

Quantum Networks: A Frontier for Condensed Matter Physics

Vedika Khemani
Stanford University

National Academy CMMRC Meeting

NETWORK: A system of *interconnected elements* representing the *organization* and/or *flow* of information, resources or other entities



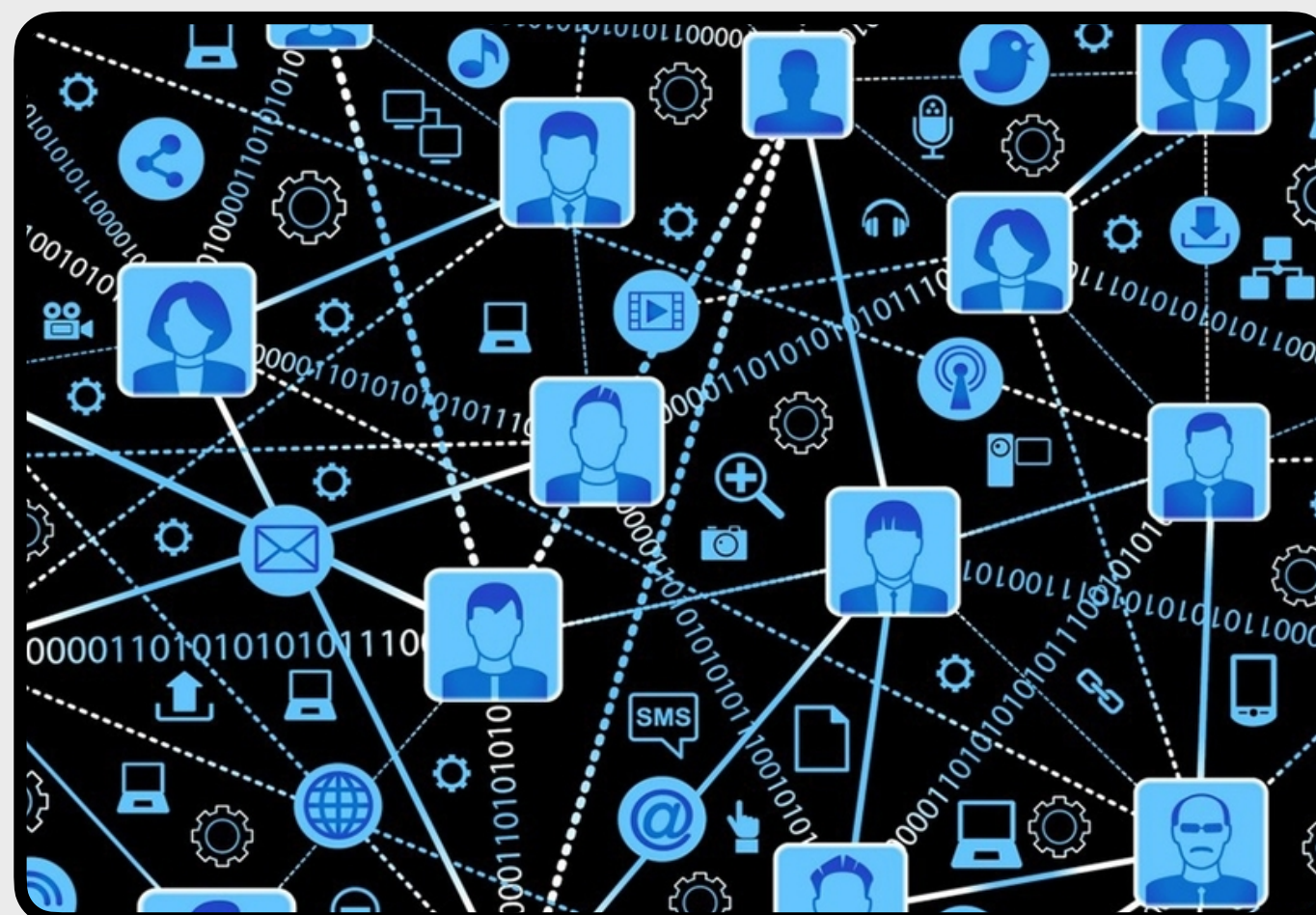
Transportation Network

Greenwich Village Society for Historic Preservation



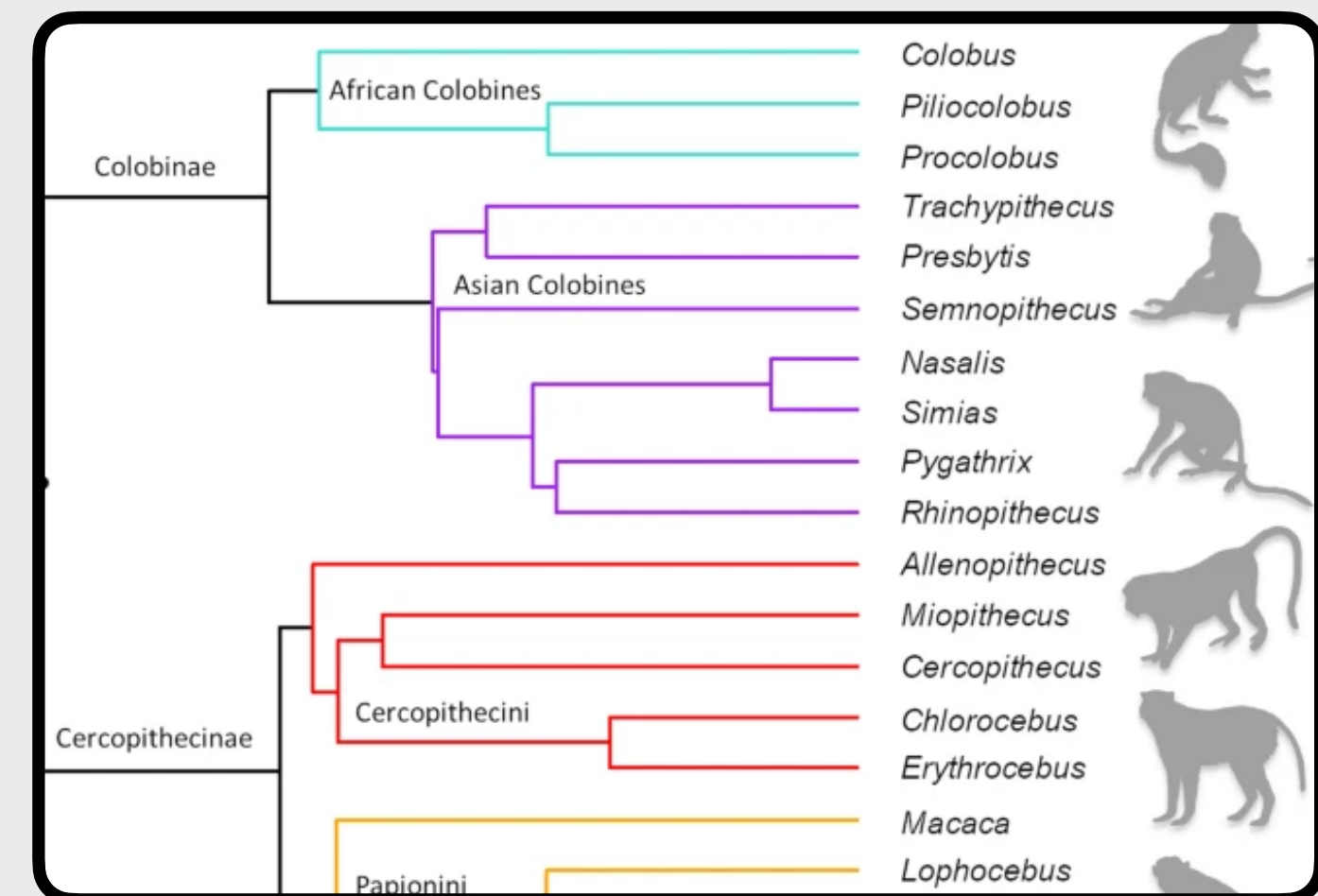
Satellite Network

Anterovium- Alamy Stock Photo



Social Network

Stefanie Koperniak, MIT News 2016



Phylogenetic Network

Sci Rep 12 (2022)

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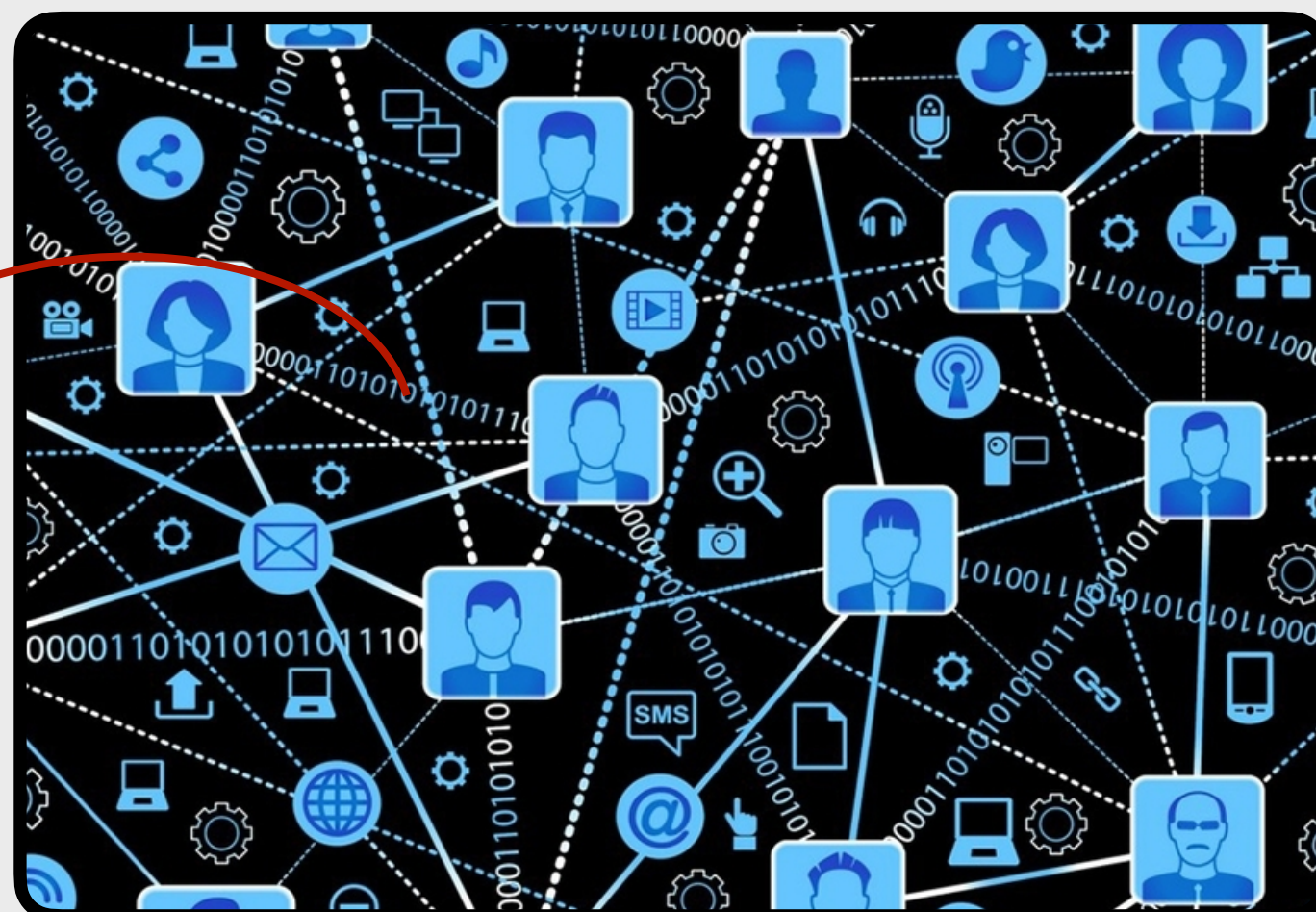
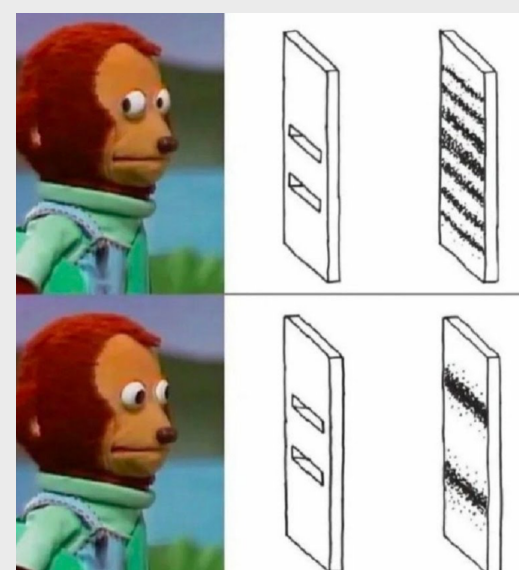
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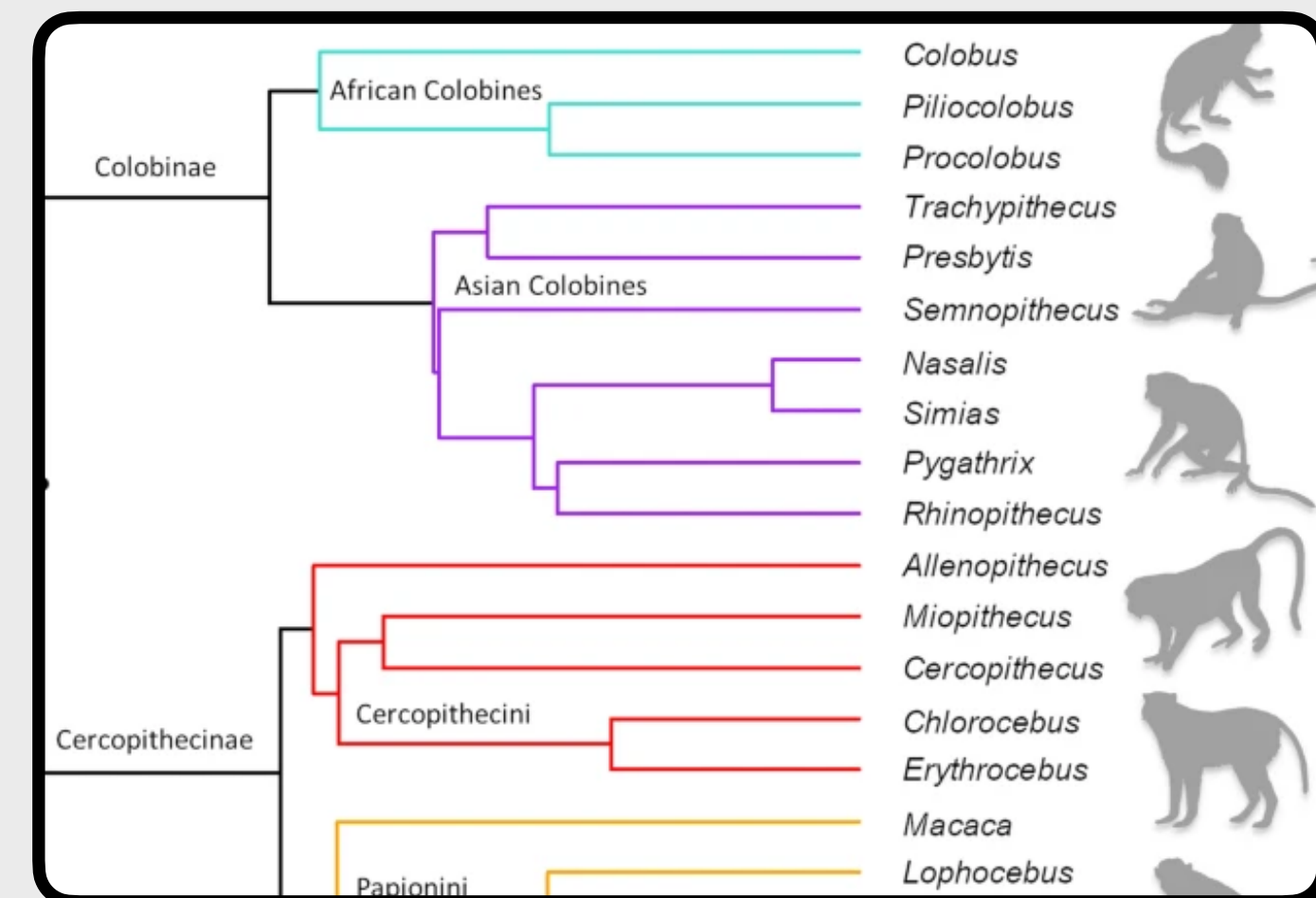
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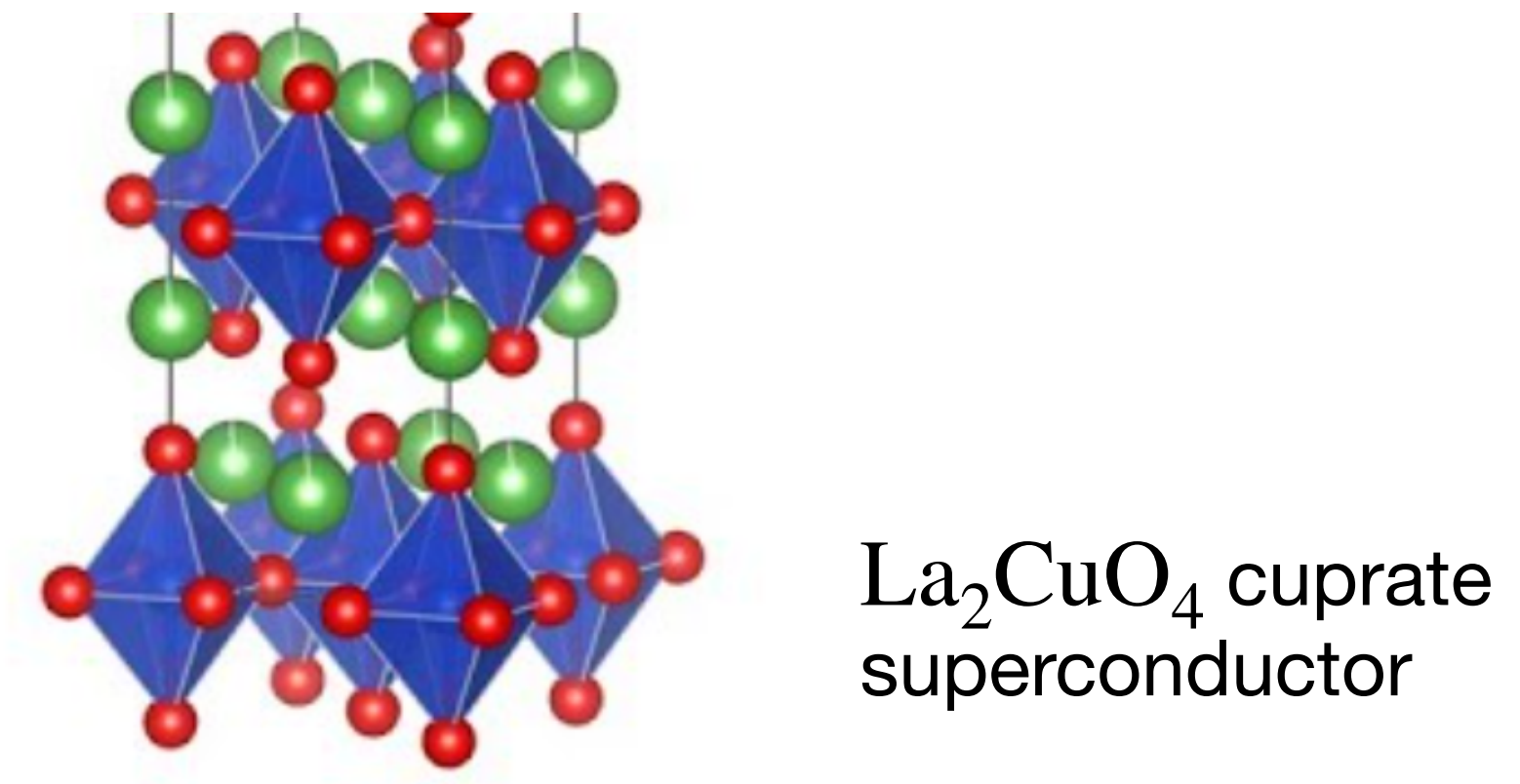
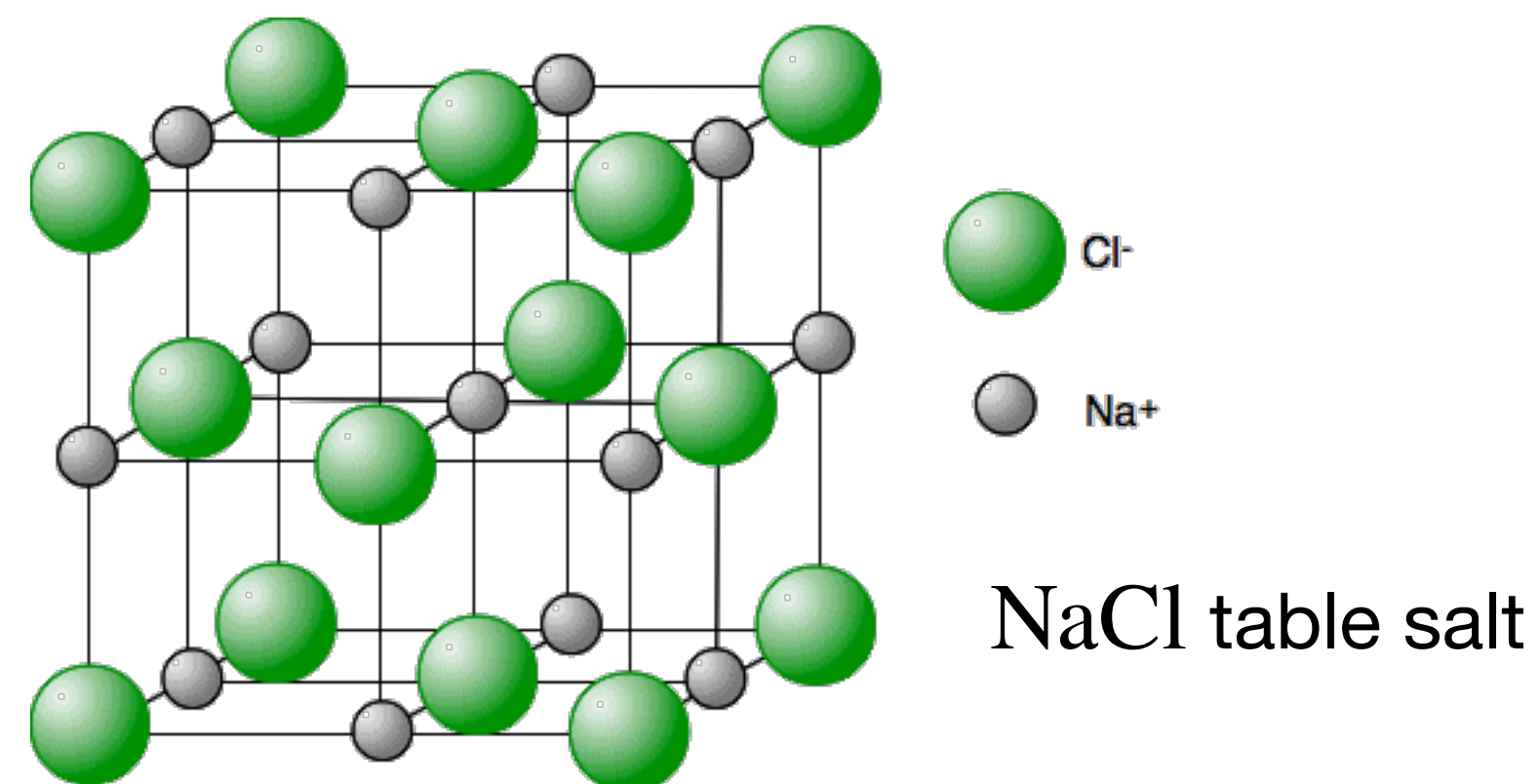
Phylogenetic Network

Sci Rep 12 (2022)

QUANTUM NETWORK

*A system of many strongly-interacting quantum elements
organized into different structures*

All matter arises from interacting electrons self-assembling into some structure: atoms, molecules, crystals, glasses, topological insulators, superconductors...



