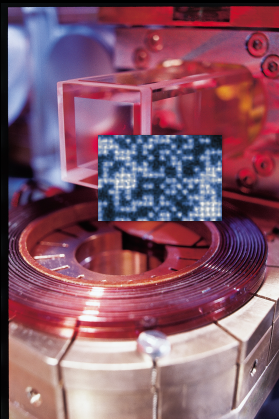
Quantum Materials



Neutron Stars



Our Universe



www.quantum-munich.de