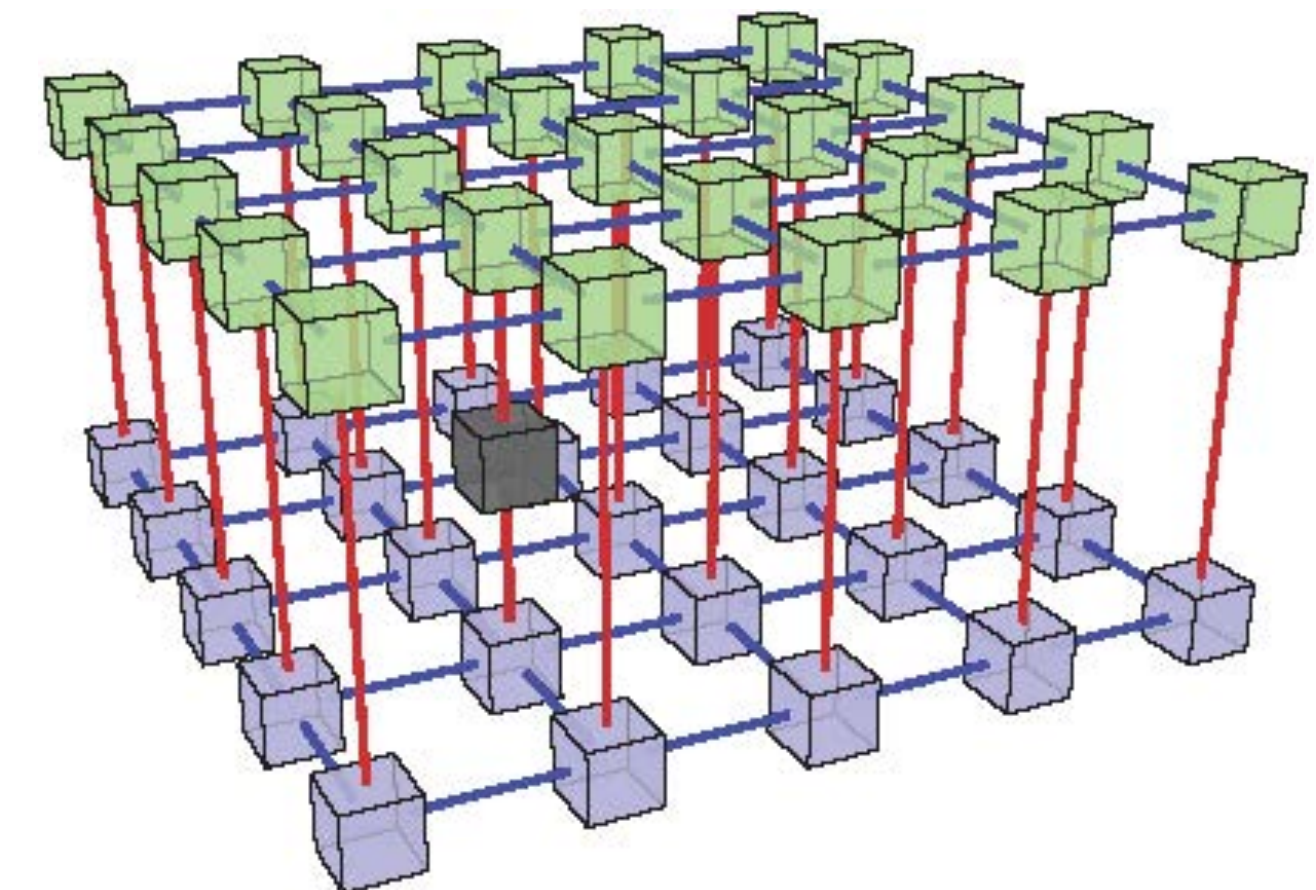
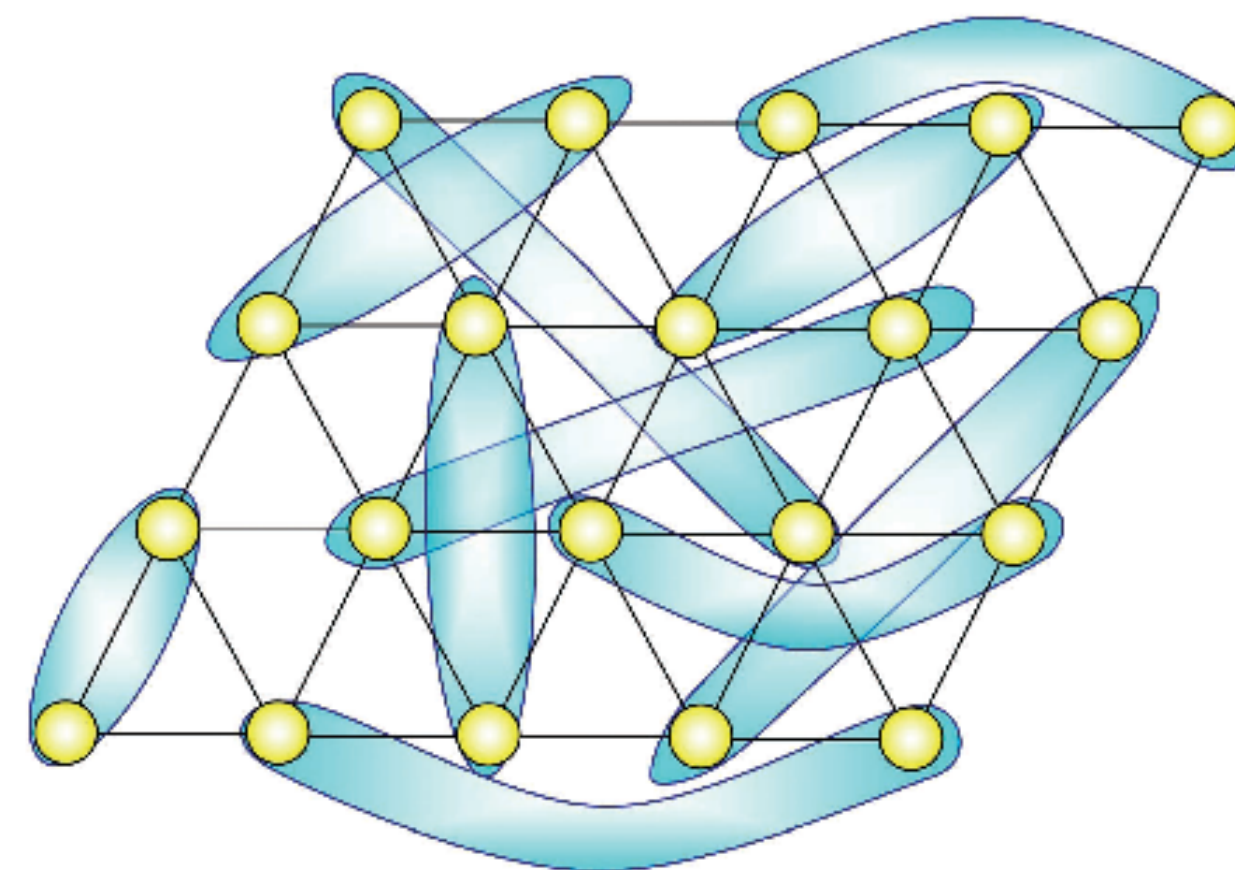
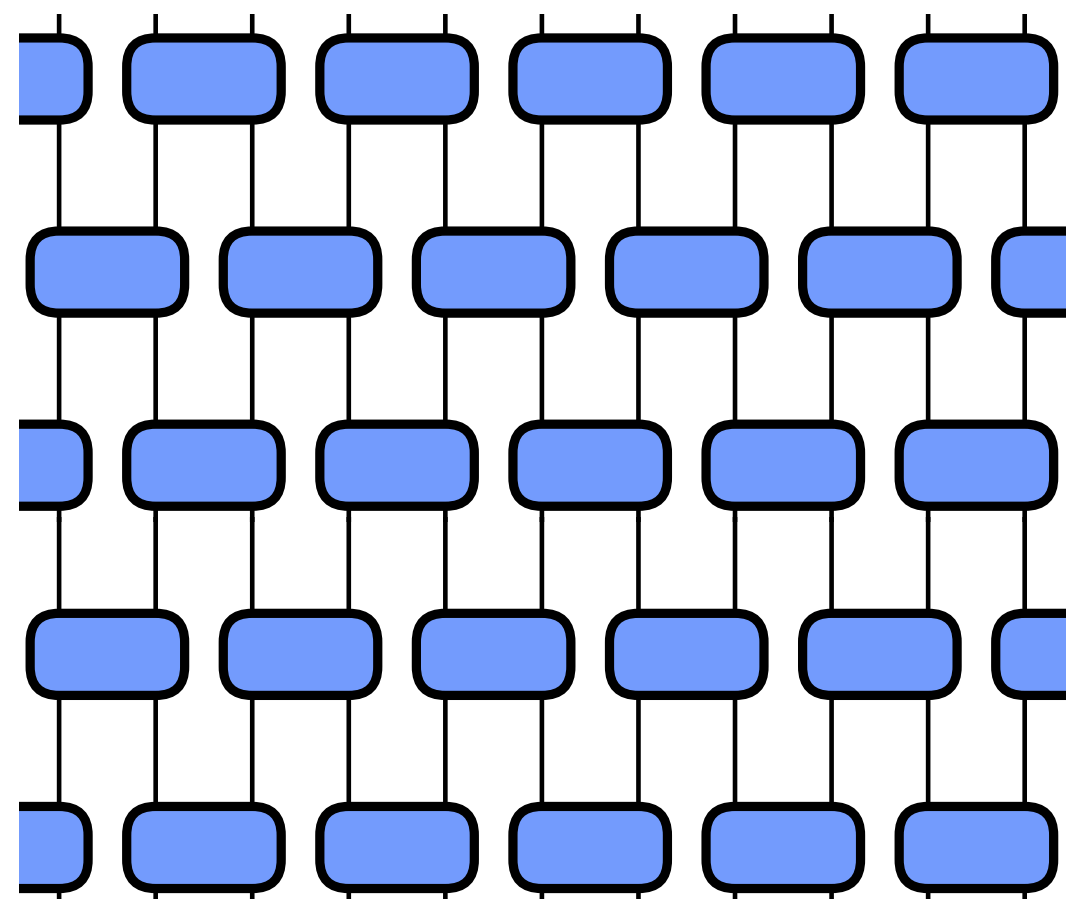
QUANTUM NETWORK

*A system of many strongly-interacting quantum elements organized by the **structure of quantum information***

c2000s — characterize ground state phases by structure of long-range entanglement.

Unitary circuits and tensor networks are powerful for encapsulating this entanglement structure

Xiao-Gang Wen, Ignacio Cirac, Frank Verstraete...

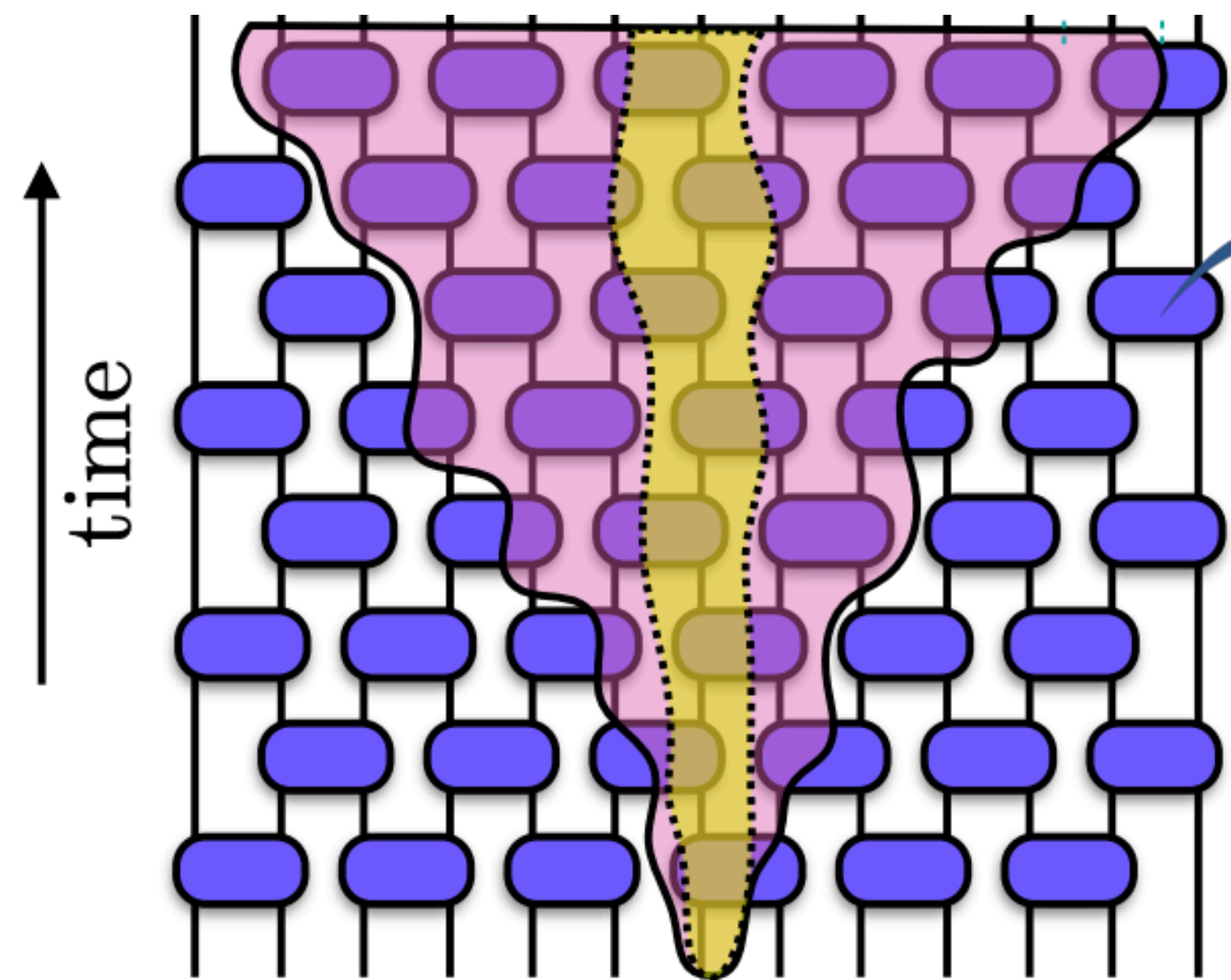


QUANTUM NETWORK

*A system of many strongly and controllably interacting quantum elements organized by the **structure and flow of quantum information***

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Fisher, Khemani, Nahum, Vijay ARCMP 2023

Dynamics: flow of quantum information through spacetime

How does an isolated quantum system reach thermal equilibrium under its own dynamics?

Can a system evade thermal equilibrium?

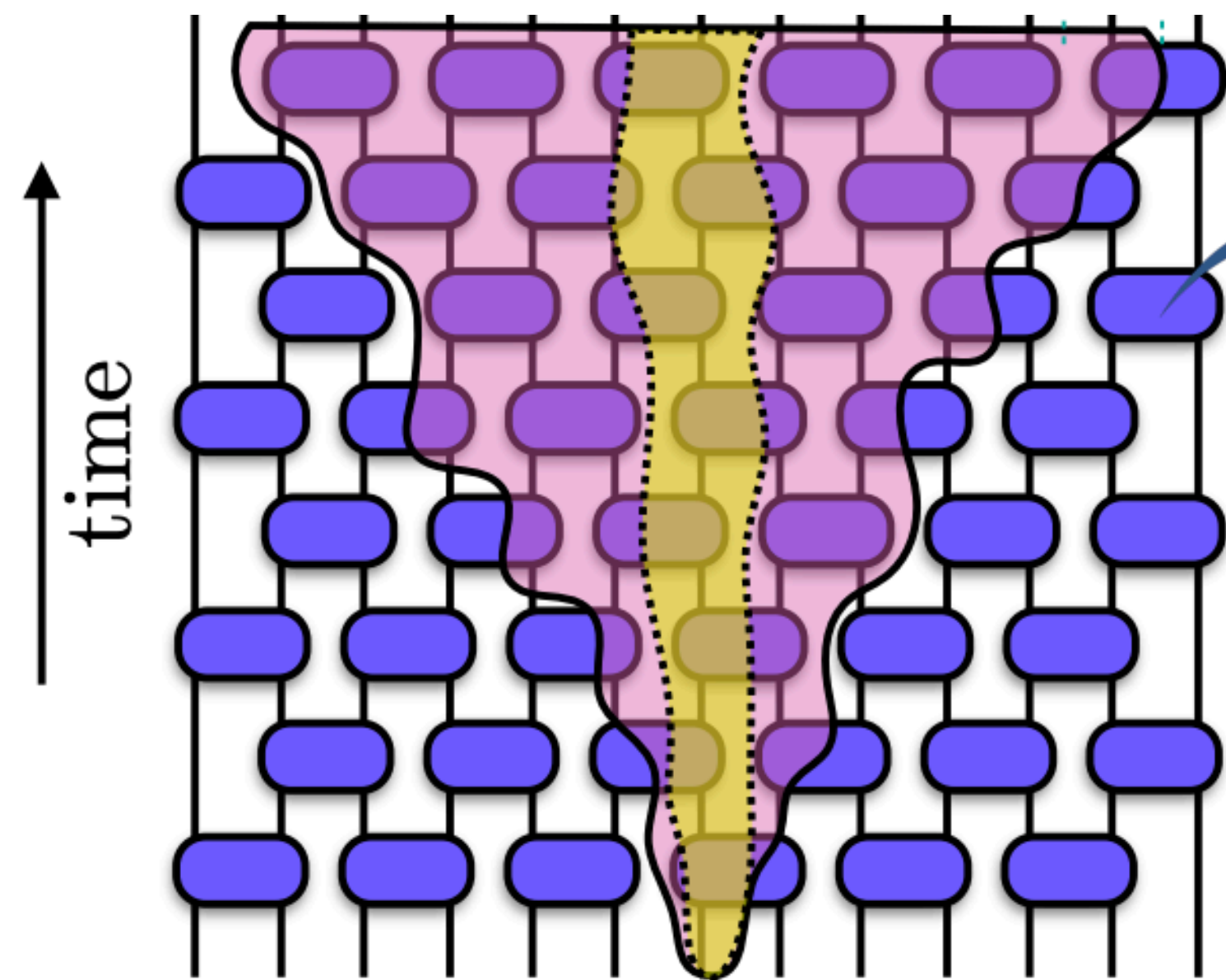
What intrinsically non-equilibrium phases of matter exist?

How do we characterize the capacity of a quantum network to retain coherent quantum information?

How do we characterize the computational capacity of a quantum network?

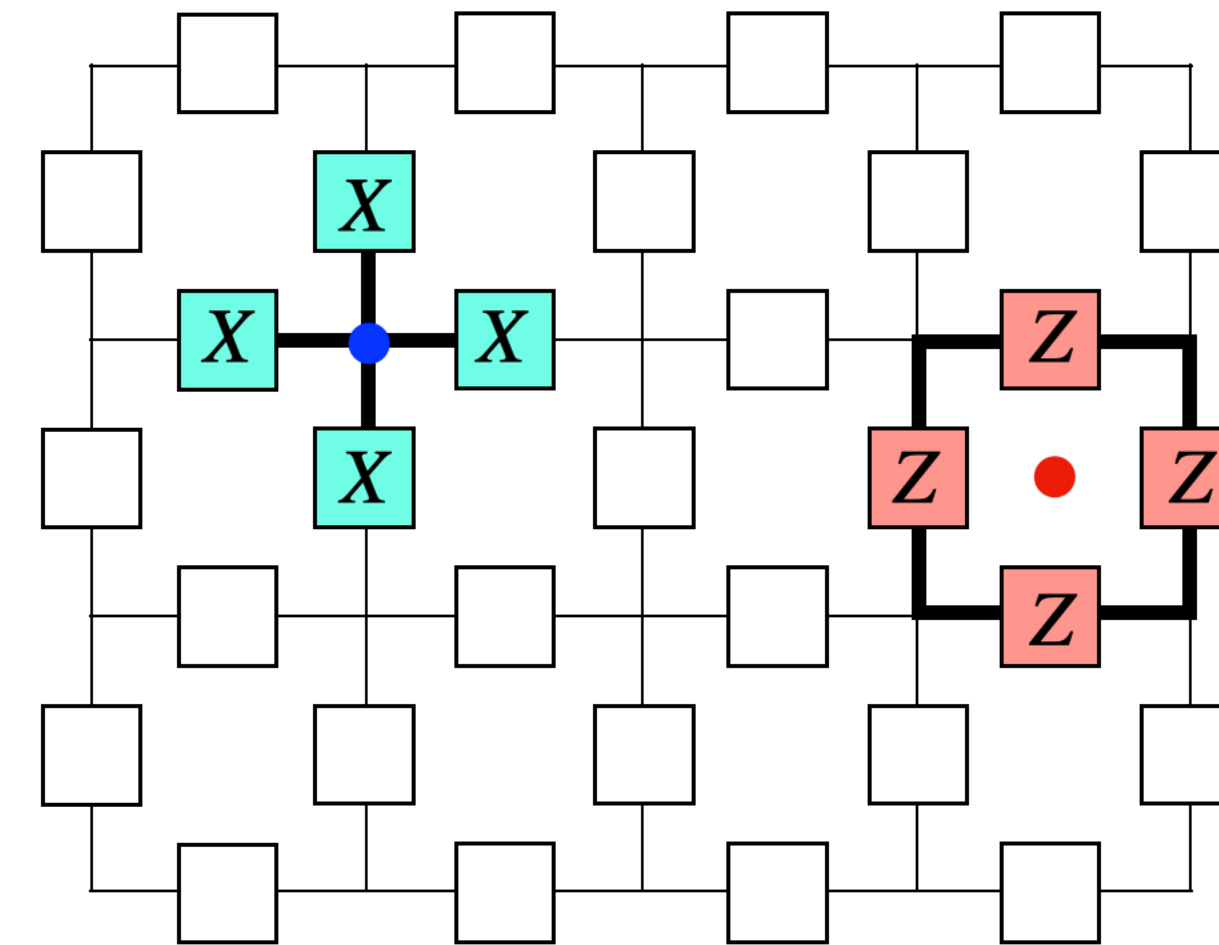
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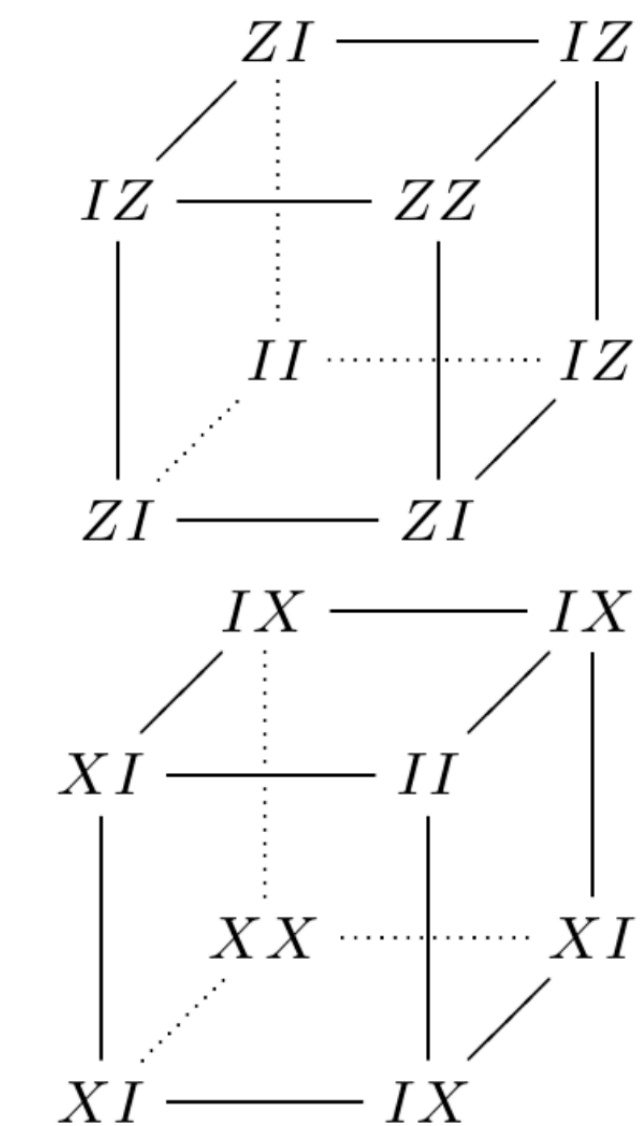


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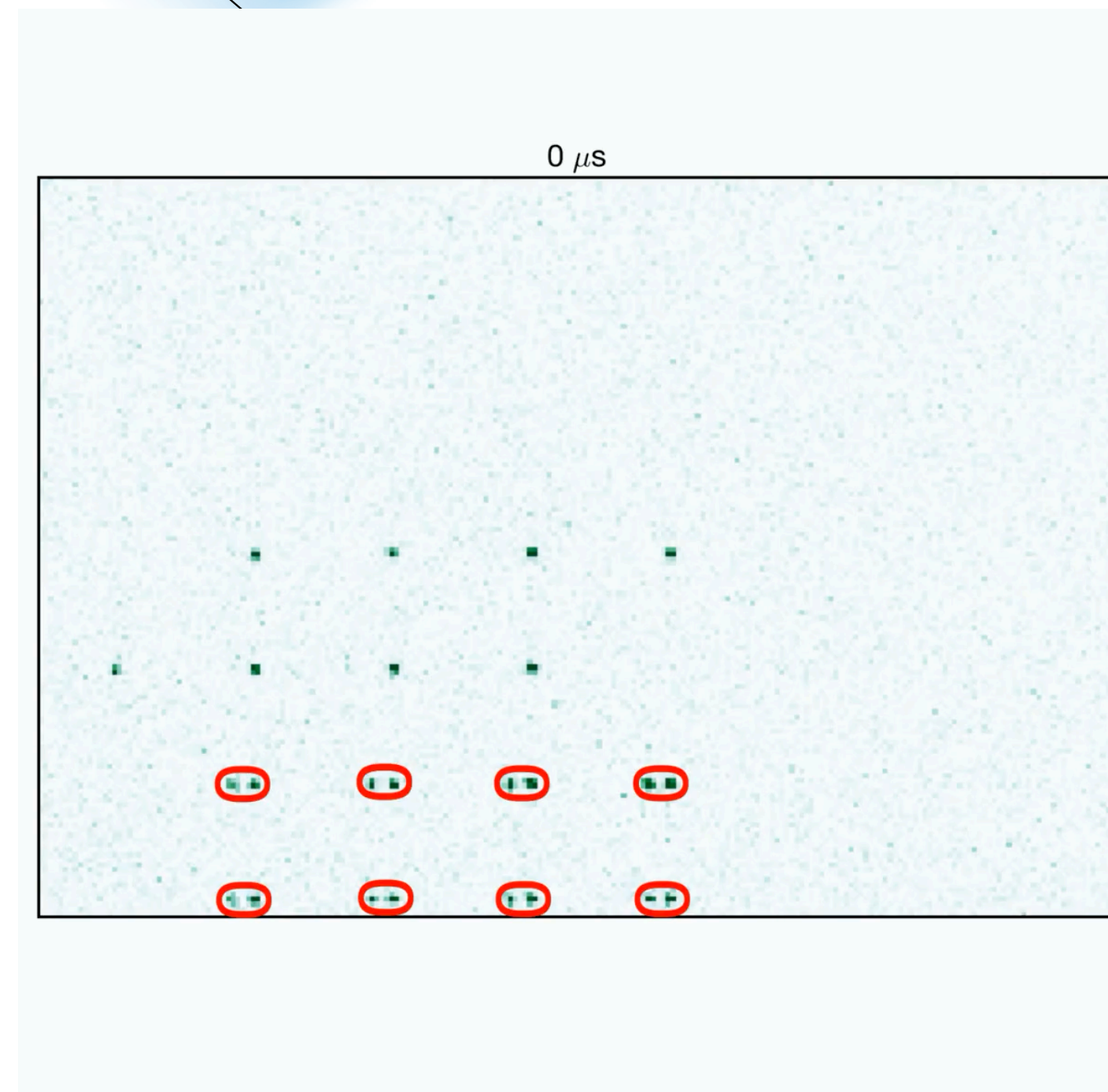
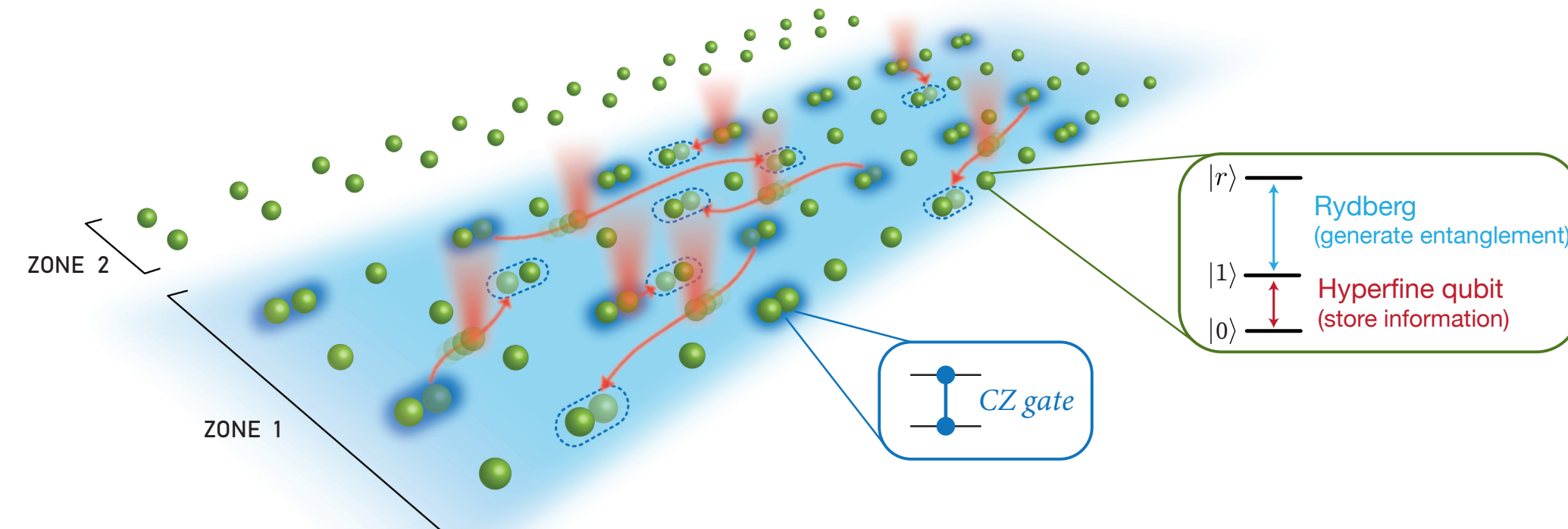
Kitaev's toric code
 $\leftrightarrow Z_2$ spin liquid



Haah's cubic code
 \leftrightarrow fracton phase

Engineered interactions
(new exotic phases)

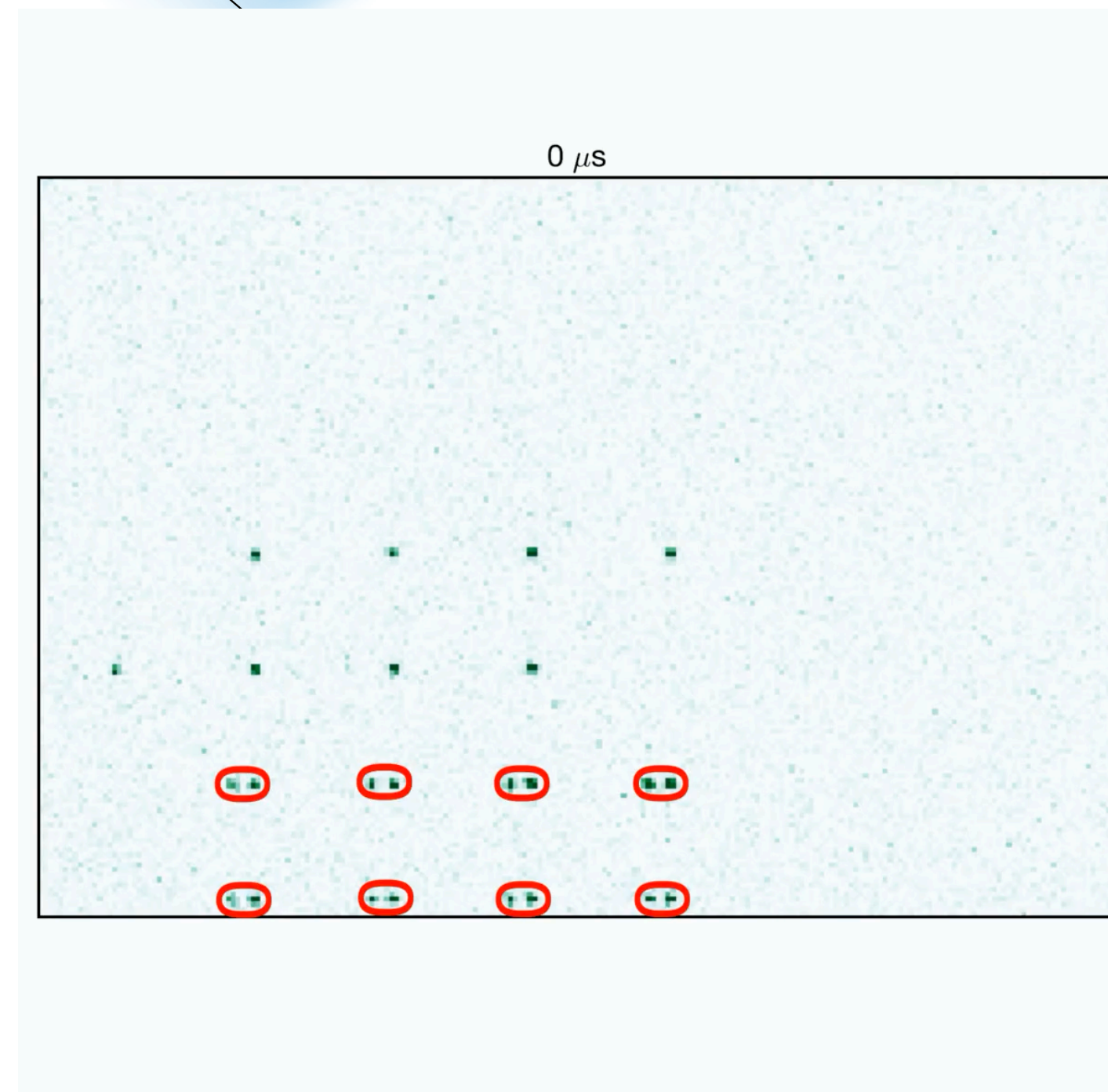
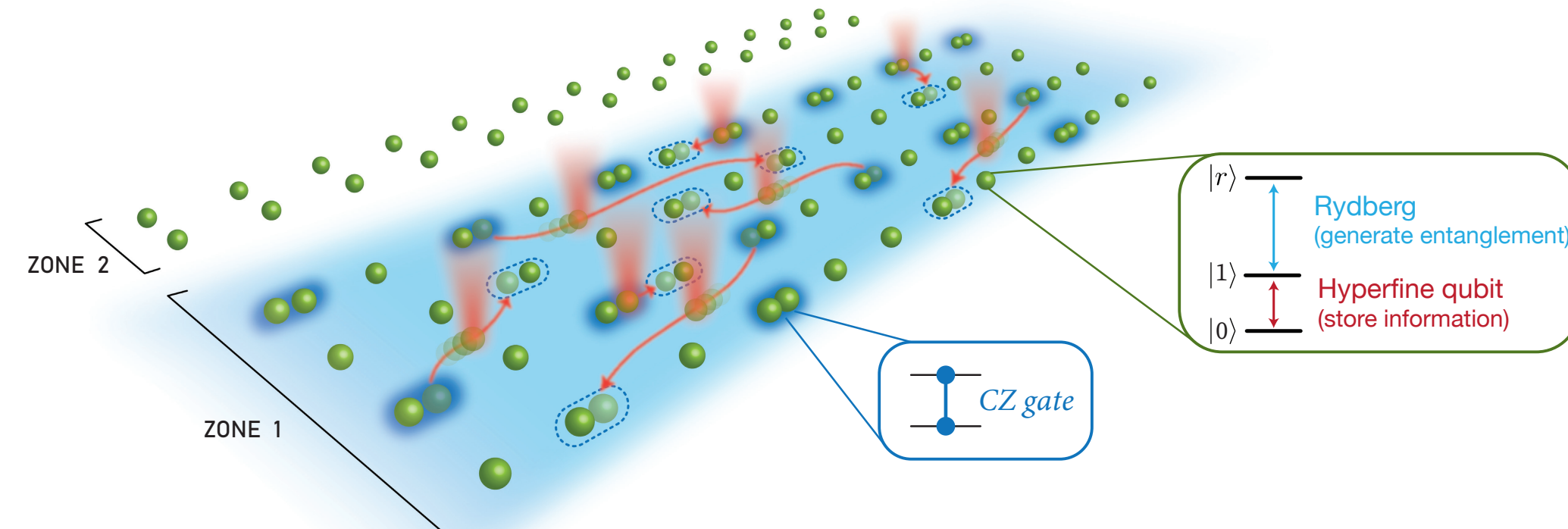
Controllable Geometry and Interactions



Bluvstein, ... , Lukin: Nature (2022)

Manetsch...Endres (2024)

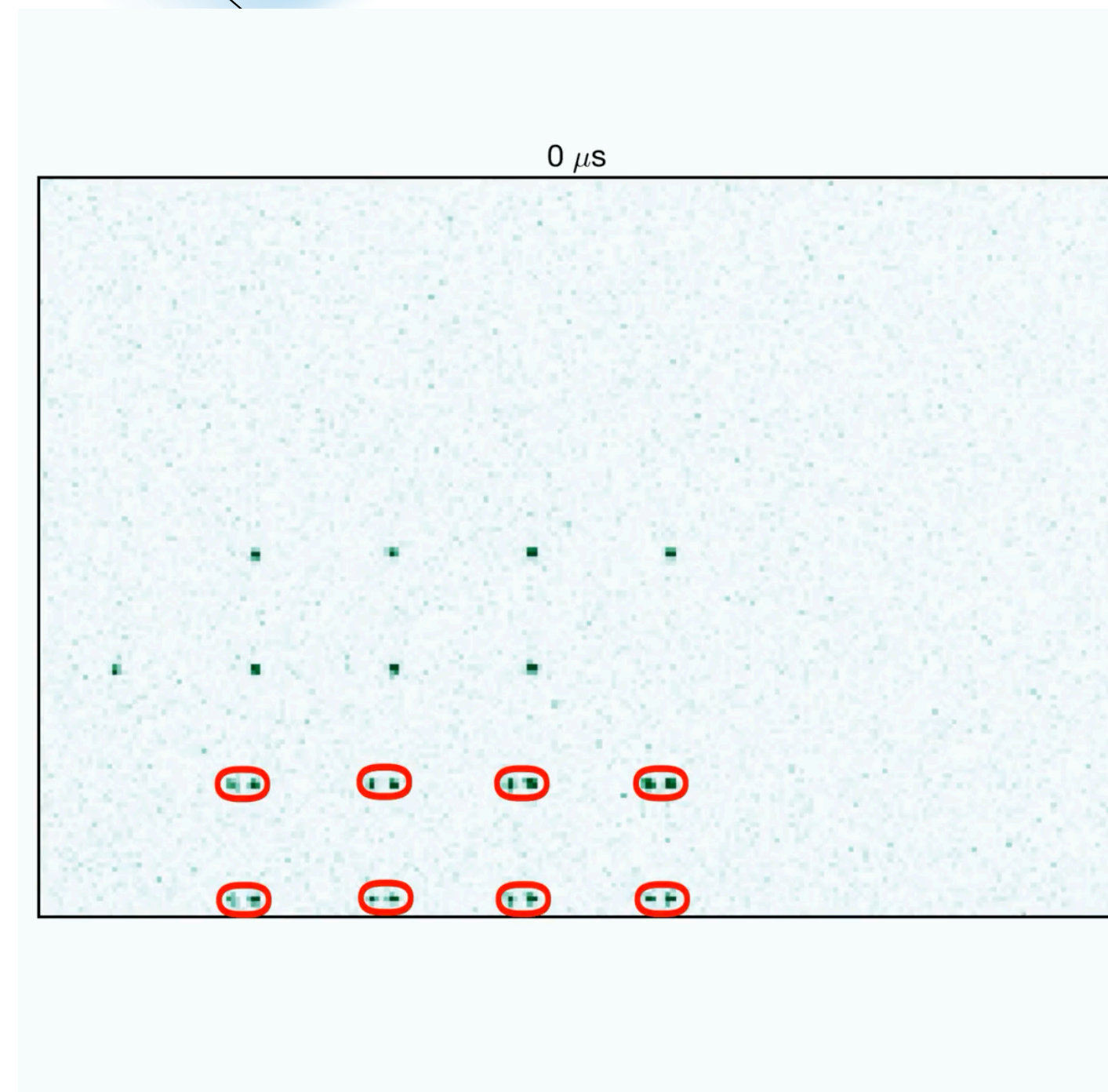
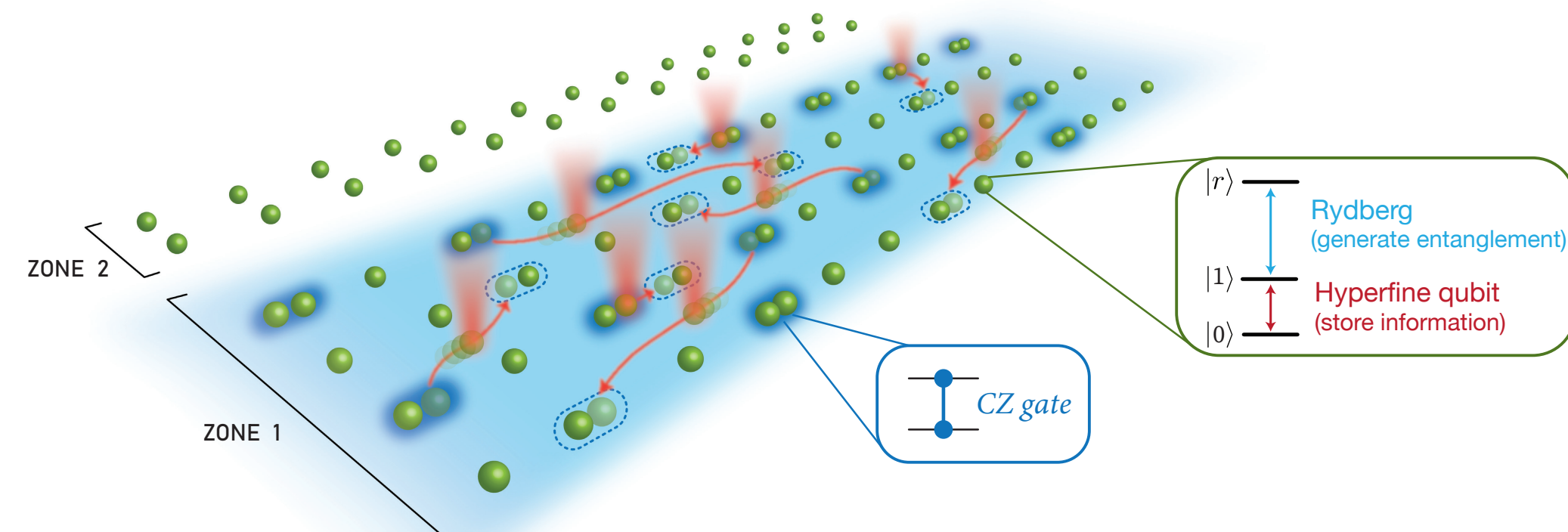
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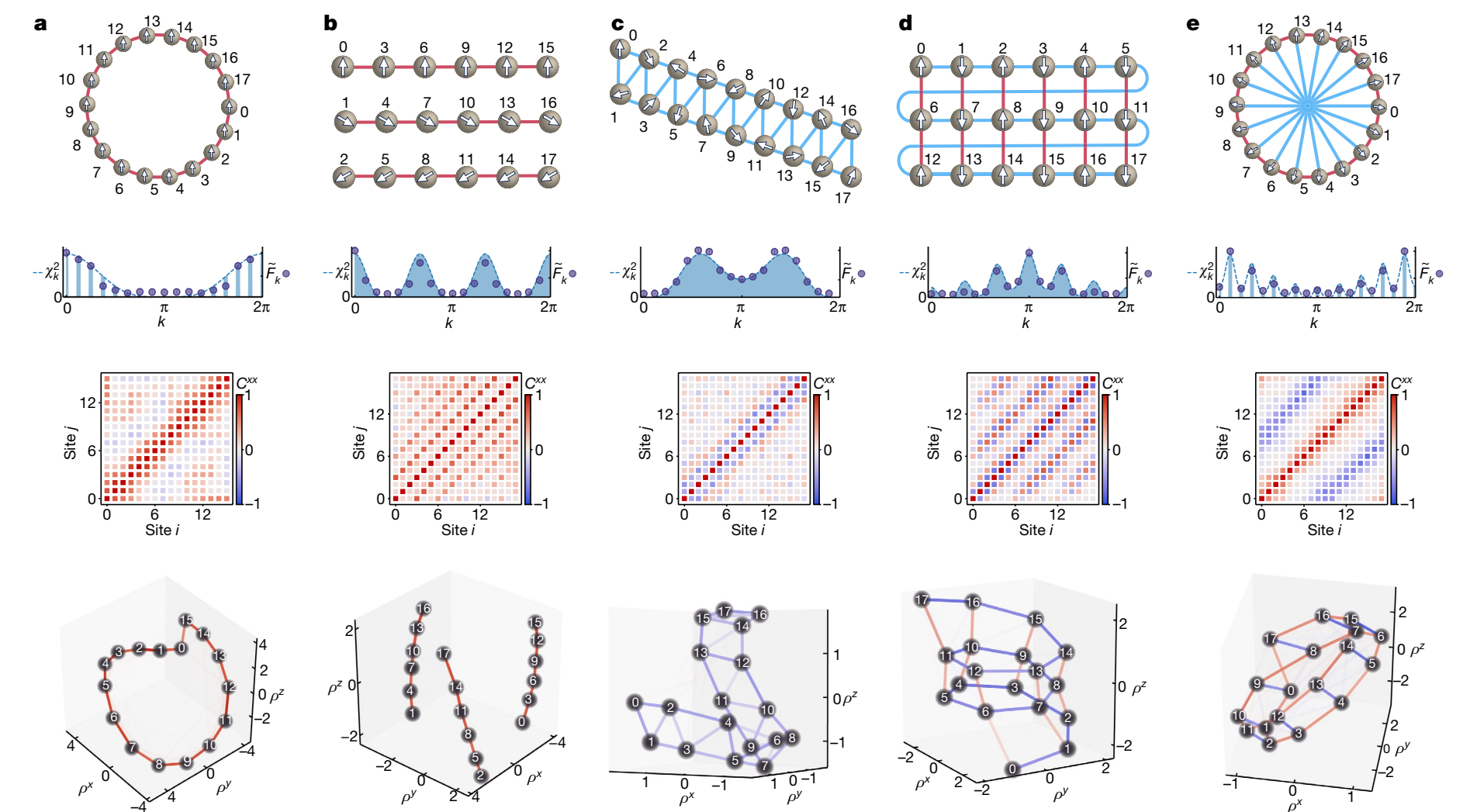
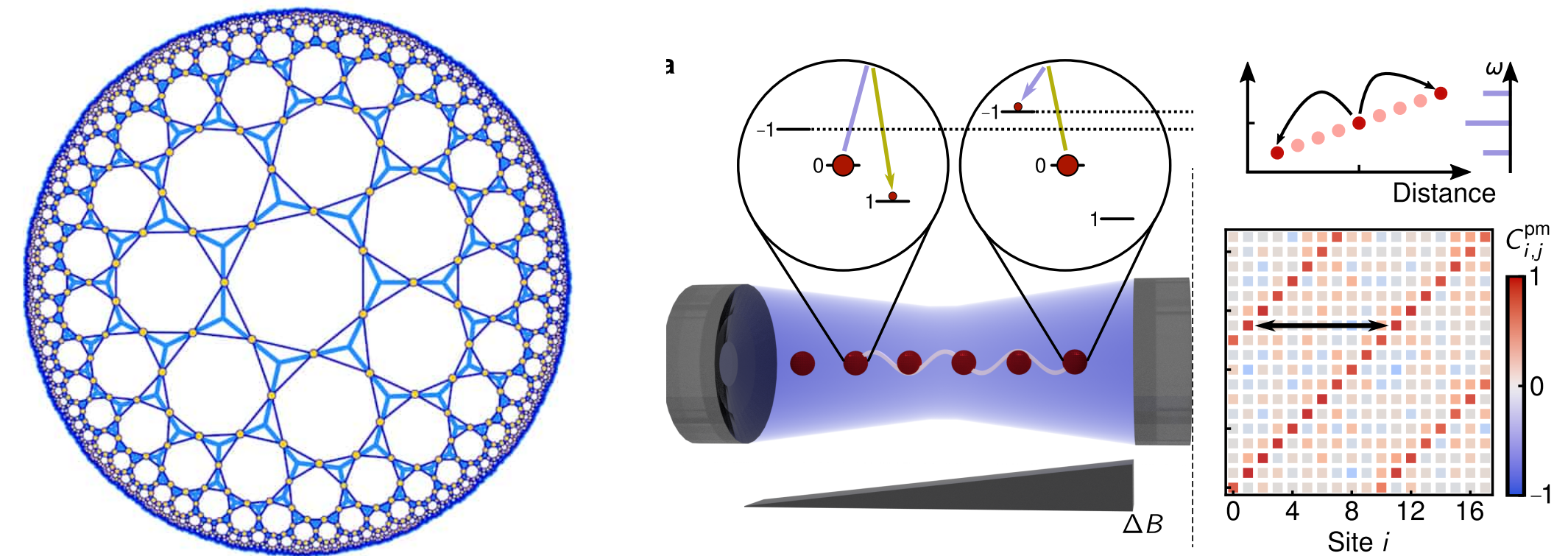
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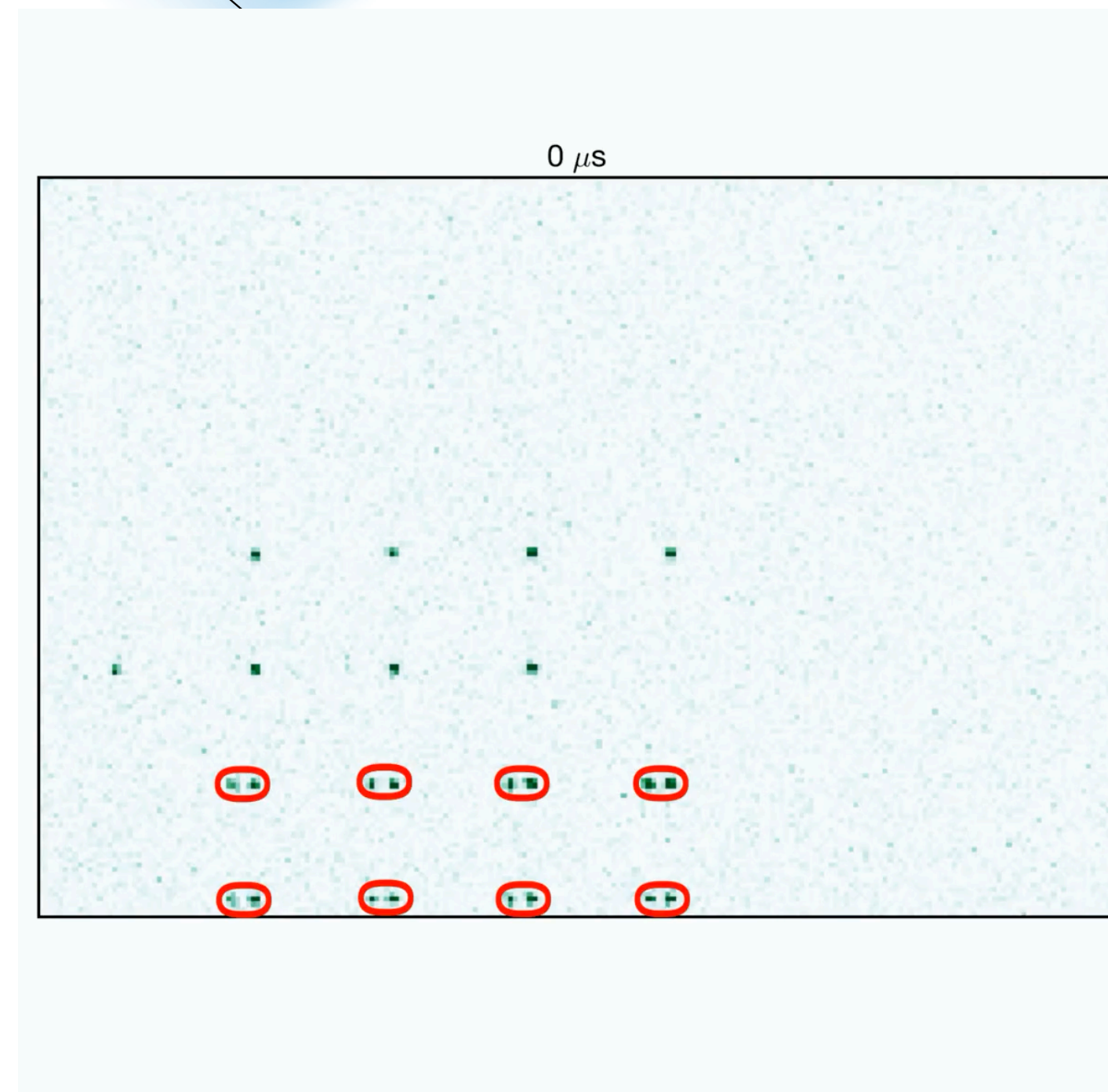
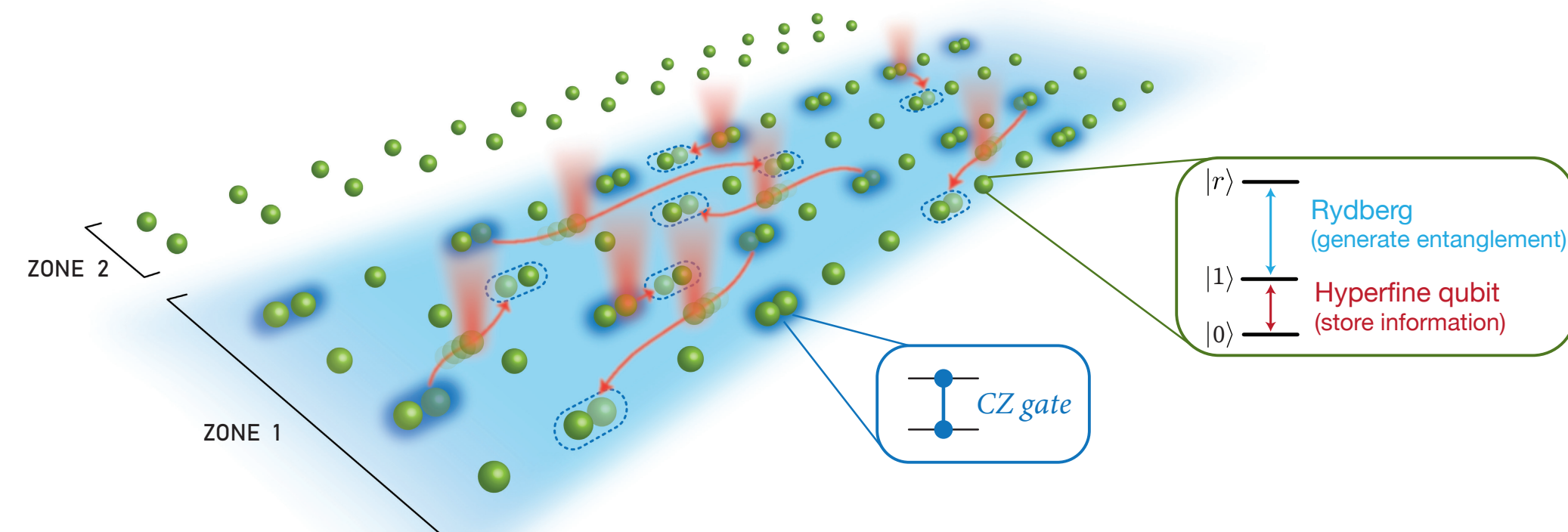
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Kollár, Fitzpatrick, Houck: Nature (2019)

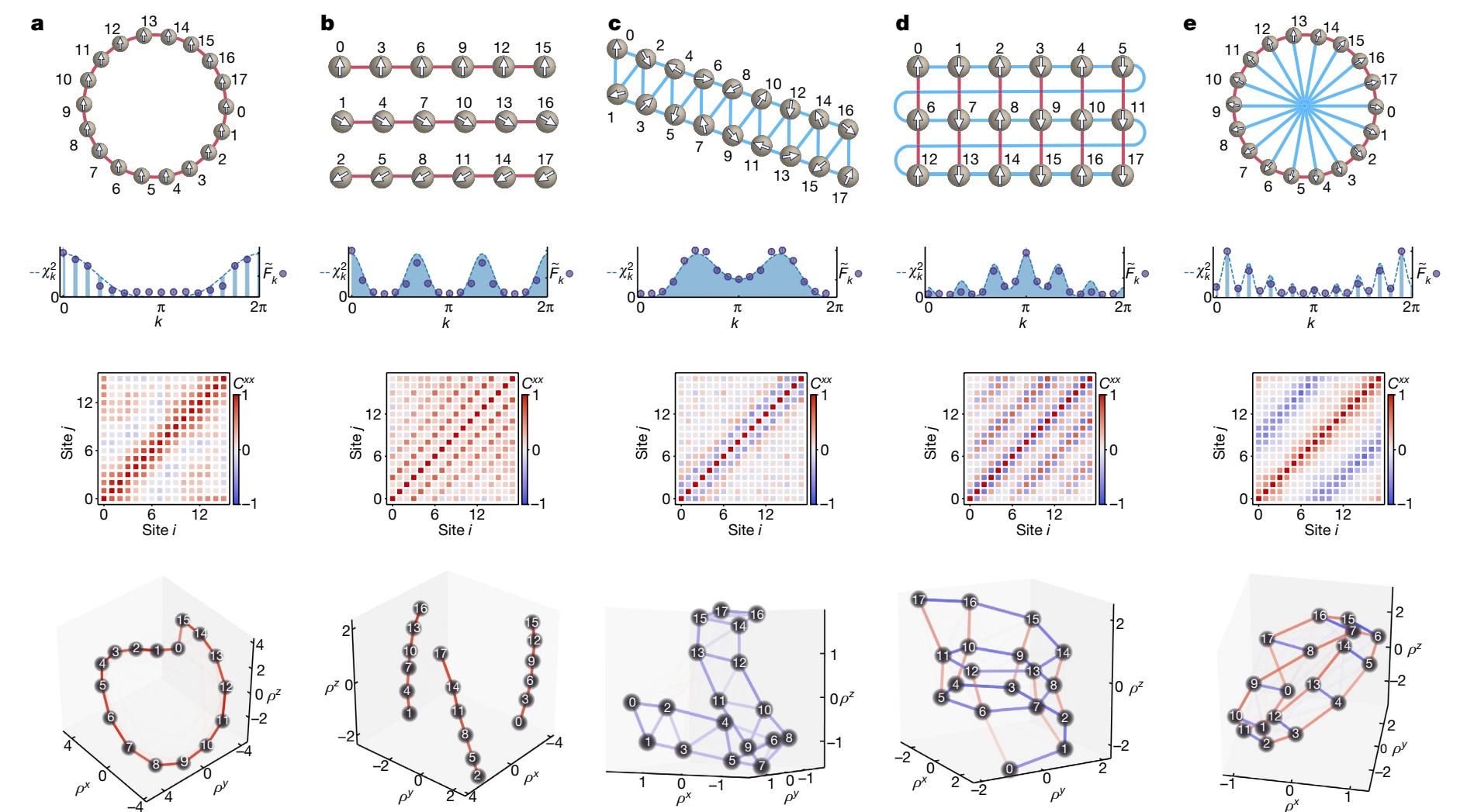
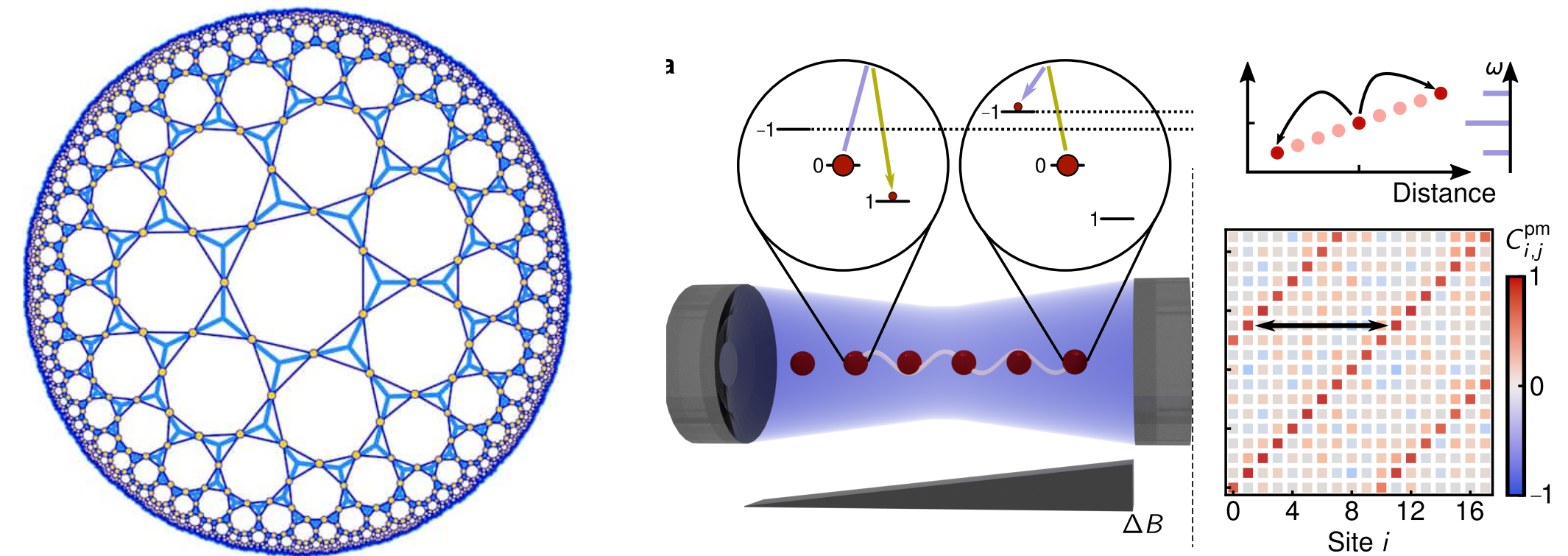
Periwal,...,Schleier-Smith: Nature (2021)

Controllable Geometry and Interactions



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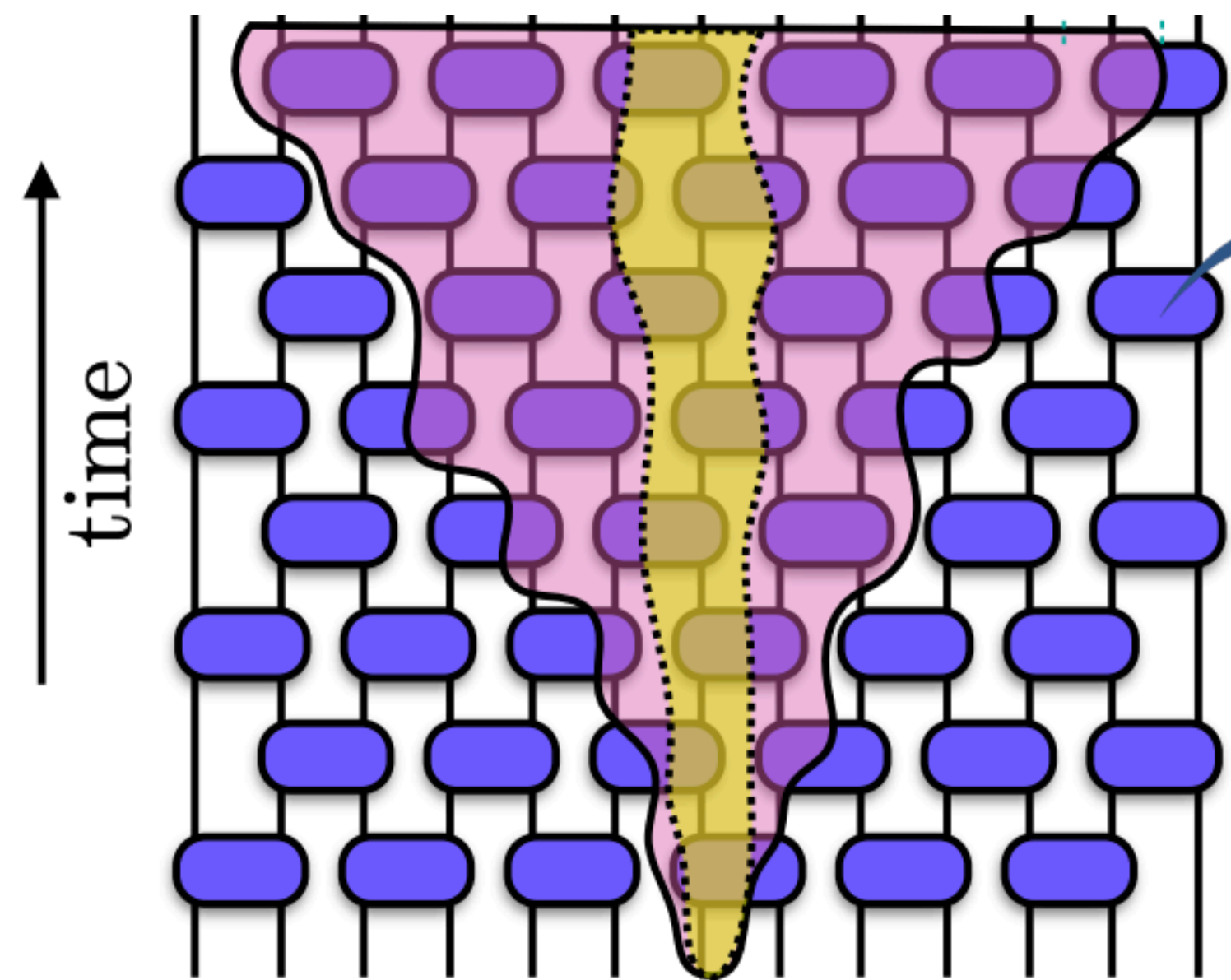


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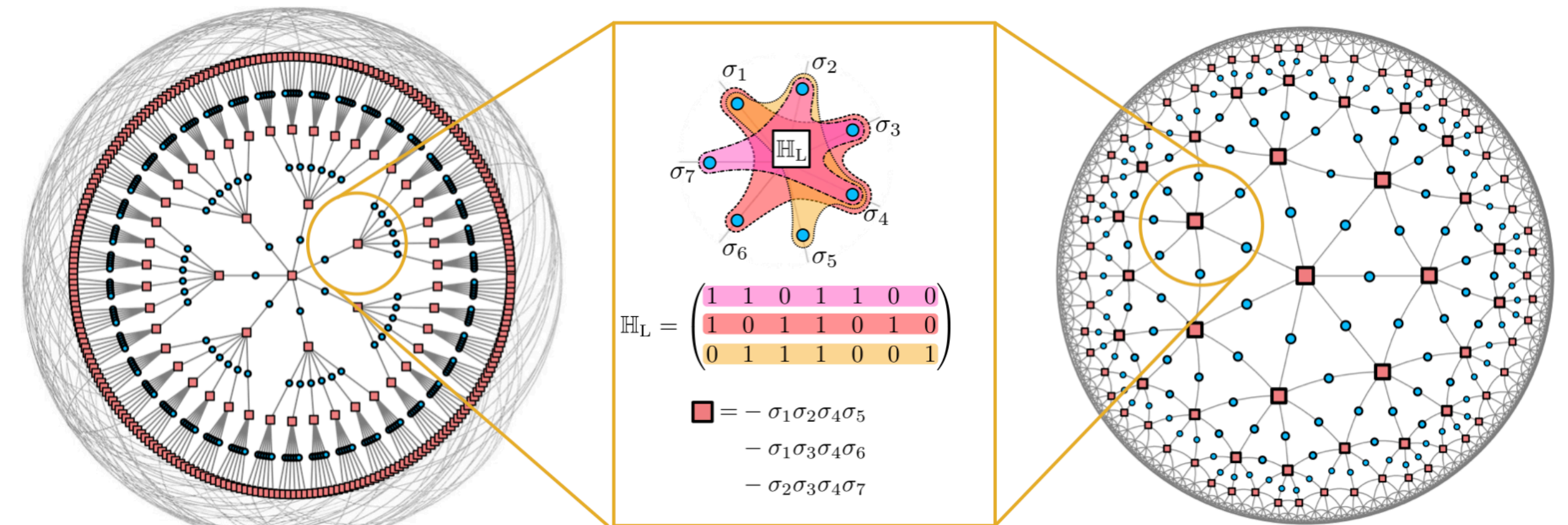
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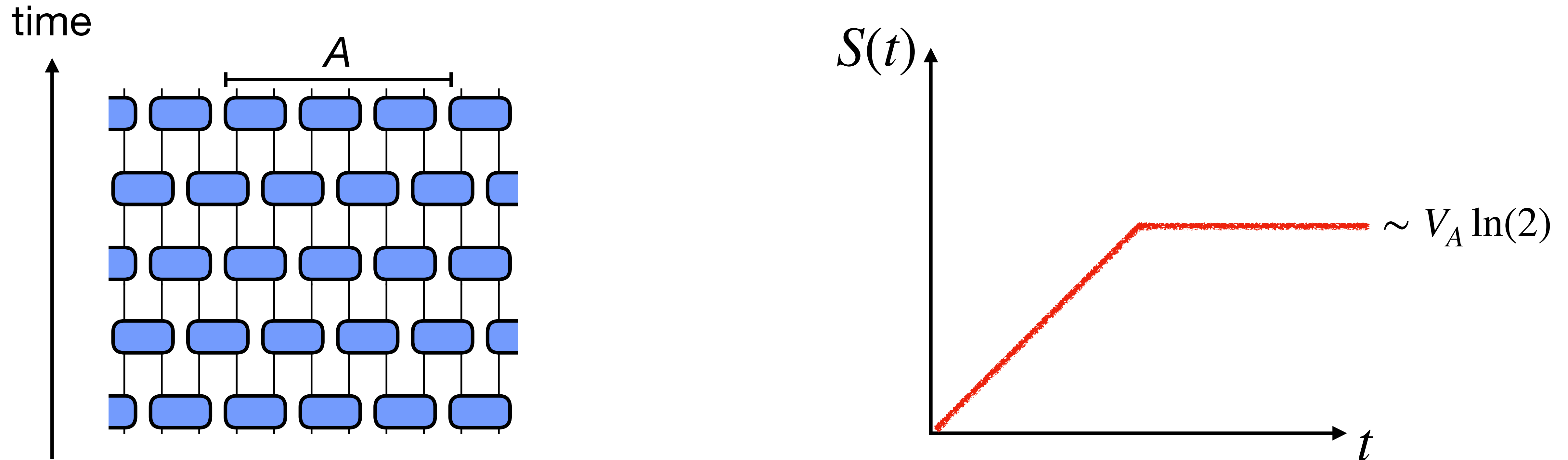


“good LDPC codes”

Engineered interactions and geometry
(new exotic phases)

Universality in Quantum Dynamics

Generic strongly-interacting isolated quantum systems are expected to thermalize: i.e. to evolve to entropy maximizing thermal states



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... interesting universality in the *approach* to thermal equilibrium:

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Dynamics of Entanglement

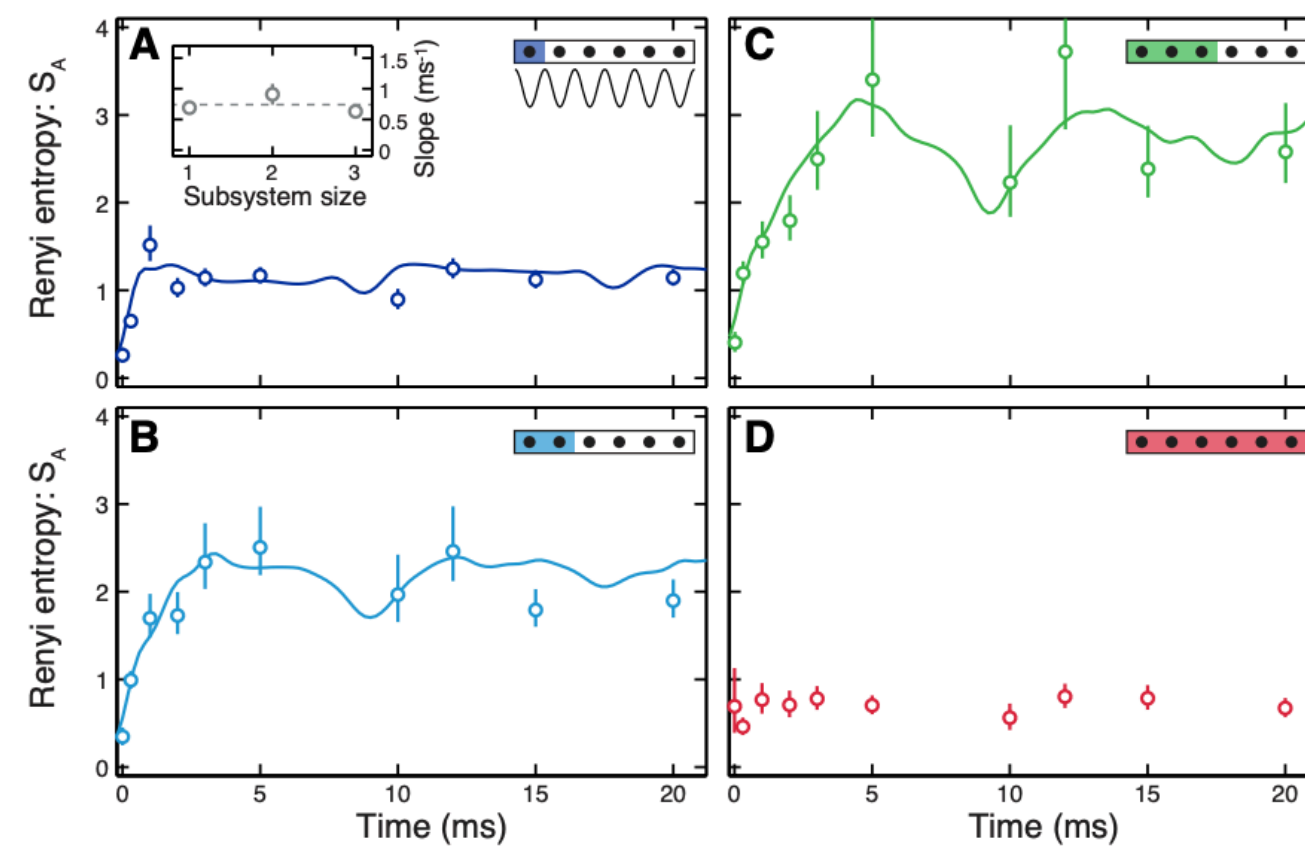
Dynamics of Information Scrambling

Emergence of Hydrodynamics

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... interesting universality in the *approach* to thermal equilibrium:

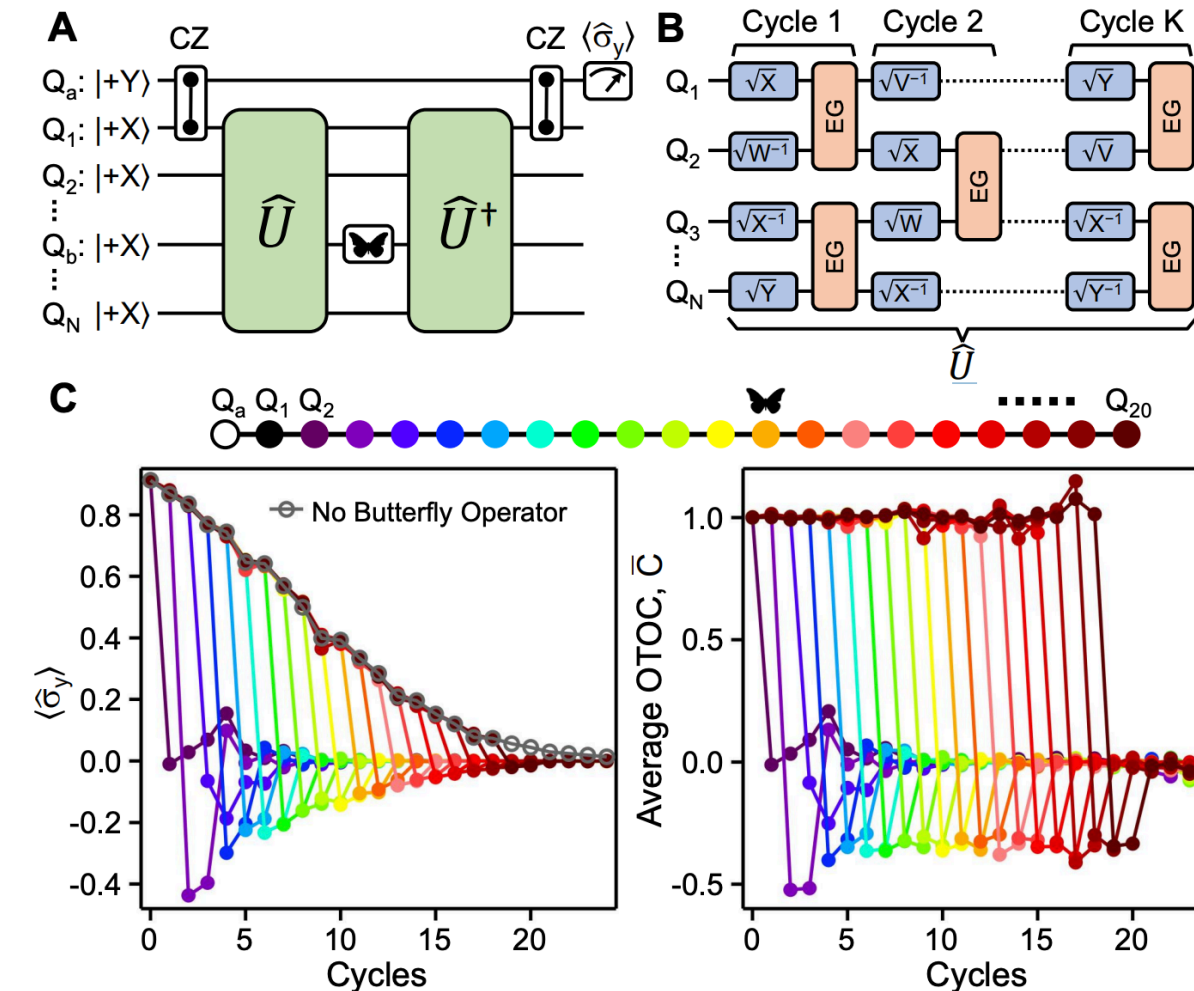
Dynamics of Entanglement



Kaufman...Greiner Science 2016

Nahum, Ruhman, Vijay Haah PRX 2017+ ...

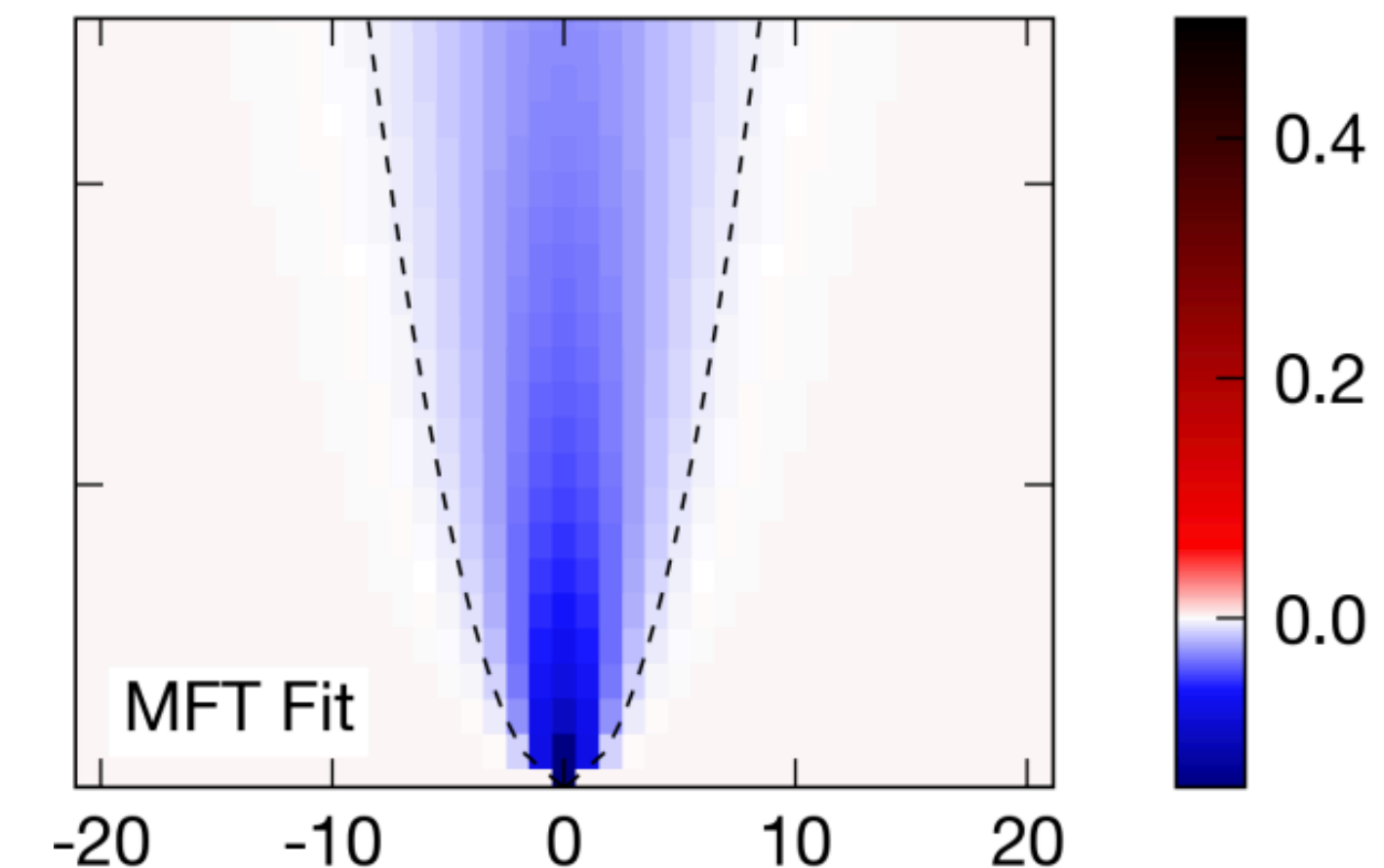
Dynamics of Information Scrambling



Google Quantum AI Science 2021

Nahum, Vijay Haah PRX 2017;
von Keyserlingk, Rakovszky, Pollmann, Sondhi PRX 2017+...

Emergence of Hydrodynamics

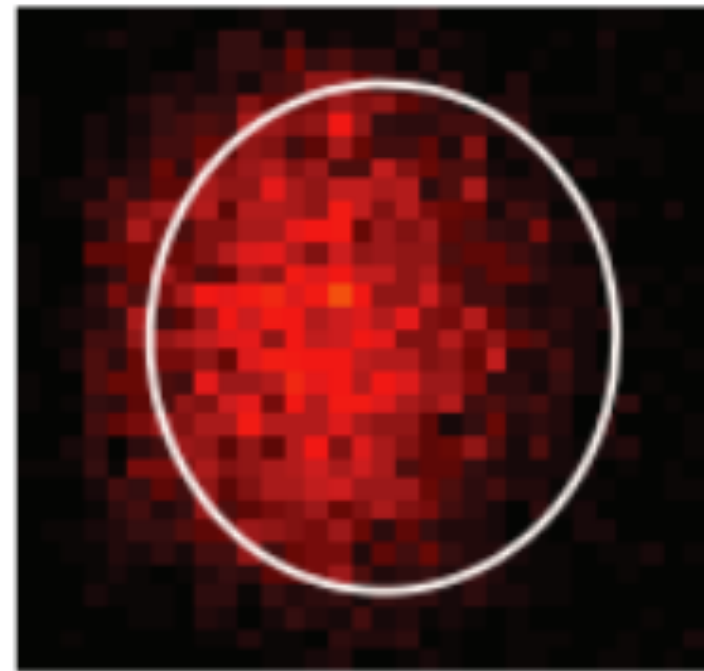
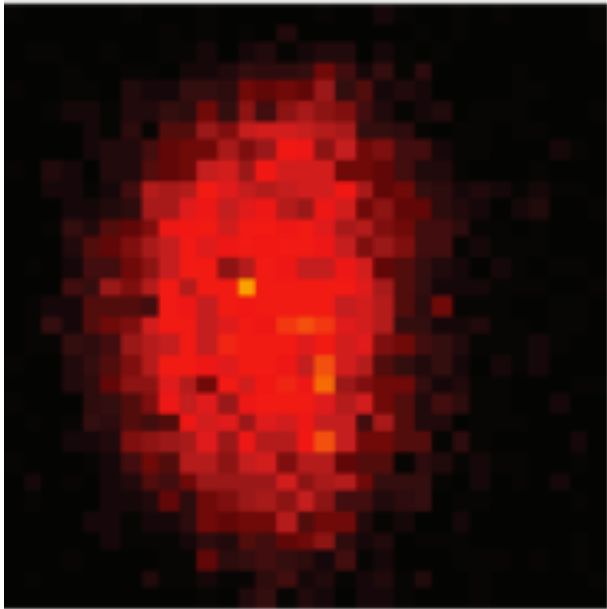
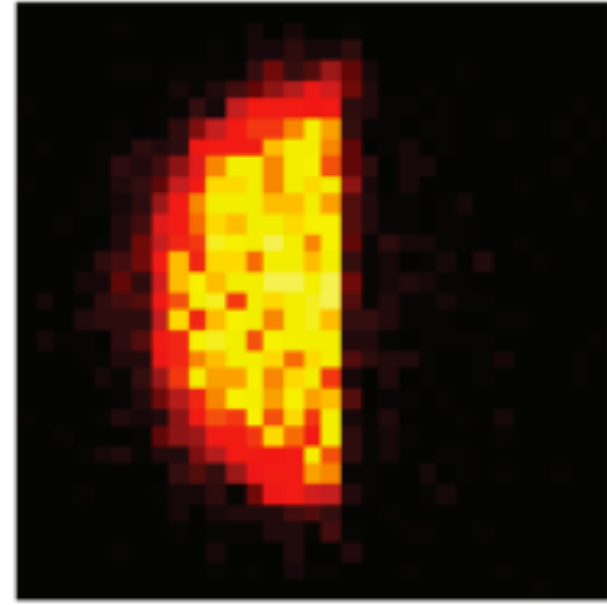


Weinand...Gopalakrishnan... Bloch 2023

VK. Vishwanath, Huse PRX 2018;
Rakovszky, Pollmann, von Keyserlingk PRX 2018+...

**Universal Non-Equilibrium
Phases by Evading
Thermalization**

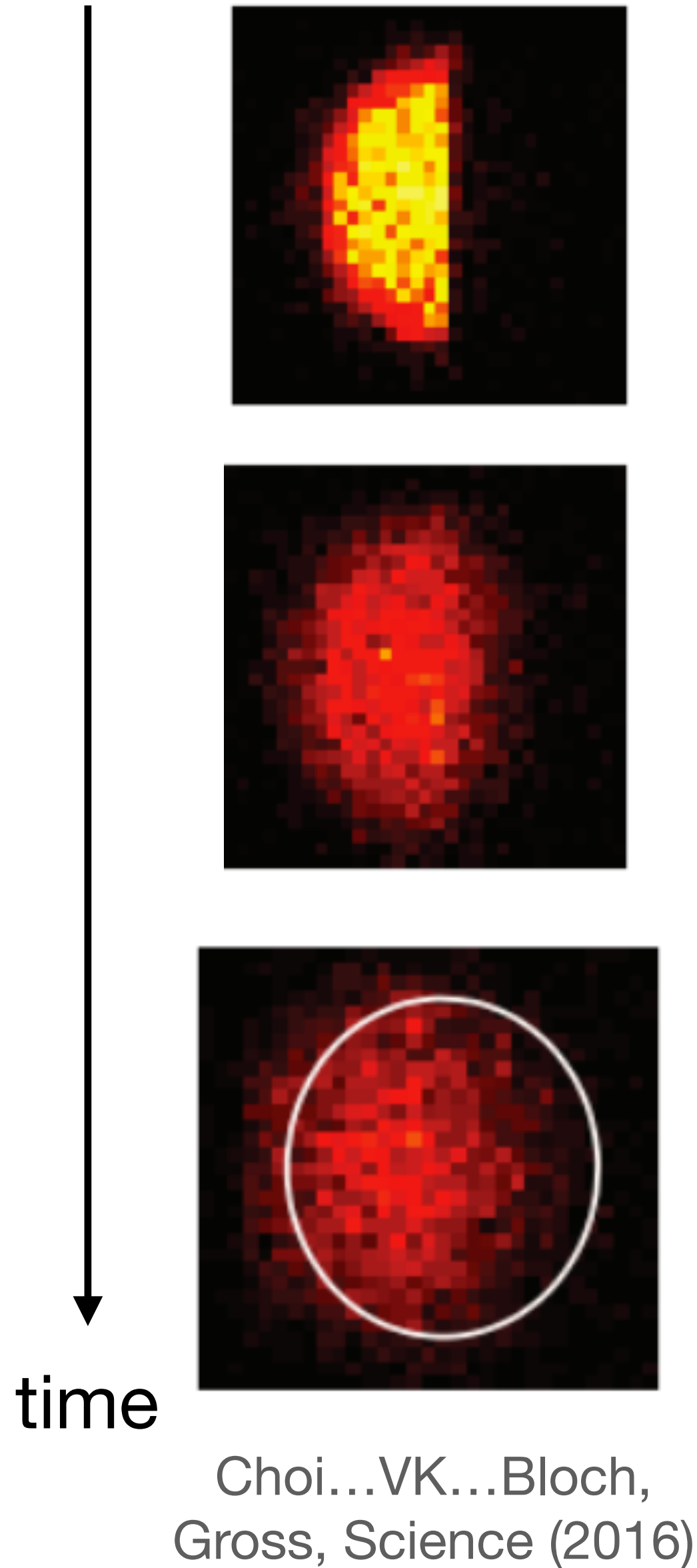
I. Many Body Localization



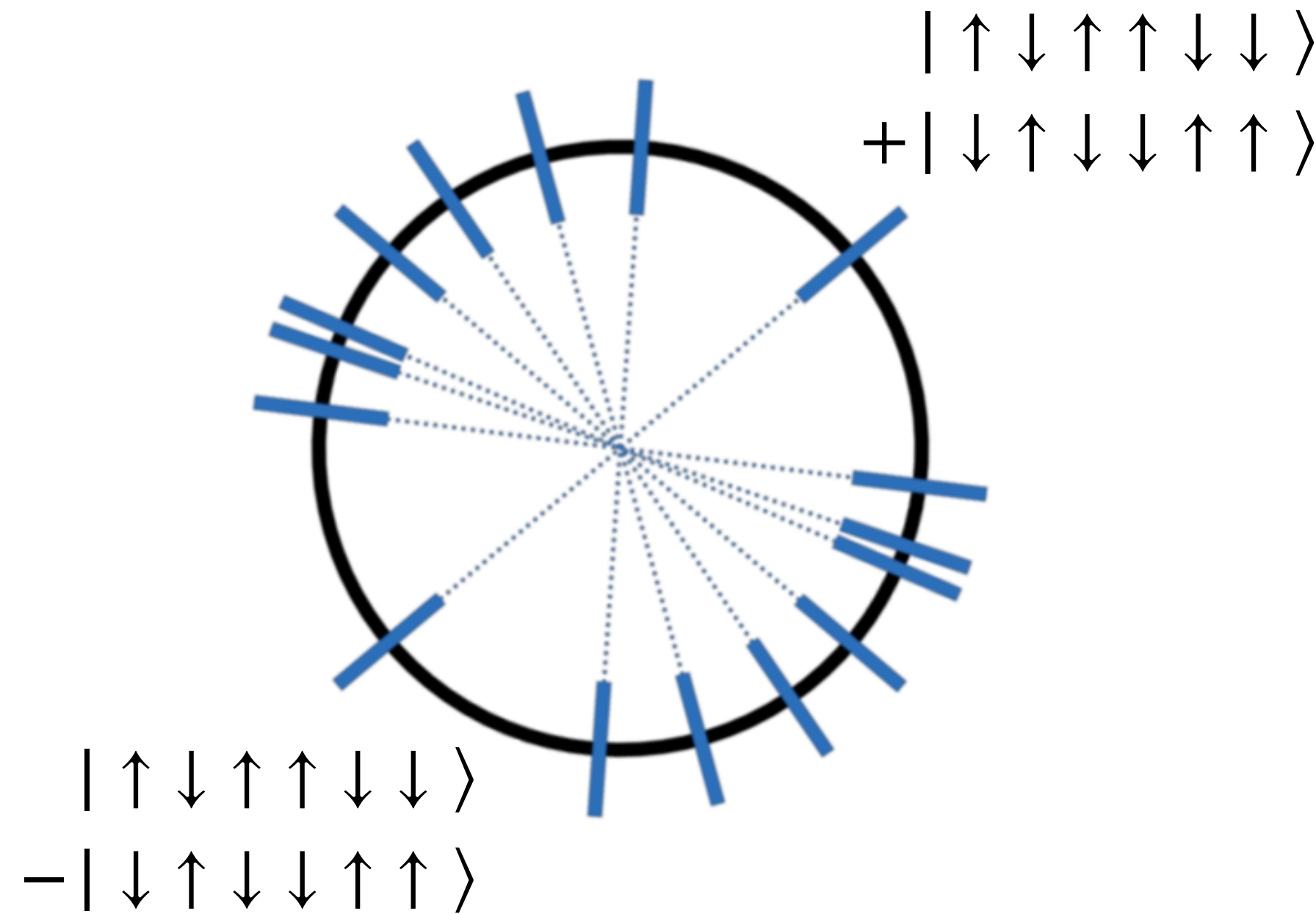
Choi...VK...Bloch,
Gross, Science (2016)

I. Many Body Localization

MBL Floquet Phases

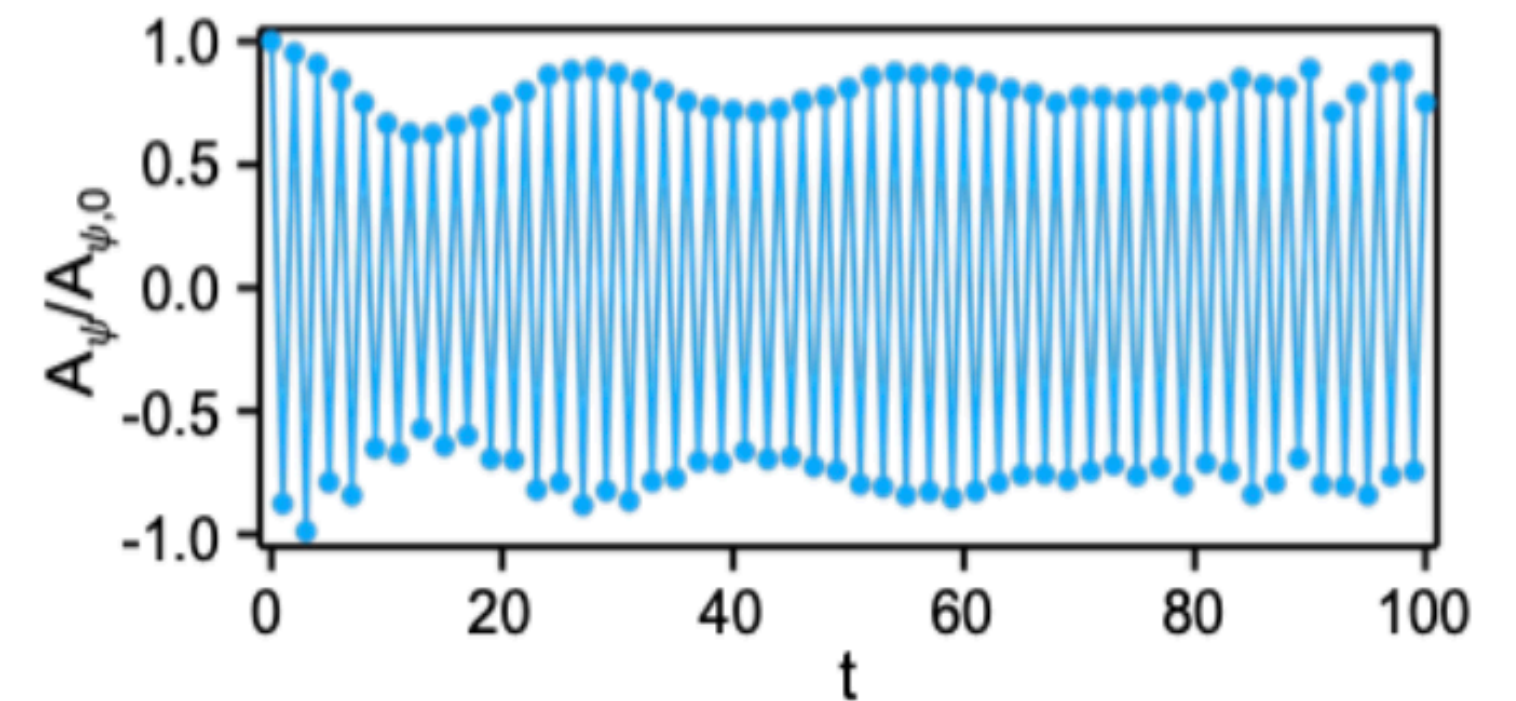
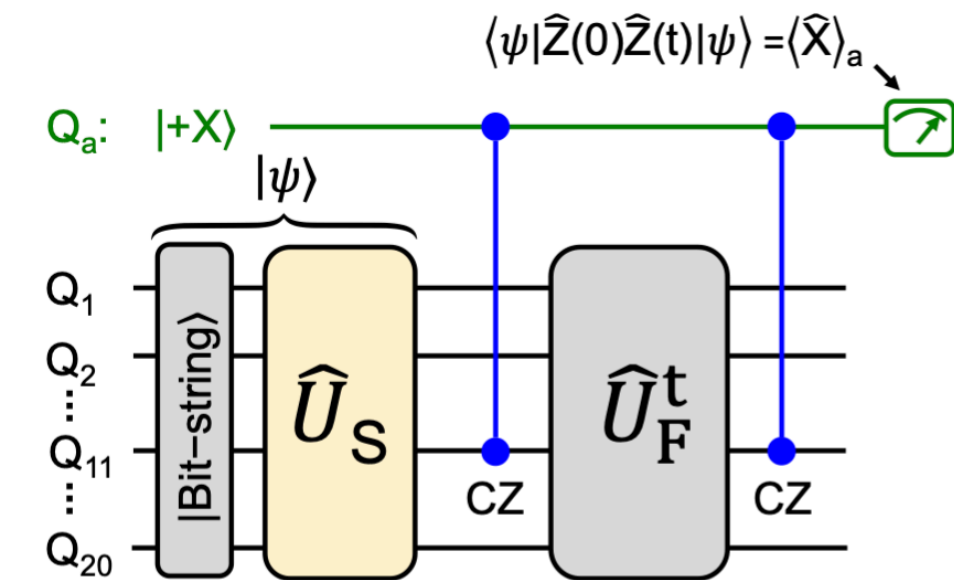
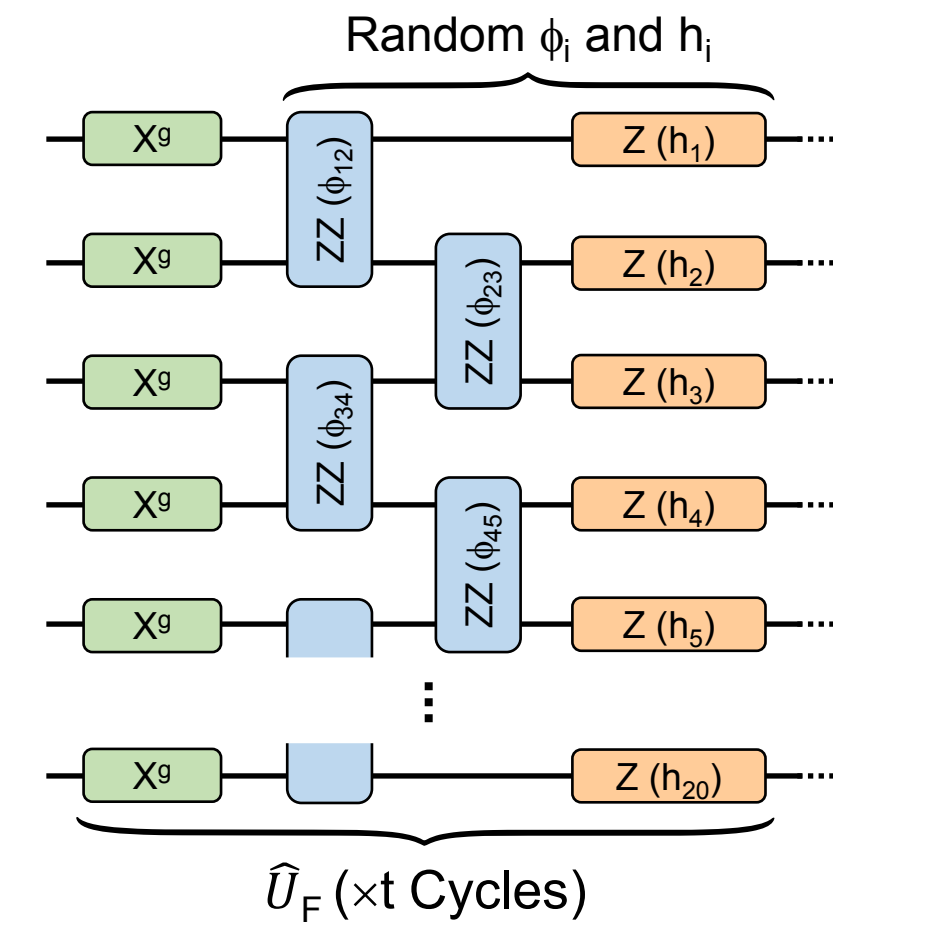


Anderson 1958; Basko Aleiner Altshuler
2006; Oganesyan Huse 2007 + ...



Time-Crystalline
eigenstate order
(spatiotemporal)

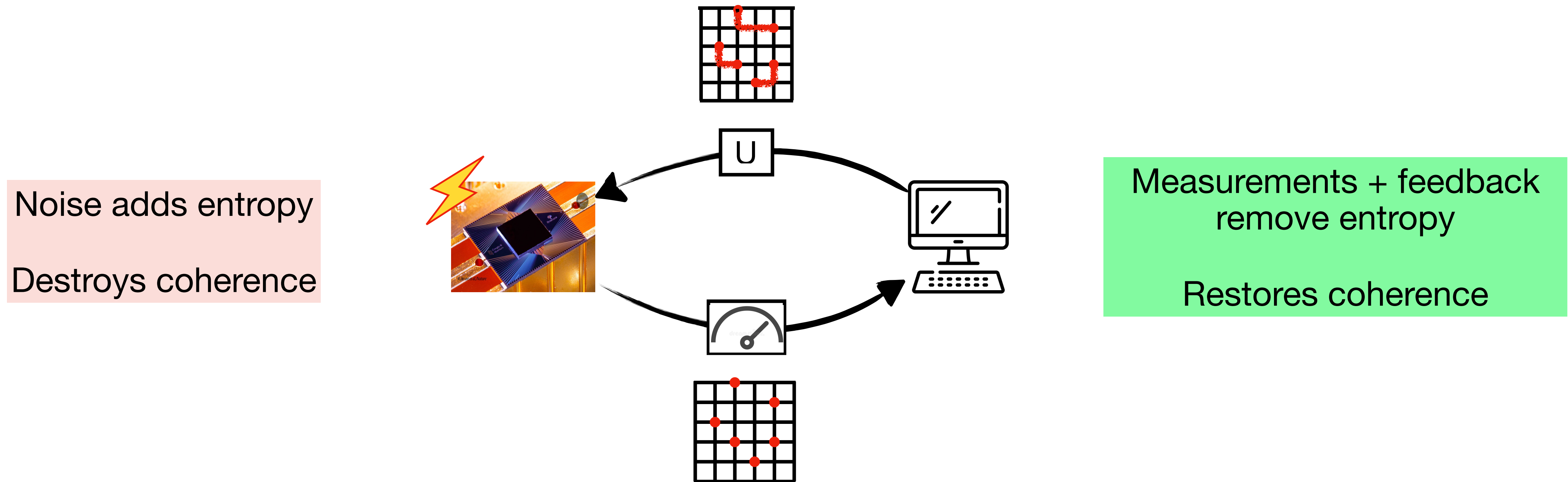
VK. Lazarides, Moessner, Sondhi (2015)
Else Bauer Nayak (2016)+ ...



Mi, Ippoliti...VK, Roushan, Nature (2022)

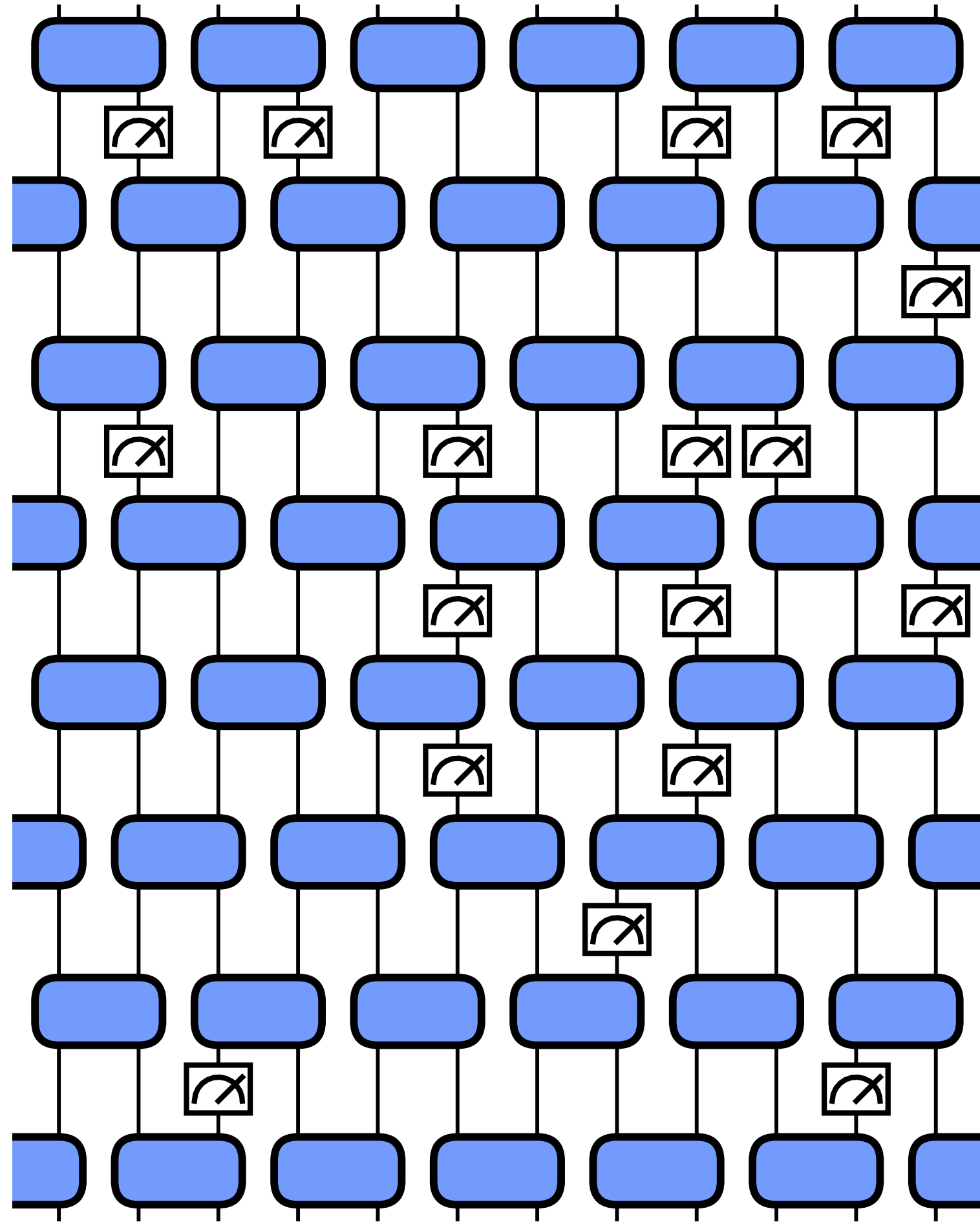
II. Monitored Dynamics: Controlled Measurements

Active error correction



Information protection via information processing

Monitored Dynamics: Controlled Measurements



Measurement *as a **part*** of many-body dynamics

Measurements can have a dramatic effect on the state being measured: can **create, destroy and restructure** quantum correlations.

Get new **nonequilibrium phases** defined by **structure of quantum information in spacetime**

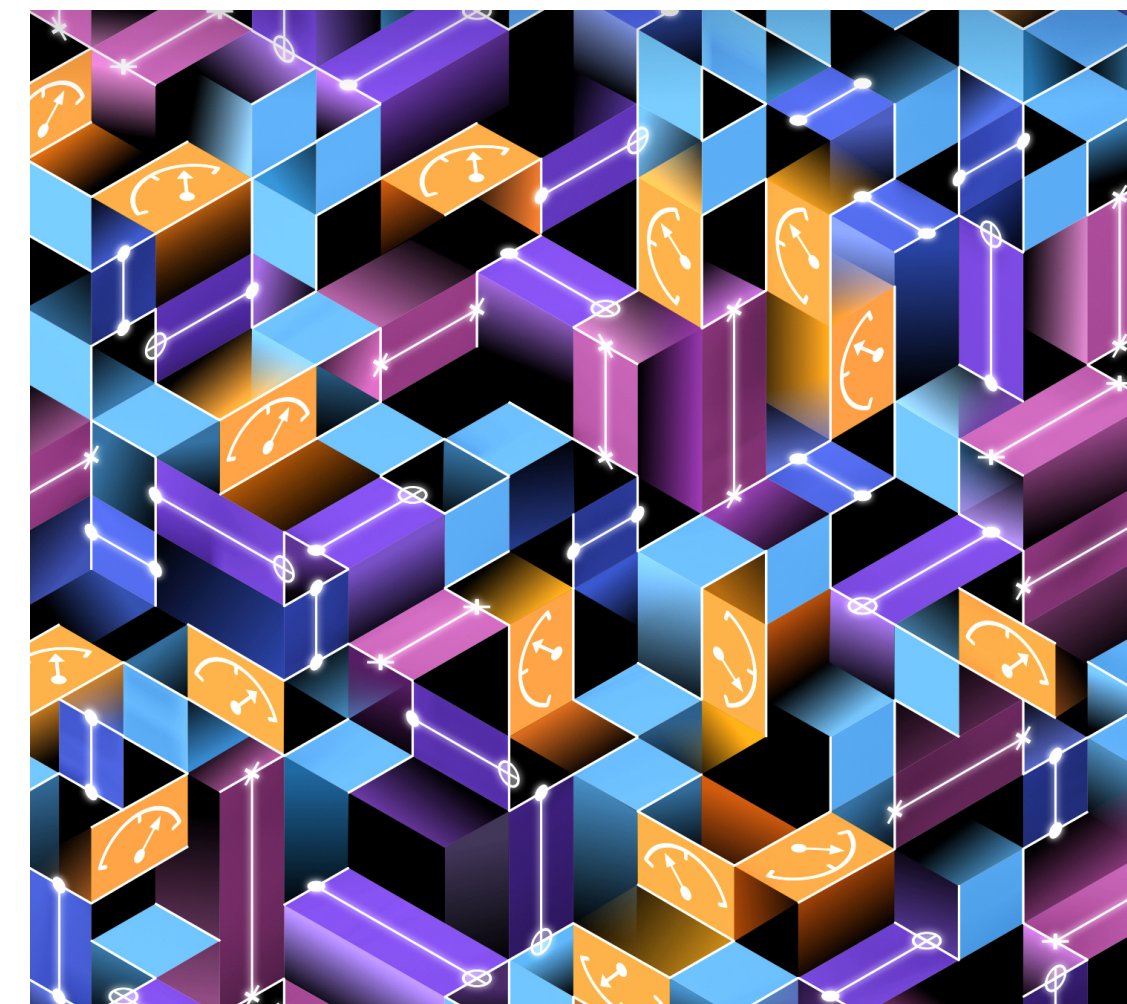
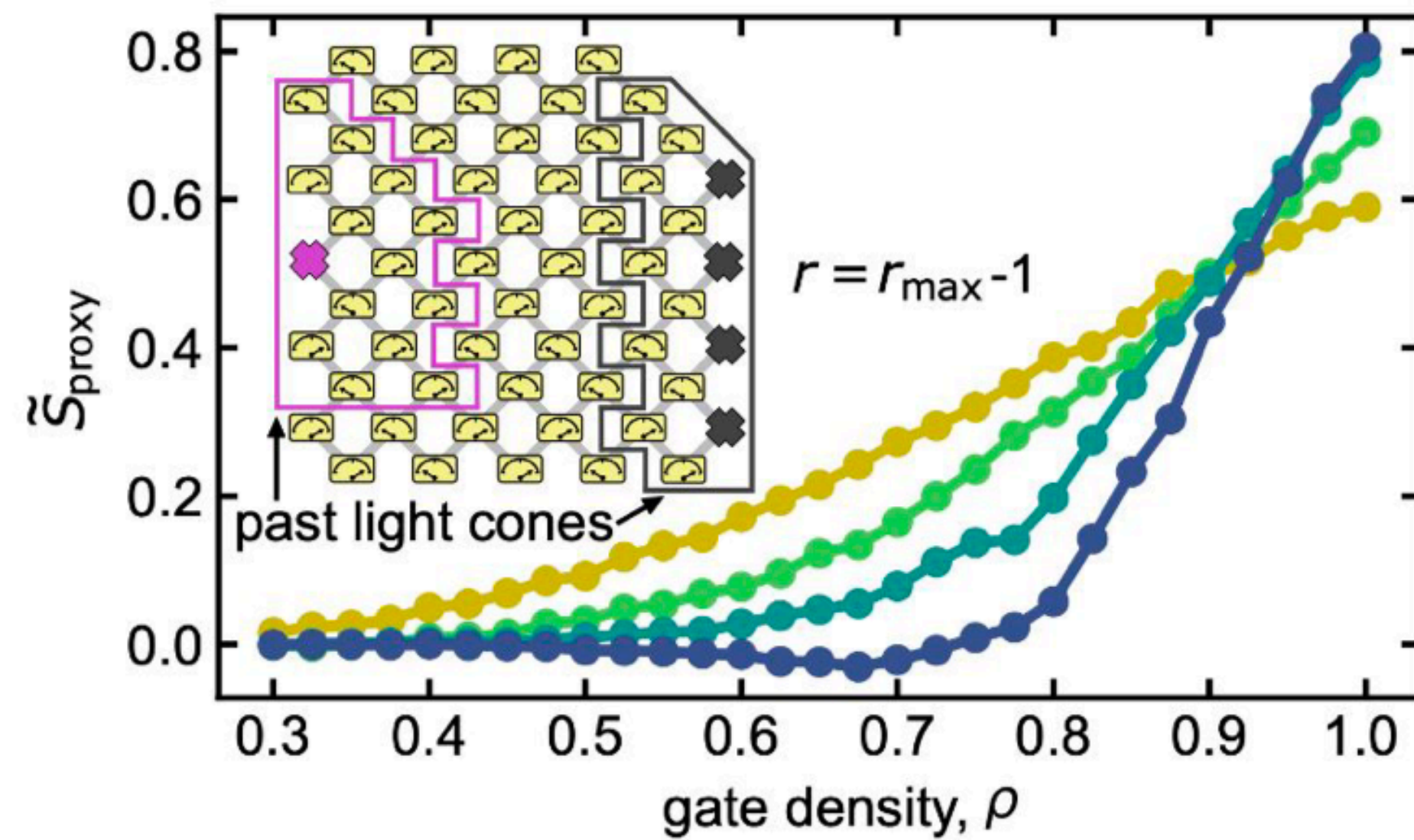
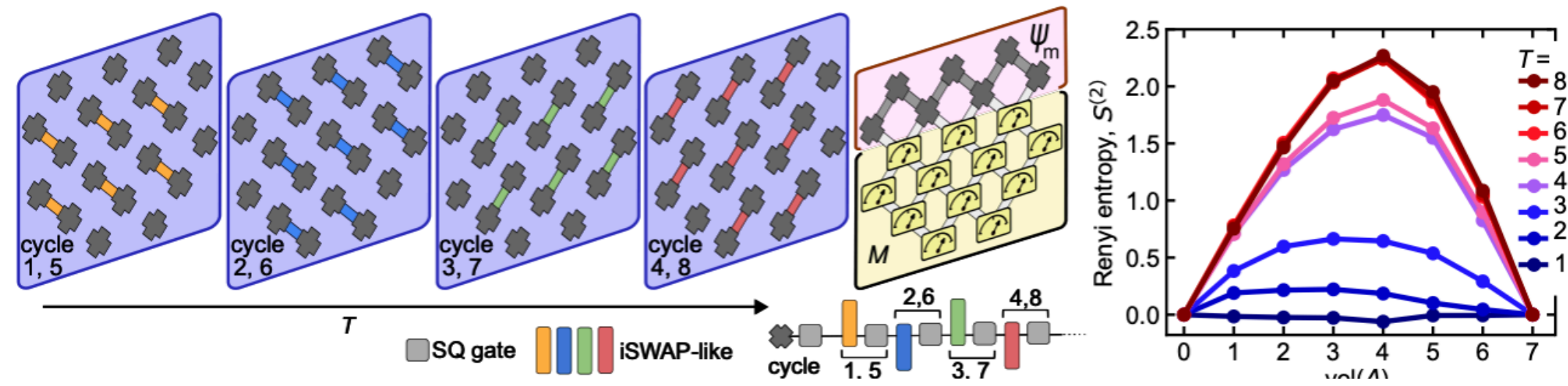


Image: Google Quantum AI

Monitored Dynamics: Controlled Measurements

Measurement Induced Phase Transition *in individual quantum trajectories*

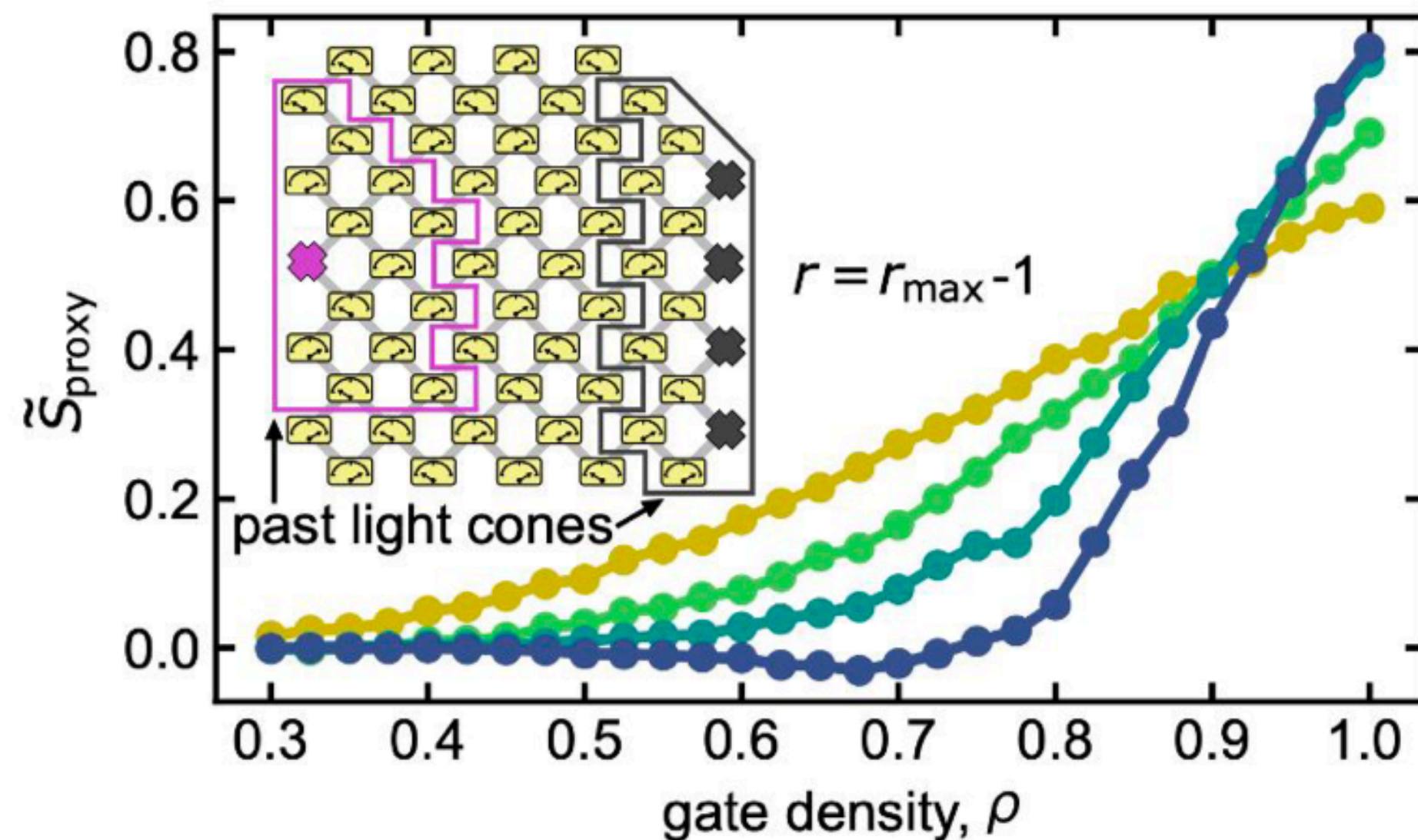
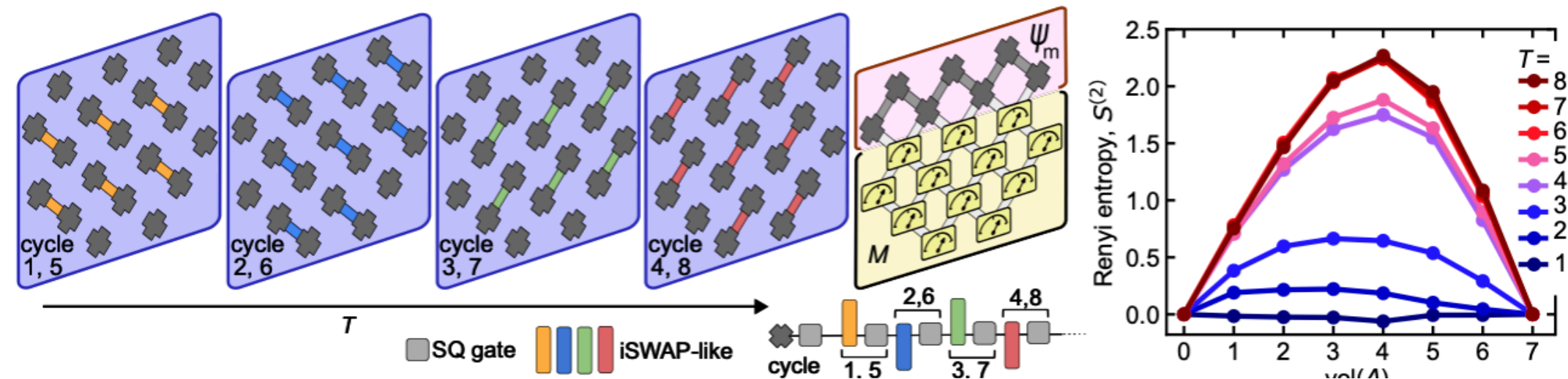


Hoke, Ippoliti...VK, Roushan, Nature (2023)

Li Chen Fisher (2018) Skinner Ruhman Nahum (2018)

Monitored Dynamics: Controlled Measurements

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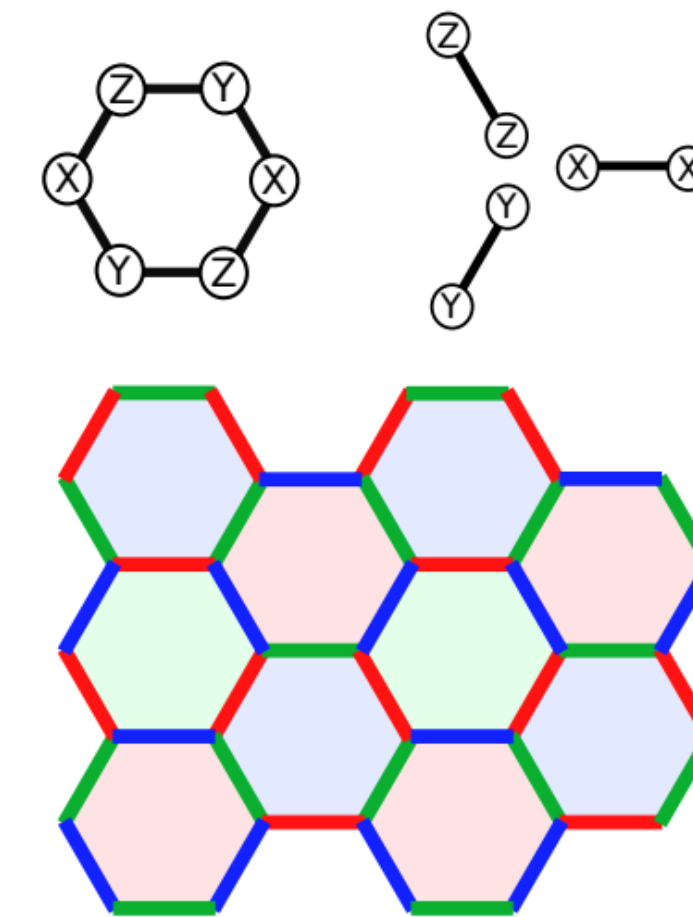
Measurement-only Dynamics

Ippoliti...VK PRX 2021

Lavasani, Alvirad, Barkeshli Nature Physics 2021

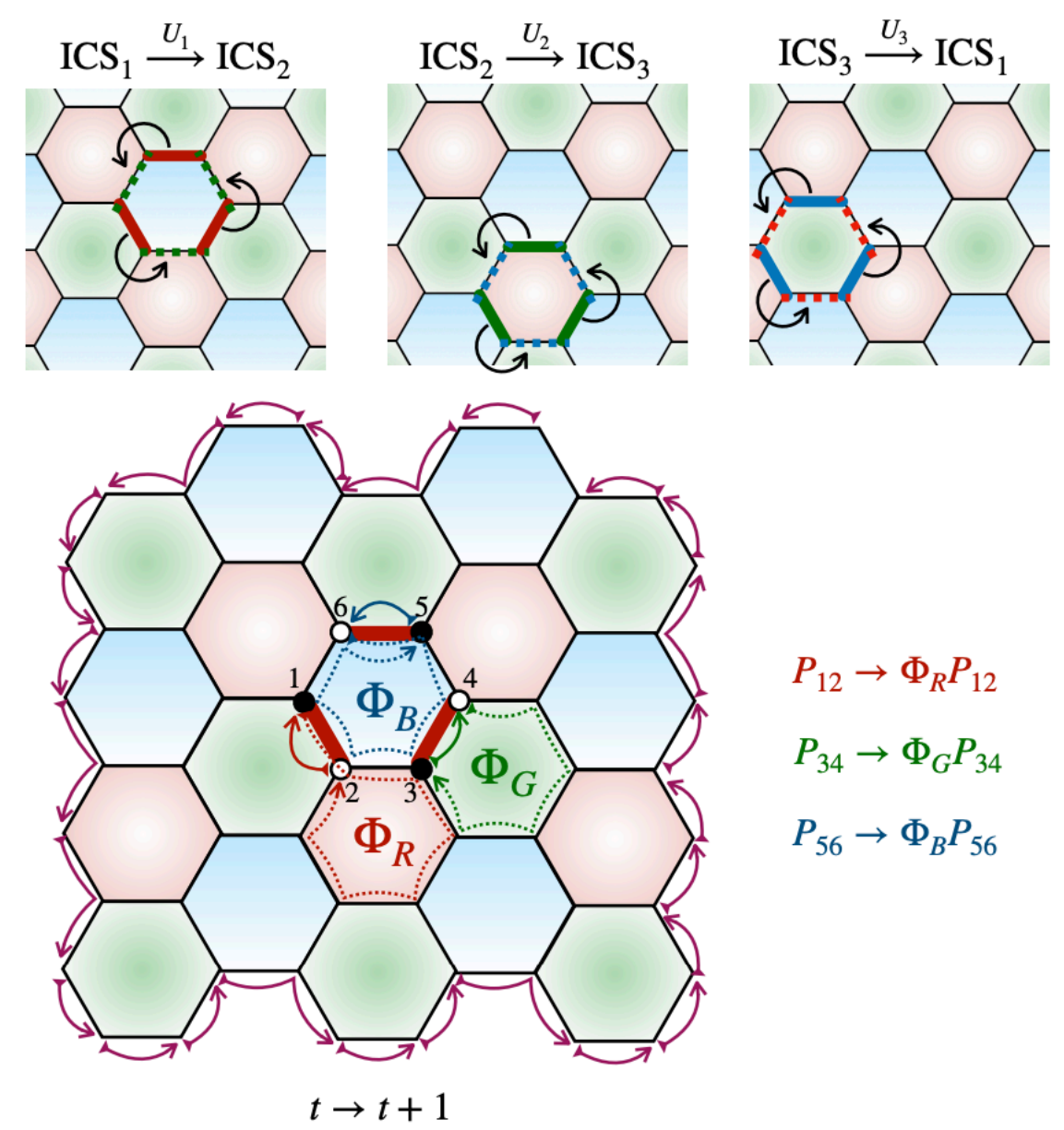
Sang Hsieh PRR 2021

Hastings-Haah Floquet Code (2021)



- Periodic sequence of **local measurements**
- **Dynamically generated error correcting code**
- Code and logical operators transform periodically in time
- $e \rightleftharpoons m$ automorphism after every period
 - “Topological” time-crystal

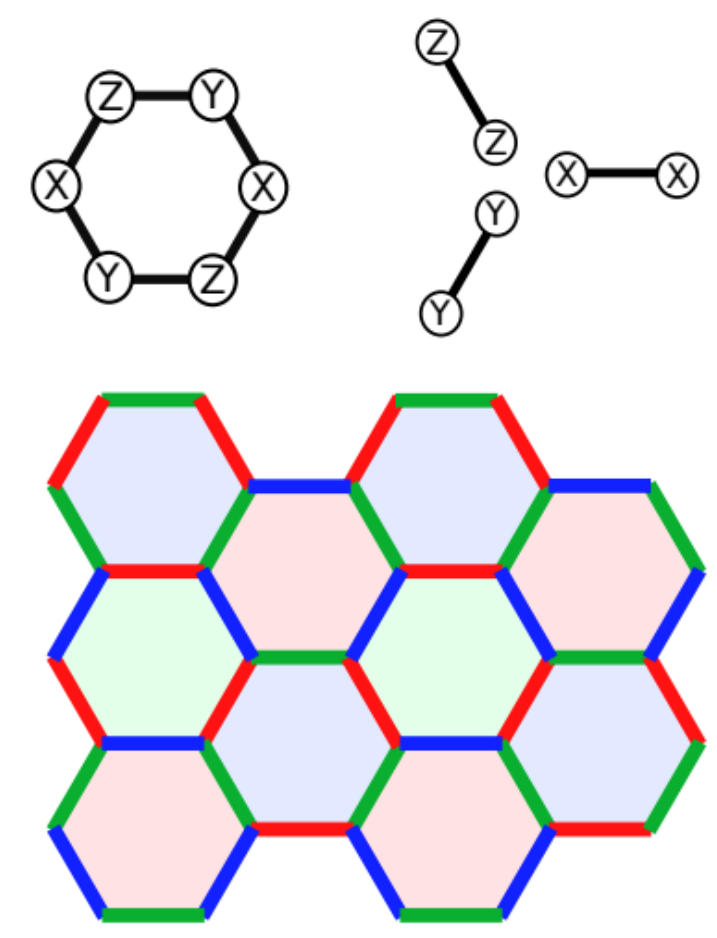
Unitary MBL Floquet Topological Order \leftrightarrow Measurement-only Floquet Code



MBL Floquet Topological Phase
(Po et al 2017)

\longleftrightarrow

Sullivan Wen Potter (2023)
Aasen Haah Li Wong (2023)
Roberts Vijay Dua (2023)



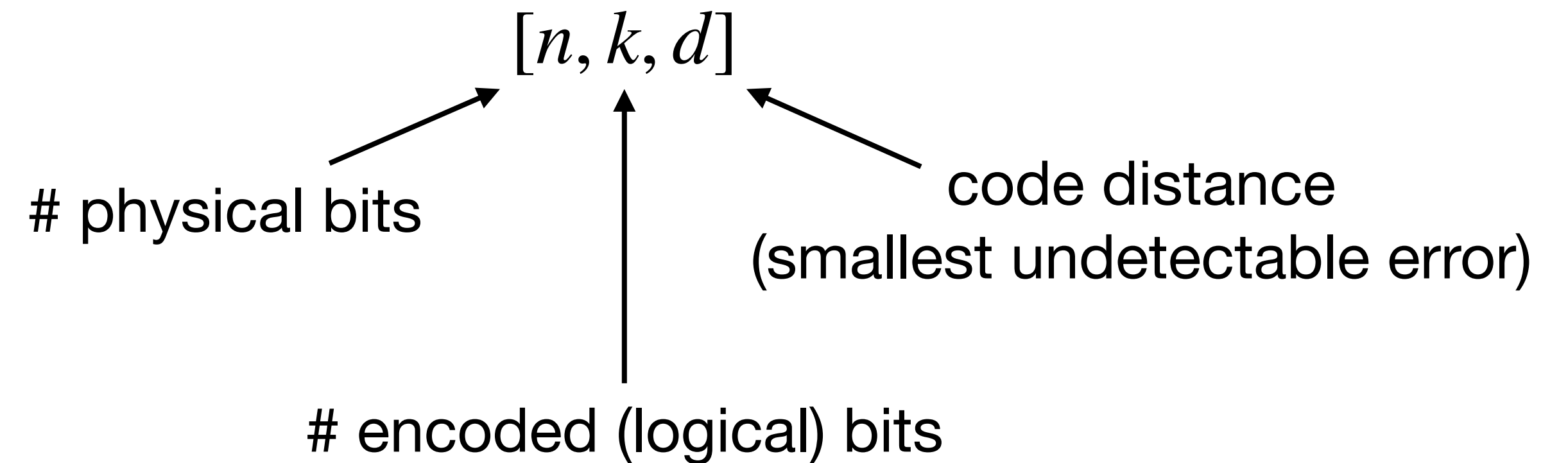
Measurement-only Floquet Code
(Hastings Haah 2021)

Controllable Geometry and Interactions

A recent theoretical breakthrough: good quantum LDPC codes

LDPC: every (qu)bit talks to only a finite number of (qu)bits

low density parity check



Good code:

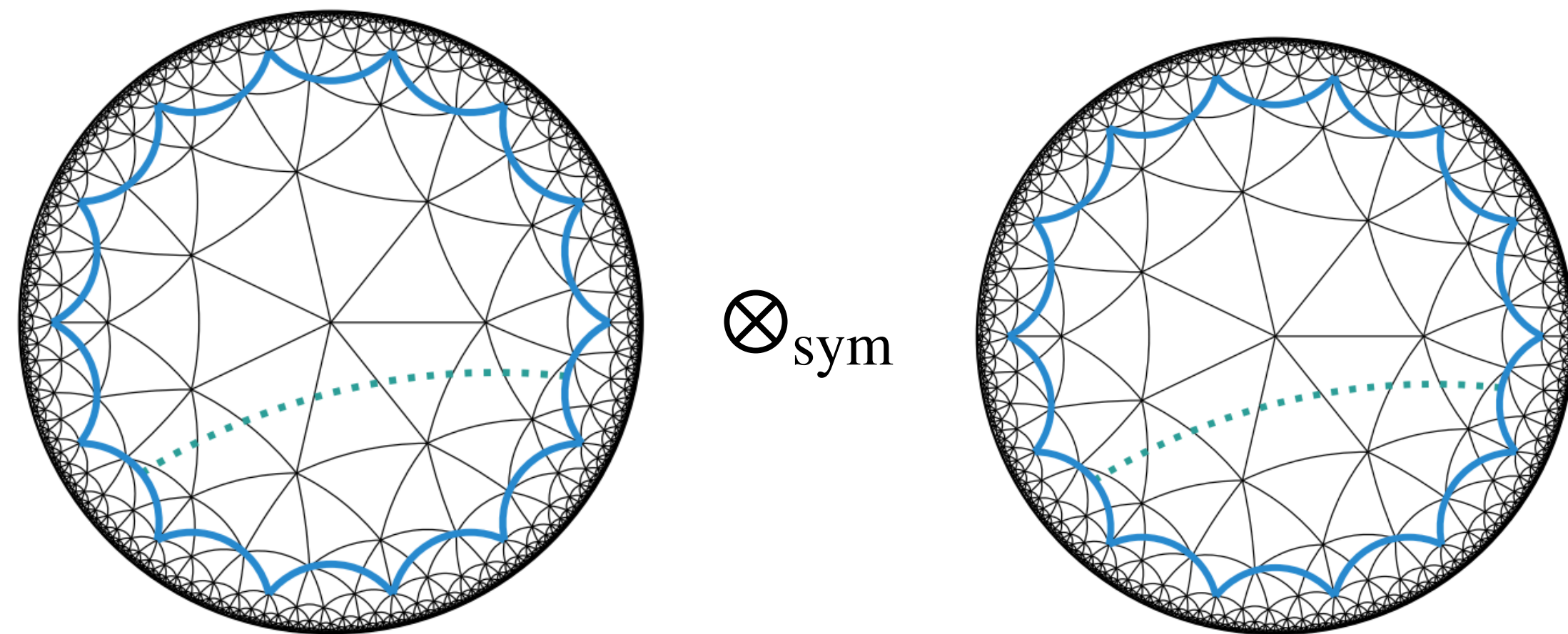
$k \propto n$ ← Low overhead!

$d \propto n$ ← Very robust!

Breuckmann Eberhardt 2021

Pantaleev, Kalachev 2021

Leverrier, Zemor 2022



Requires **expander graph**

boundary is proportional to volume

The Physics of LDPC Codes

Rakovszky VK (2023)

Rakovszky VK (2024)

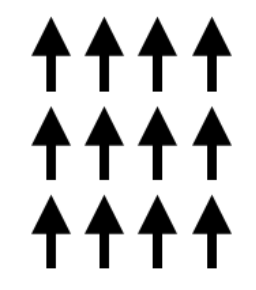
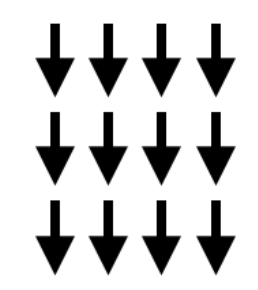
Placke Rakovszky Sommers Breuckmann VK (in progress)

Error Correcting Codes

Ordered Phases of Matter

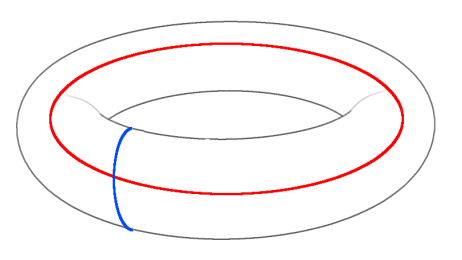
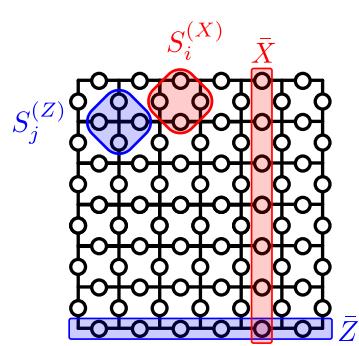


Classical Code (Repetition)



Symmetry Breaking

Quantum Code (Toric code)



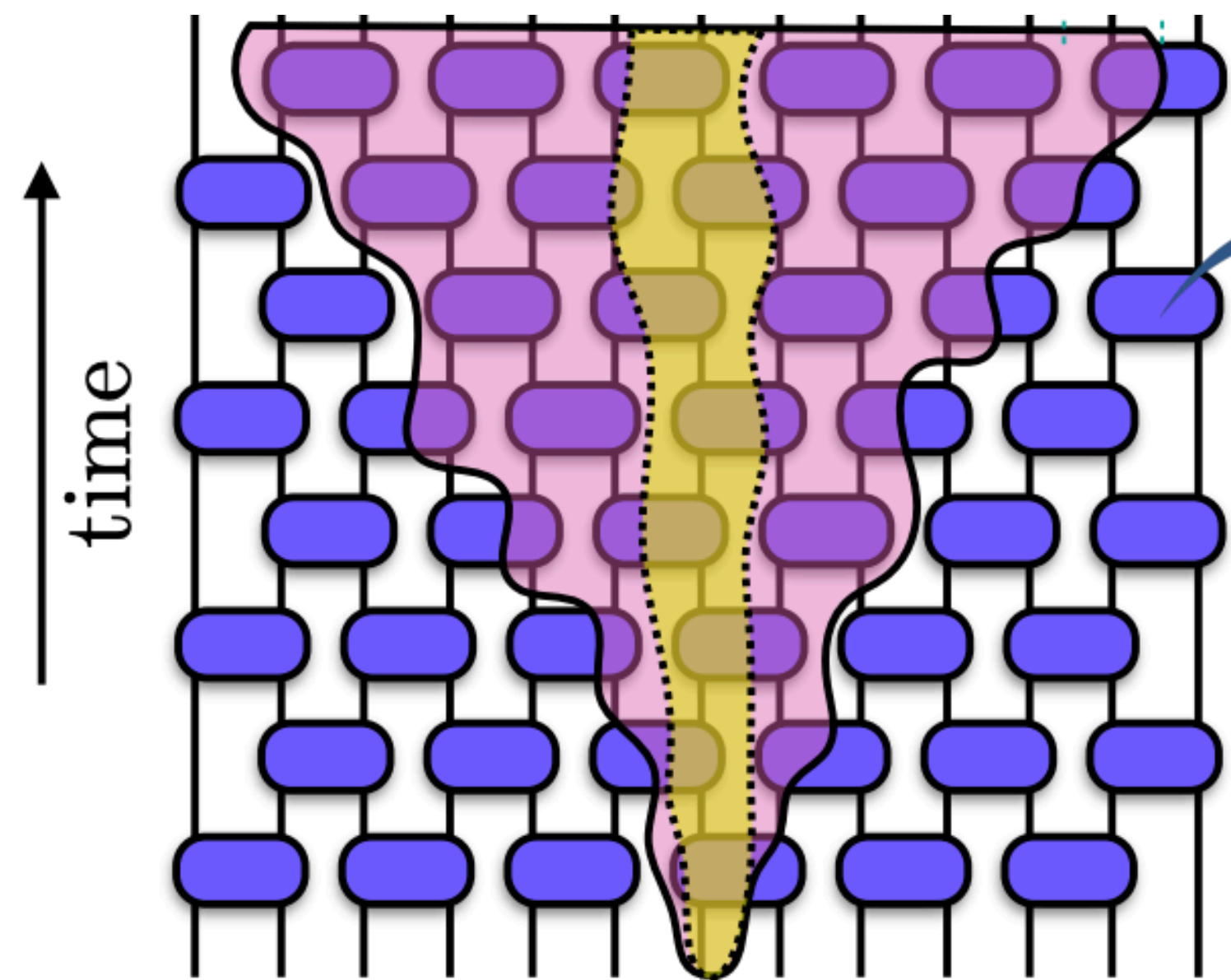
Topological Order

LDPC Codes

Novel gauge theories
and spin glasses

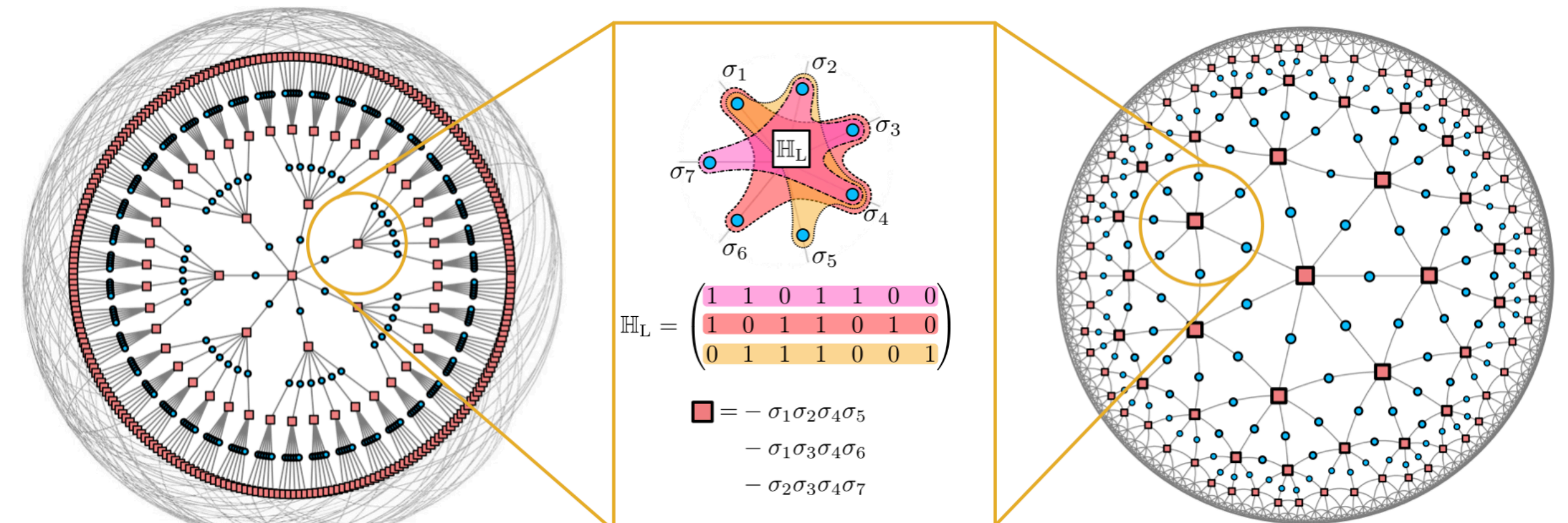
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Engineered interactions and **geometry**